

Theory of Sound

St. Paul's Cathedral

L. Rayleigh The problem of the whispering gallery, *Phil. Mag.*, **20**, 1001(1910)

Mie

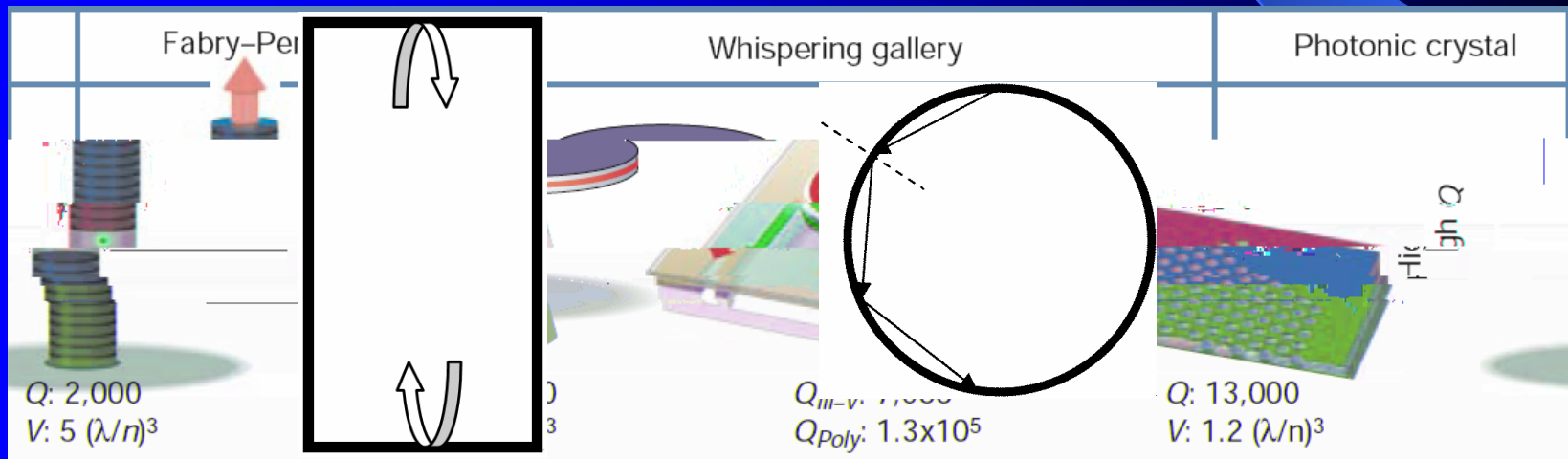
Light scattering at particle with



Mie G, Ann. Phys., 1908, 25(4):377

(Fabry-Pérot, FP) VCSEL
(Whispering-Gallery, WG)

(Photonic Crystal, PC)



K. J. Vahala, Nature vol.424, p. 839 (2003).

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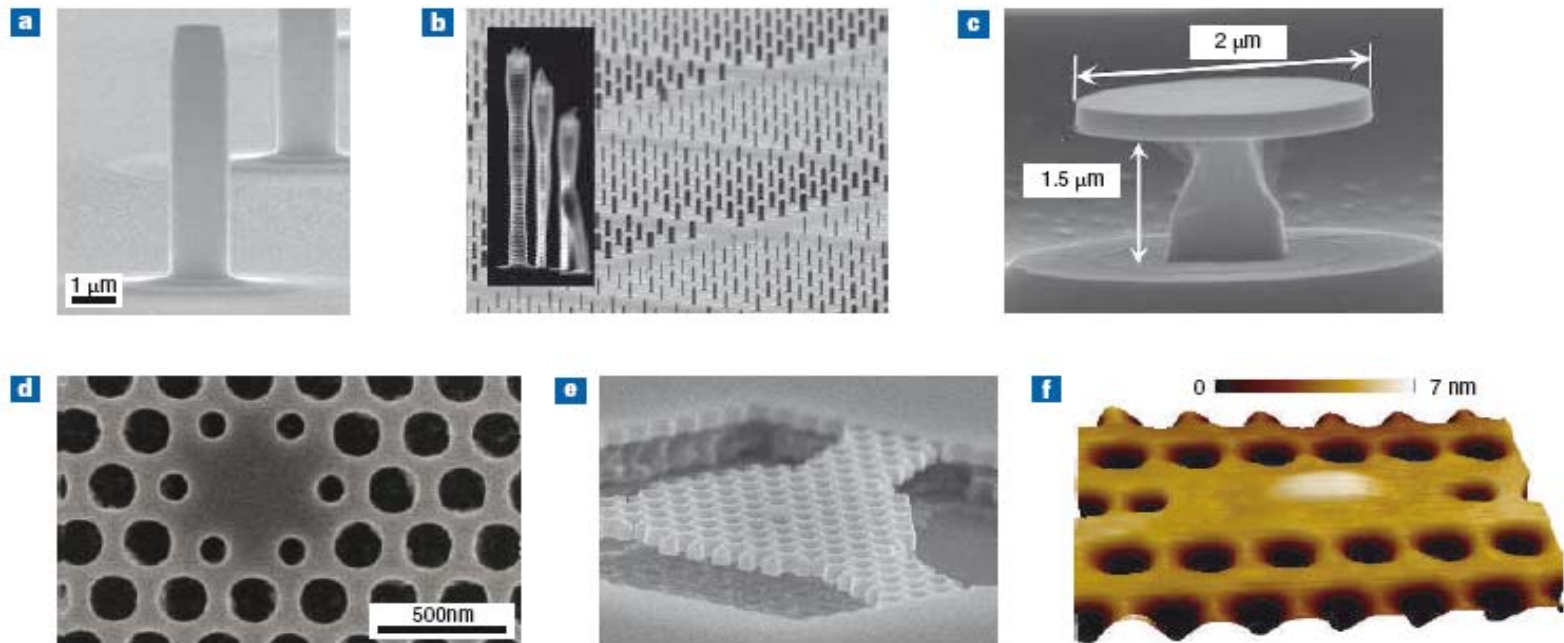
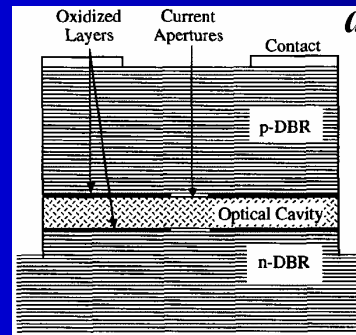


Figure 3 Scanning-electron-microscope images of semiconductor cavities. **a,b**, Pillar microcavities. **c**, microdisks. **d-f**, Photonic-bandgap defect cavities. The structures were fabricated at: **a**, University of Würzburg; **b,c,e**, CNRS-LPN (UPR-20); **d**, Univ. Cambridge; **f**, UCSB/ETHZ. (Image sources and permissions: **a**, Ref. 56. **c**, Ref. 51, copyright (2005) APS. **d**, Ref. 47, copyright (2006) AIP. **e,f**, Ref. 48)

A.

1. VCSEL

1979 InGaAsP 77K
1983 GaAs 77K
1988 850nm GaAs
1998 VCSEL



2

1992
1992
1993
1998
2000

150 A
40 A

1.

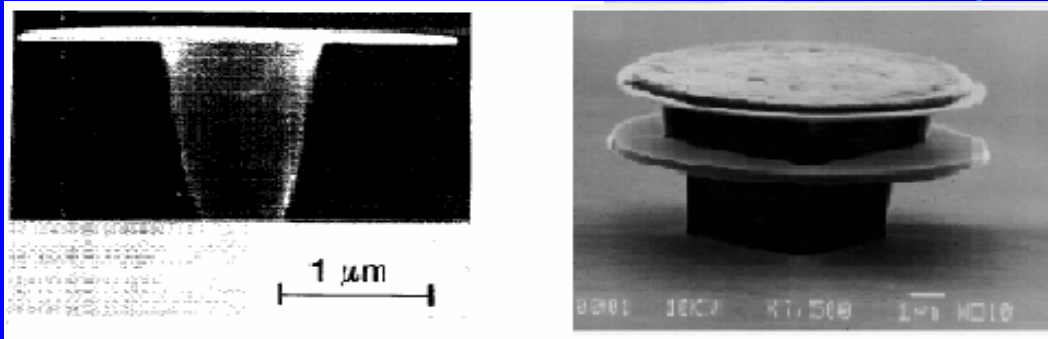
2.

3.

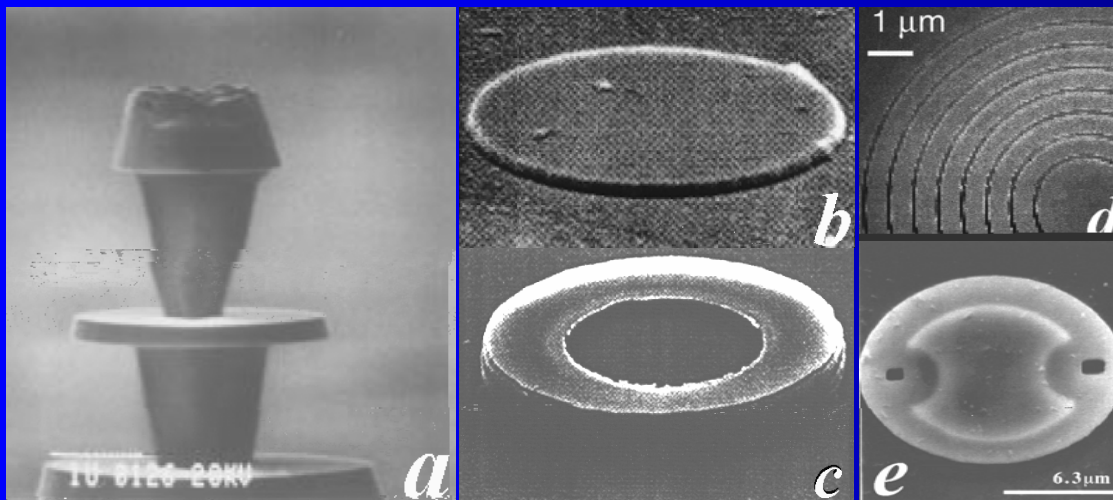
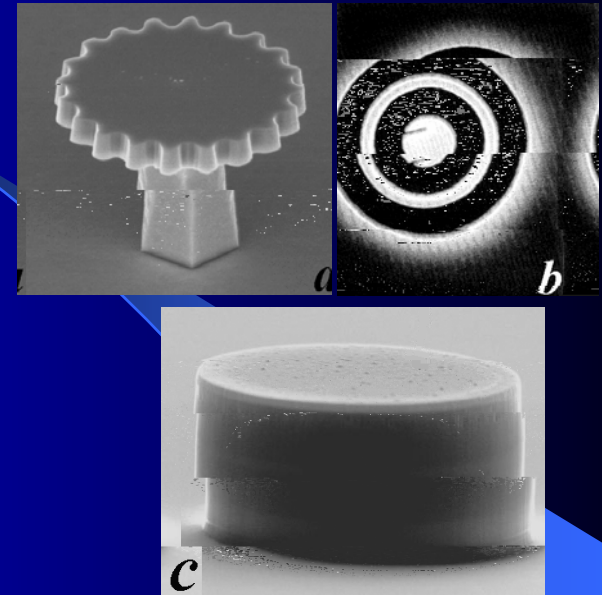
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Whispering-Gallery Mode (WGM)



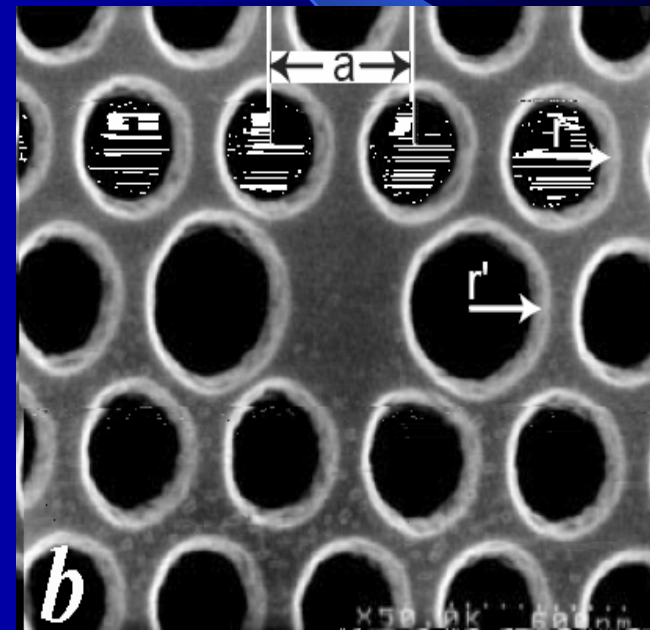
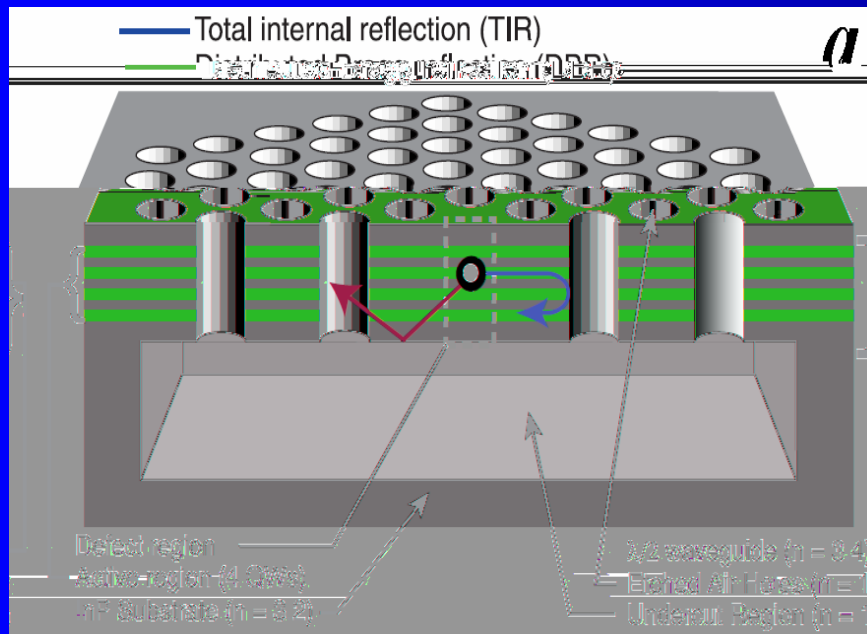
S. L. McCall et al, Appl. Phys. Lett., vol.60, 289
(1992), Electron. Lett., vol.28, p.1010(1992)



P. Michler et al, Science, vol.
290, p.2282(2000)

1999
2000
2004

6.75mW
300 μ A
0.25



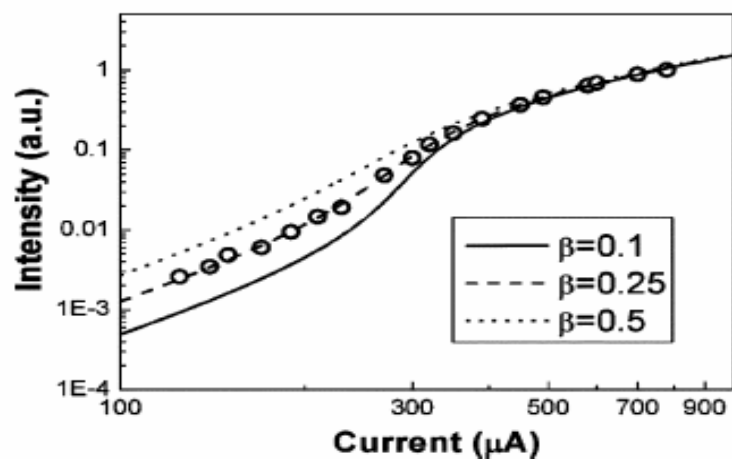
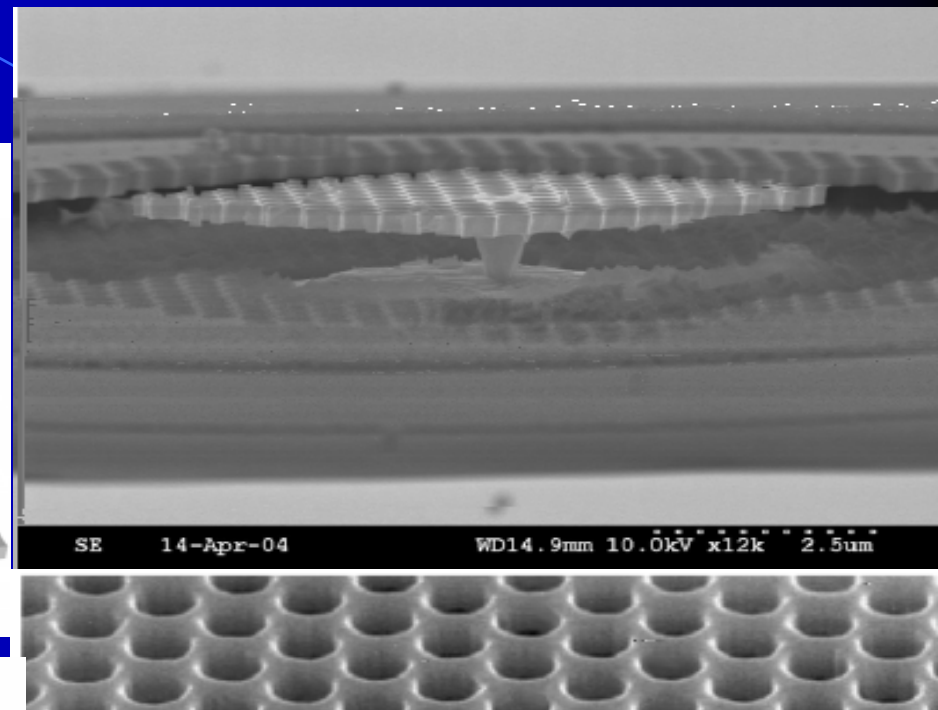
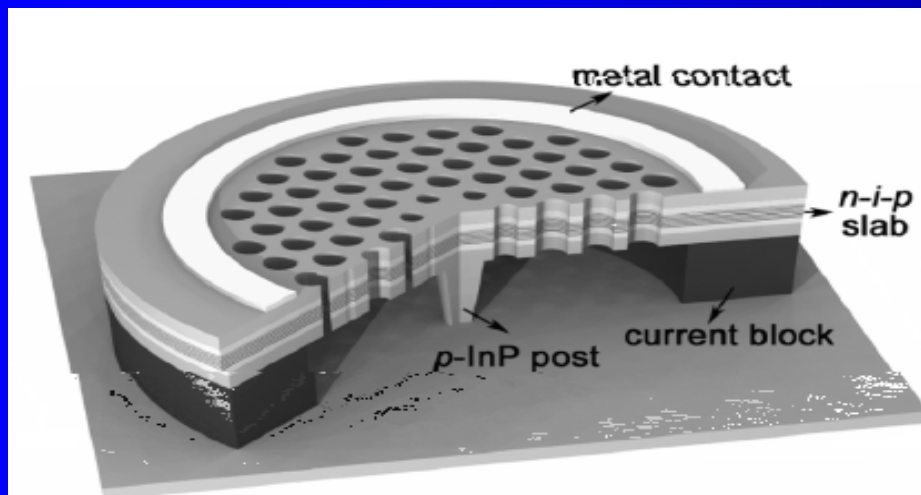
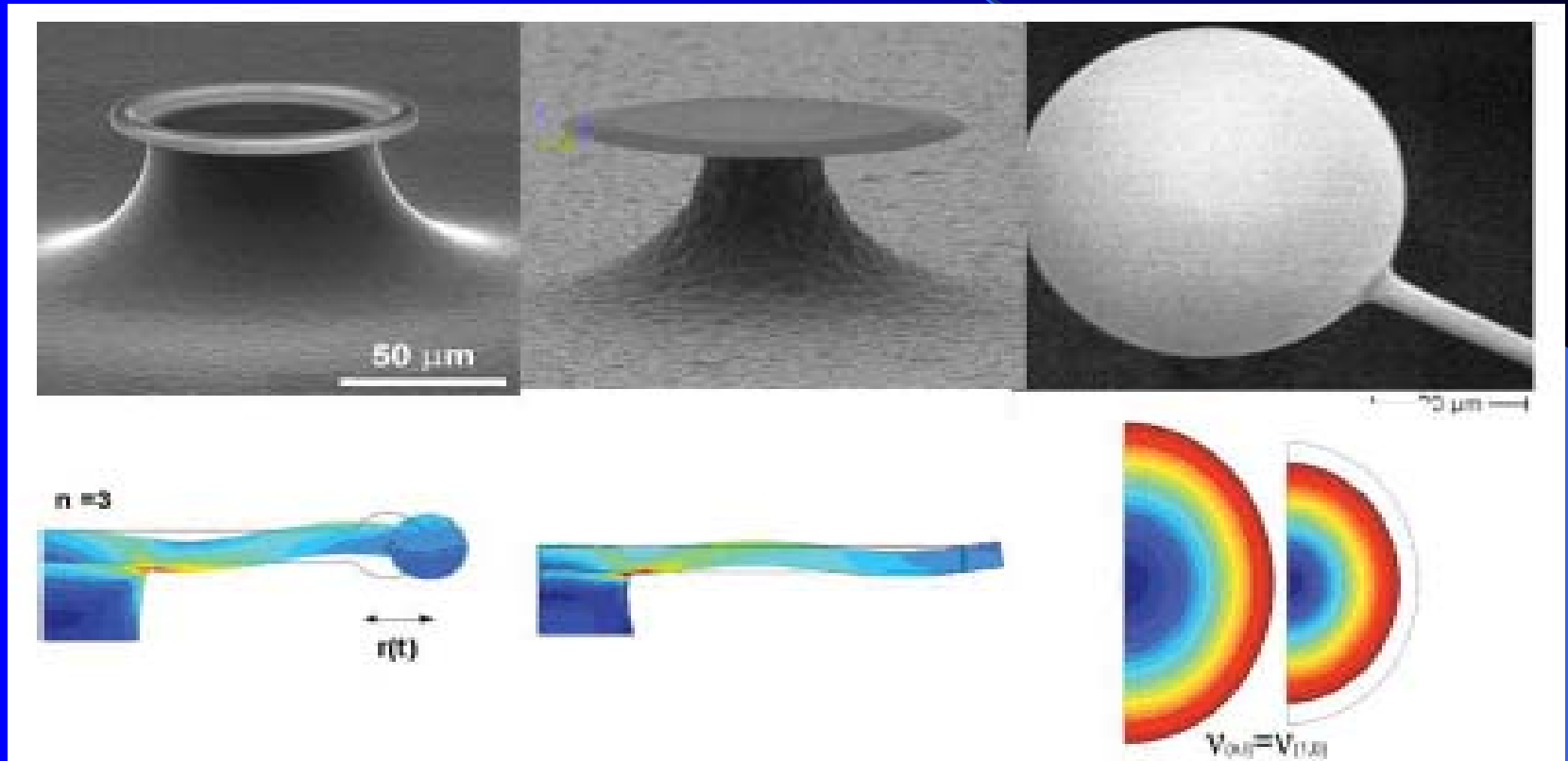


Fig. 14. Comparison of the measured $L-I$ curves (dots) with those obtained from the rate equations (lines) for the monopole mode.

The coupling of mechanical and optical degrees of freedom via radiation pressure has been a subject of early research in the context of gravitational wave detection.



T.J. Kippenberg and K.J. Vahala, “Cavity opto-mechanics” Optics Express, vol.15, p.17172(2007)

K. Hennessy, et al, “Quantum nature of a strongly coupled single quantum dot–cavity system,” Nature, vol.445, p.896(2007)

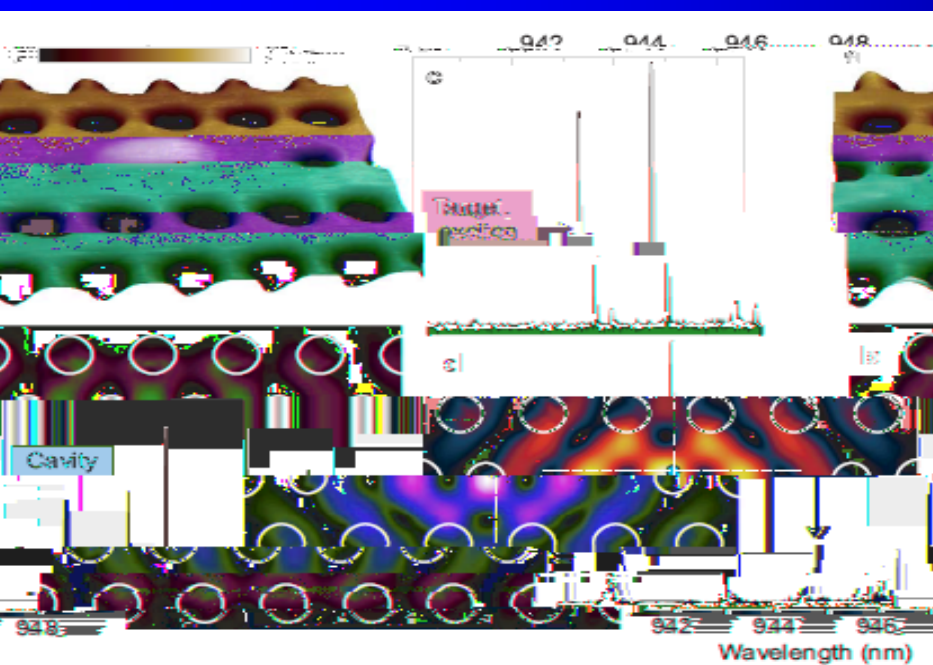


Figure 1 | Positioning a photonic crystal cavity mode relative to a single quantum dot. **a**, False-color scanning electron micrograph of the photonic crystal surface. The height scale is depicted by the colour bar. **b**, Electric field intensity of photonic crystal cavity mode showing that the location of the buried quantum dot, indicated by the teal dot, overlaps the field maximum. The field intensity ranges from zero (black) to a maximum (white), going through blue, red, and yellow. **c**, Photoluminescence spectrum before cavity fabrication of a single quantum dot, which was selected for cavity coupling on the basis of clear emission from a few discrete excitonic transitions. **d**, Photoluminescence spectrum from the same quantum dot after cavity fabrication, showing emission from the cavity at 942.5 nm.

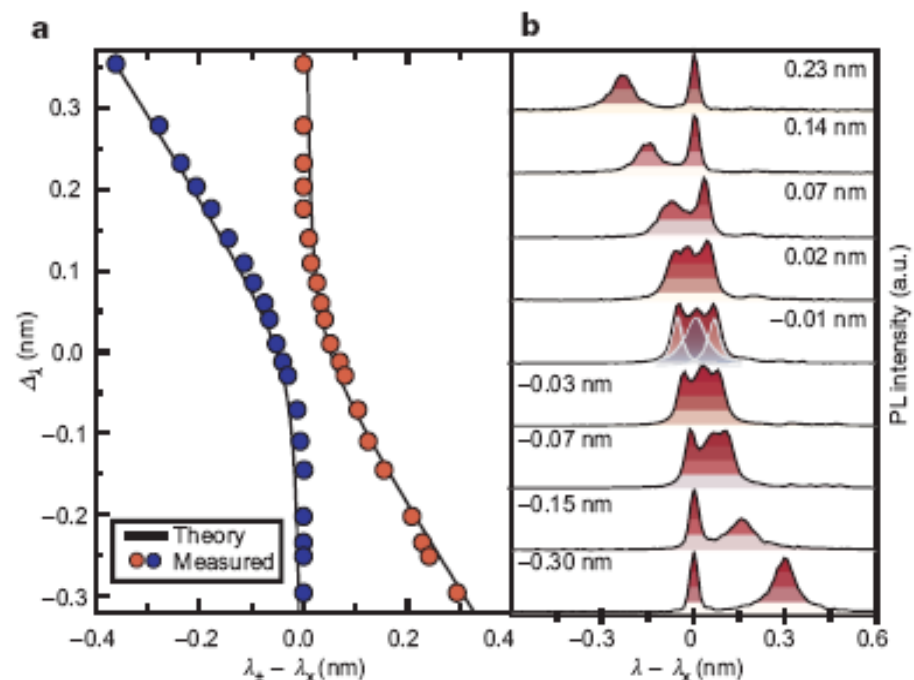
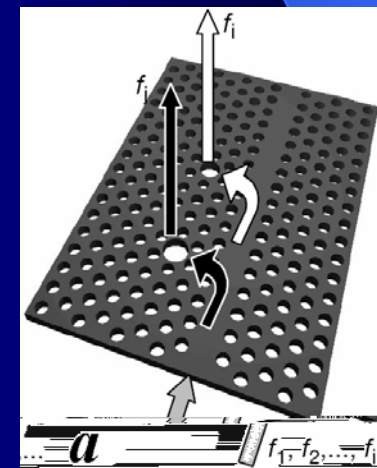
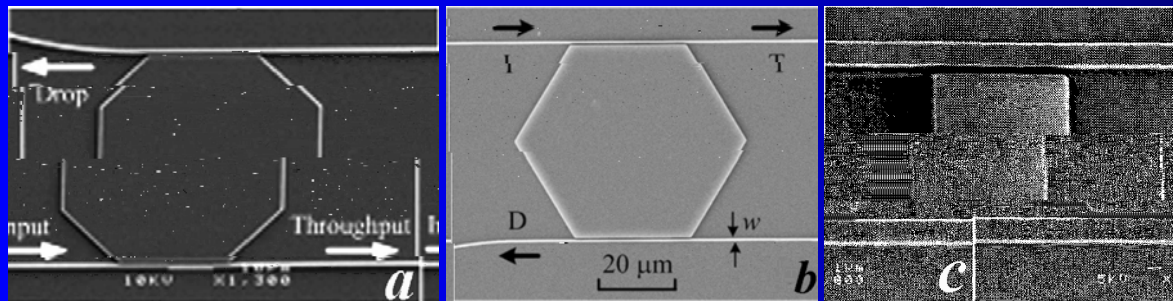
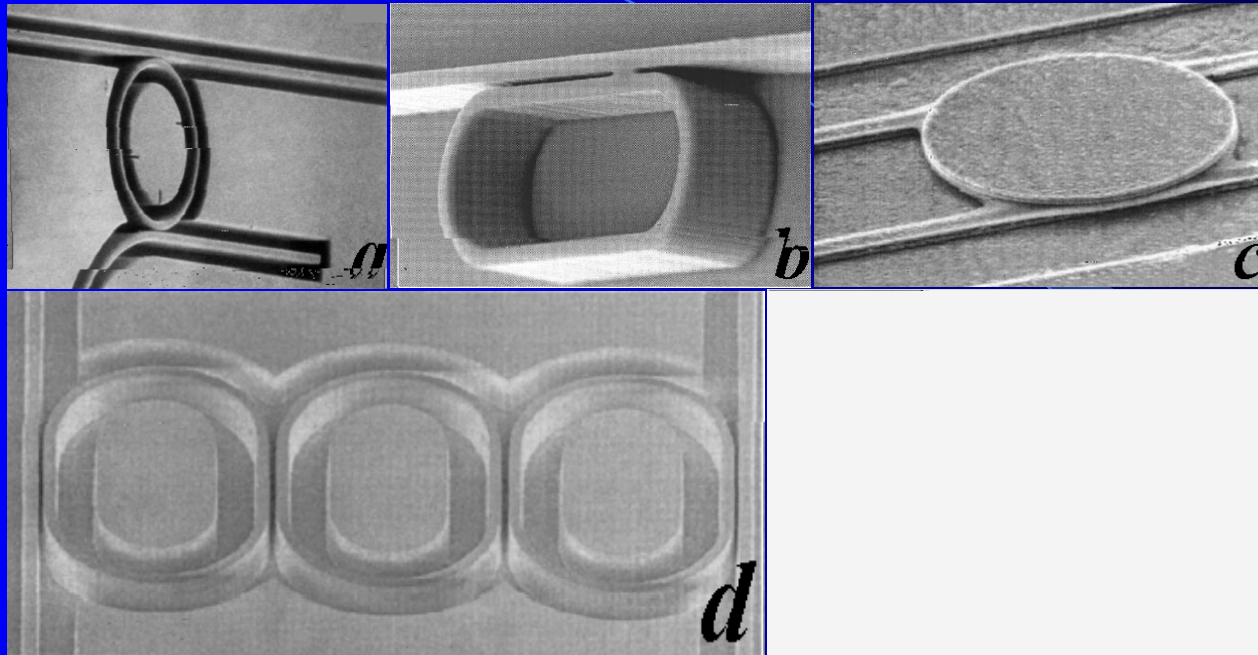


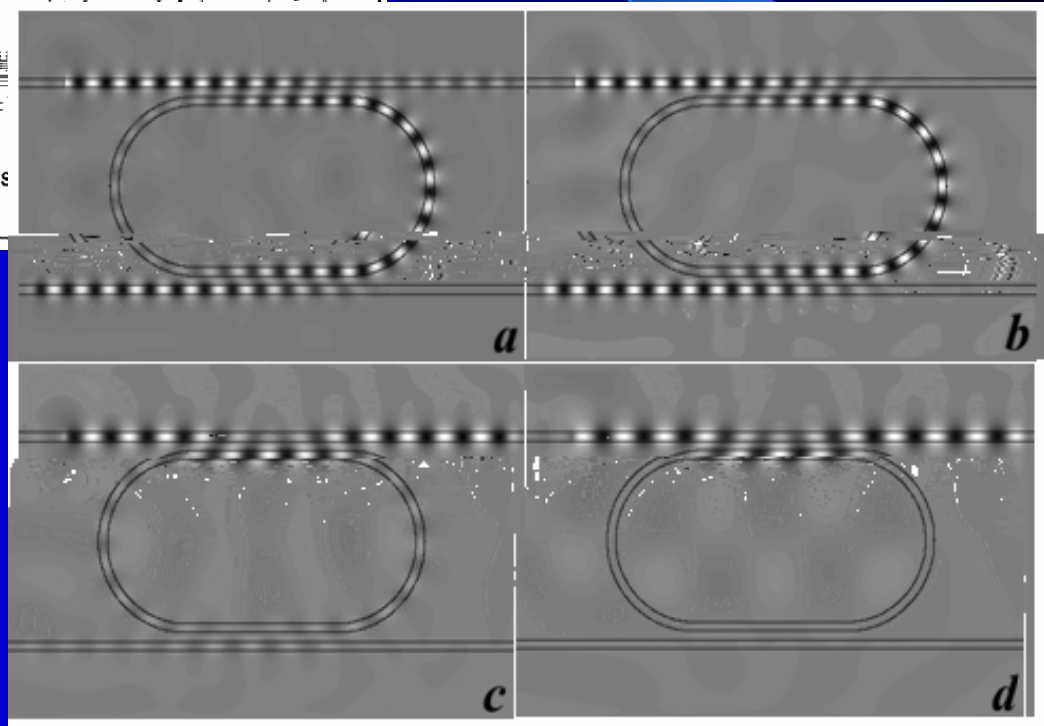
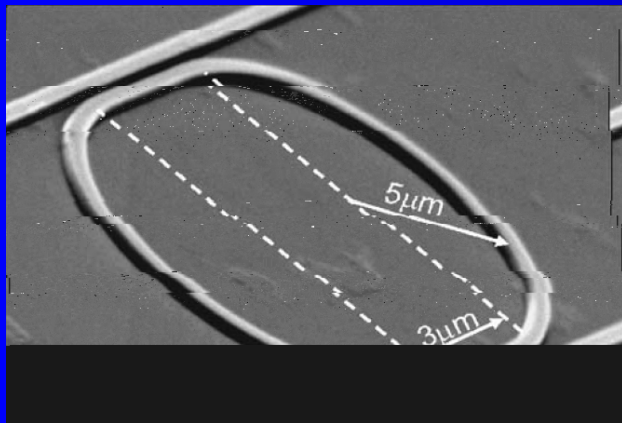
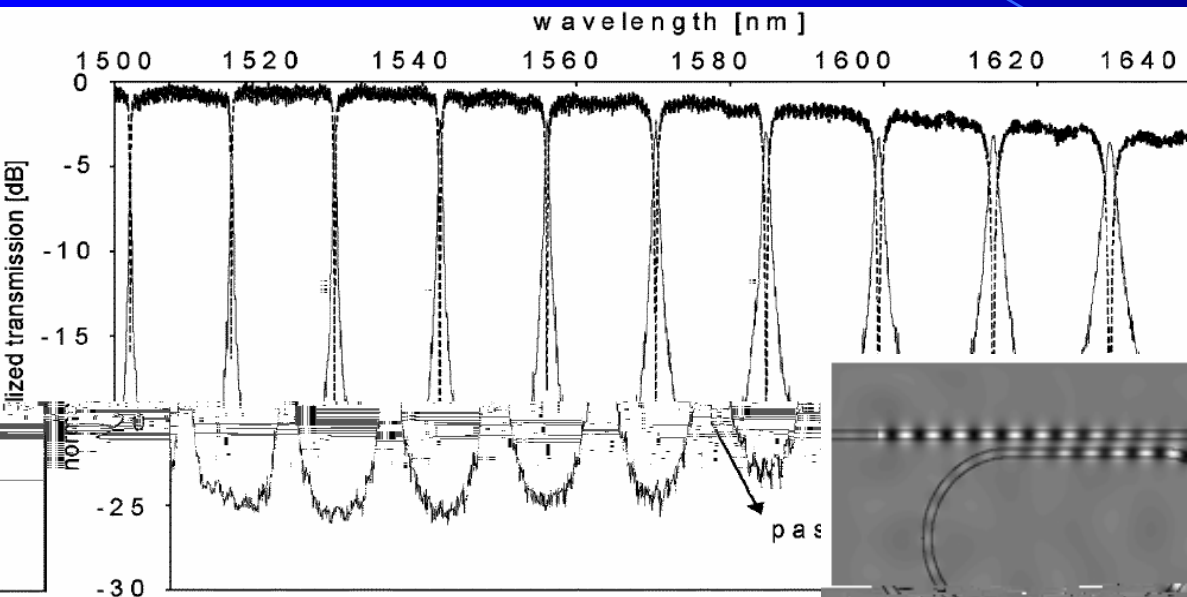
Figure 3 | Characteristics of the strong-coupling regime in the spectral domain. **a**, Wavelength of the polaritons for various detunings, $\Delta\lambda$. Calculated spectral peak positions describing the strongly coupled system are plotted as solid lines, with measured peak positions extracted from photoluminescence plotted in red and blue dots. **b**, Spectra of the two anticrossing polariton states near zero detuning. An additional peak is identified as the pure photonic state of the cavity. Values of $\Delta\lambda$ are shown for each spectrum. PL, photoluminescence; a.u., arbitrary units.

B.

zzz



微腔光学滤波器：



Q. Xu, et al, "Micrometre-scale silicon electro-optic modulator," Nature, vol.435, p.325(2005)

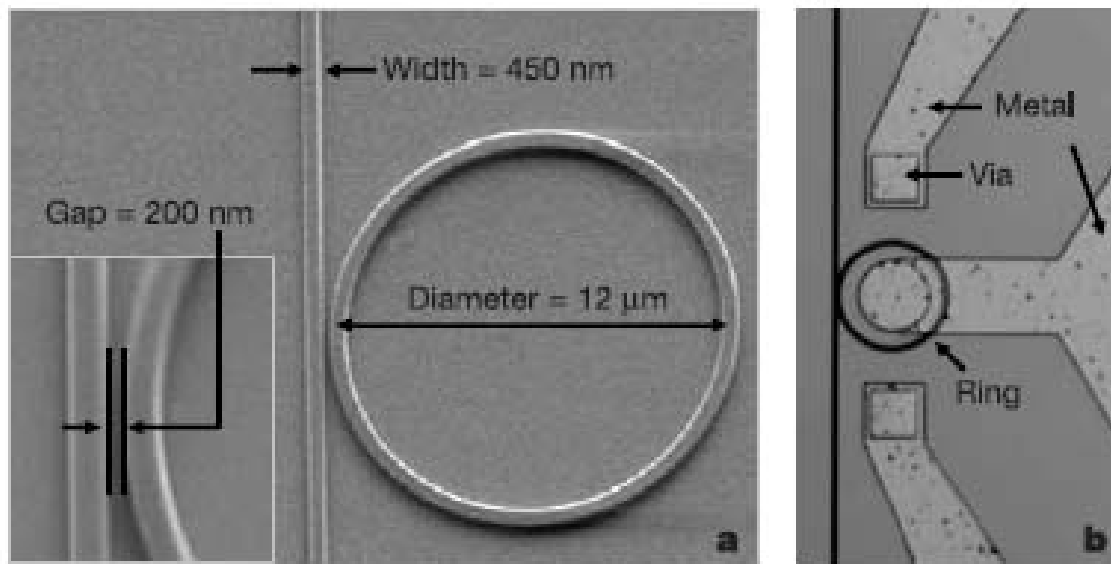
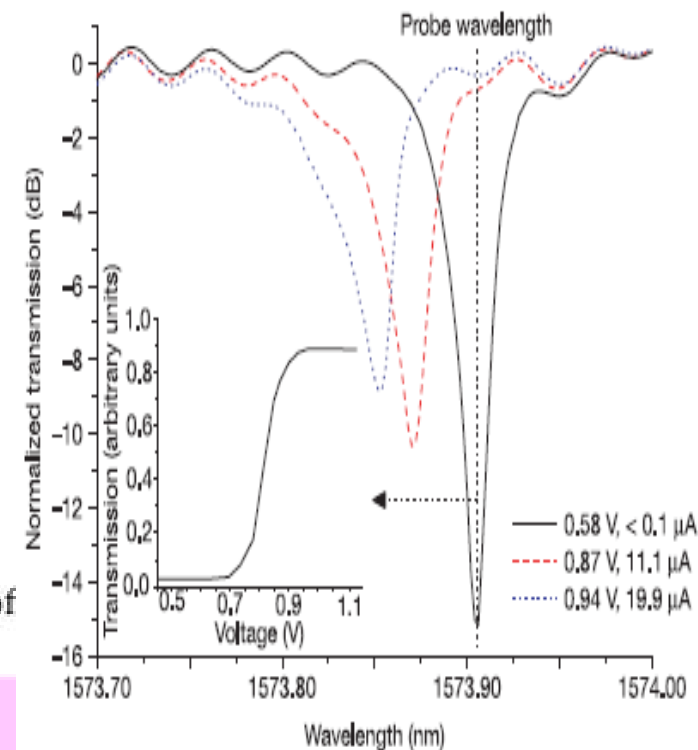


Figure 2 | SEM and microscope images of the fabricated device. a, Top-view SEM image of the ring coupled to the waveguide with a close-up view of the coupling region. **b,** Top-view microscope image of the ring resonator after the metal contacts are added. The metal contact on the central p-doped region of the ring goes over the ring with a 1- μm -thick silicon dioxide layer between the metal and the ring.



K.Preston, et al, Opt. Exp., vol.15, p.17284(2007)

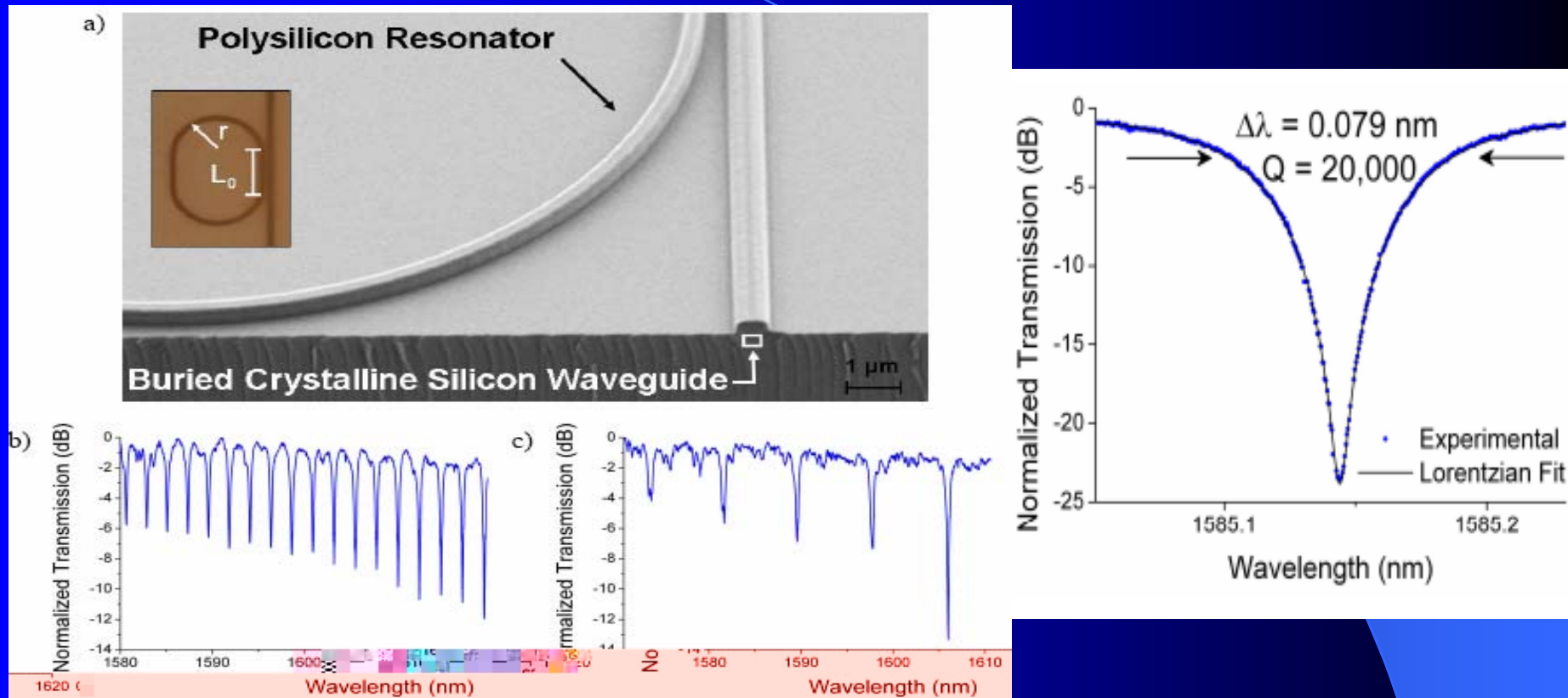


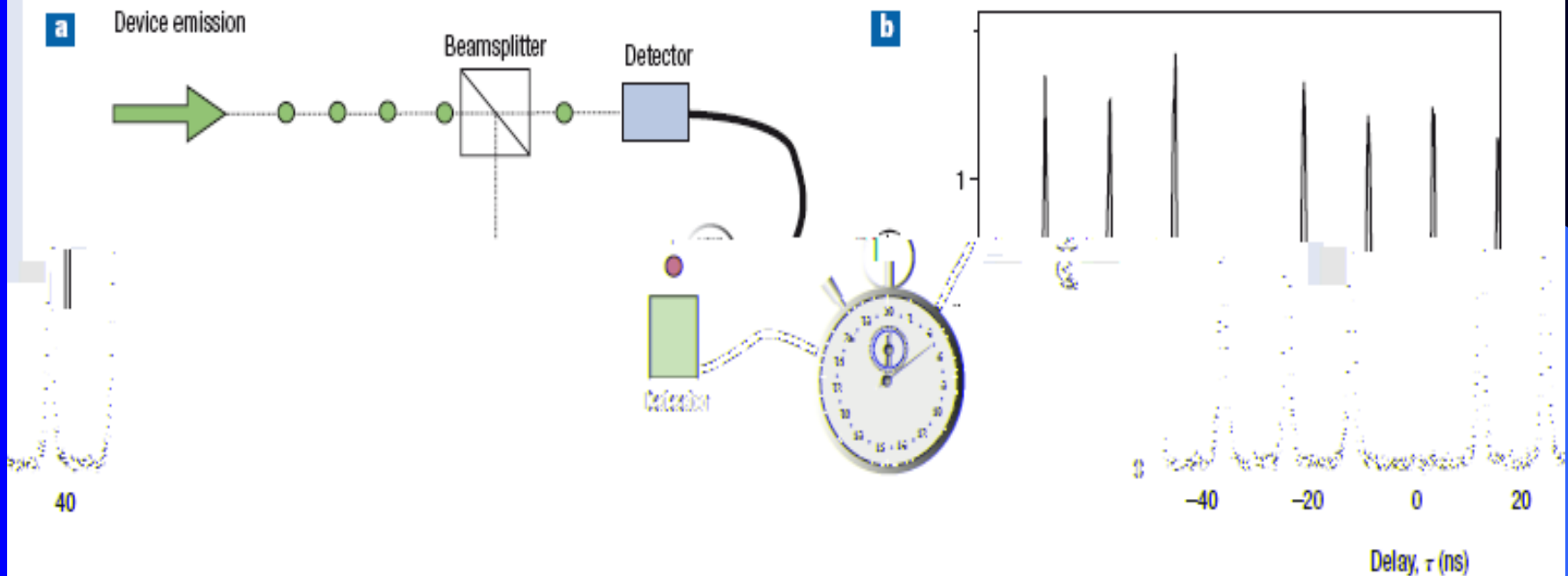
Fig. 5. Polysilicon racetrack resonators coupled to crystalline silicon waveguides. (a): Cross section SEM of the structure before oxide cladding. Inset: Definition of r and coupling length L_0 . (b) and (c): Quasi-TM polarized transmission as a function of wavelength for (b) $r = 40 \mu\text{m}$, $L_0 = 3 \mu\text{m}$ and (c) $r = 10 \mu\text{m}$, $L_0 = 5 \mu\text{m}$.

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$$g^{(2)}(\tau) = \langle I(t)I(t+\tau) \rangle / \langle I(t) \rangle^2$$

Box 1 Photon-correlation measurements

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Figure B1 Measuring the correlation. **a**, Schematic of the set-up used for photon-correlation measurements. **b**, Second-order correlation function $g^{(2)}(\tau)$ for the exciton emission of a single dot in a pillar microcavity. Reproduced with permission from ref. 41. Copyright (2005) OSA.

A. J. SHIELDS, "Semiconductor quantum light sources," Nature Photonics, vol.1, p.215(2007)

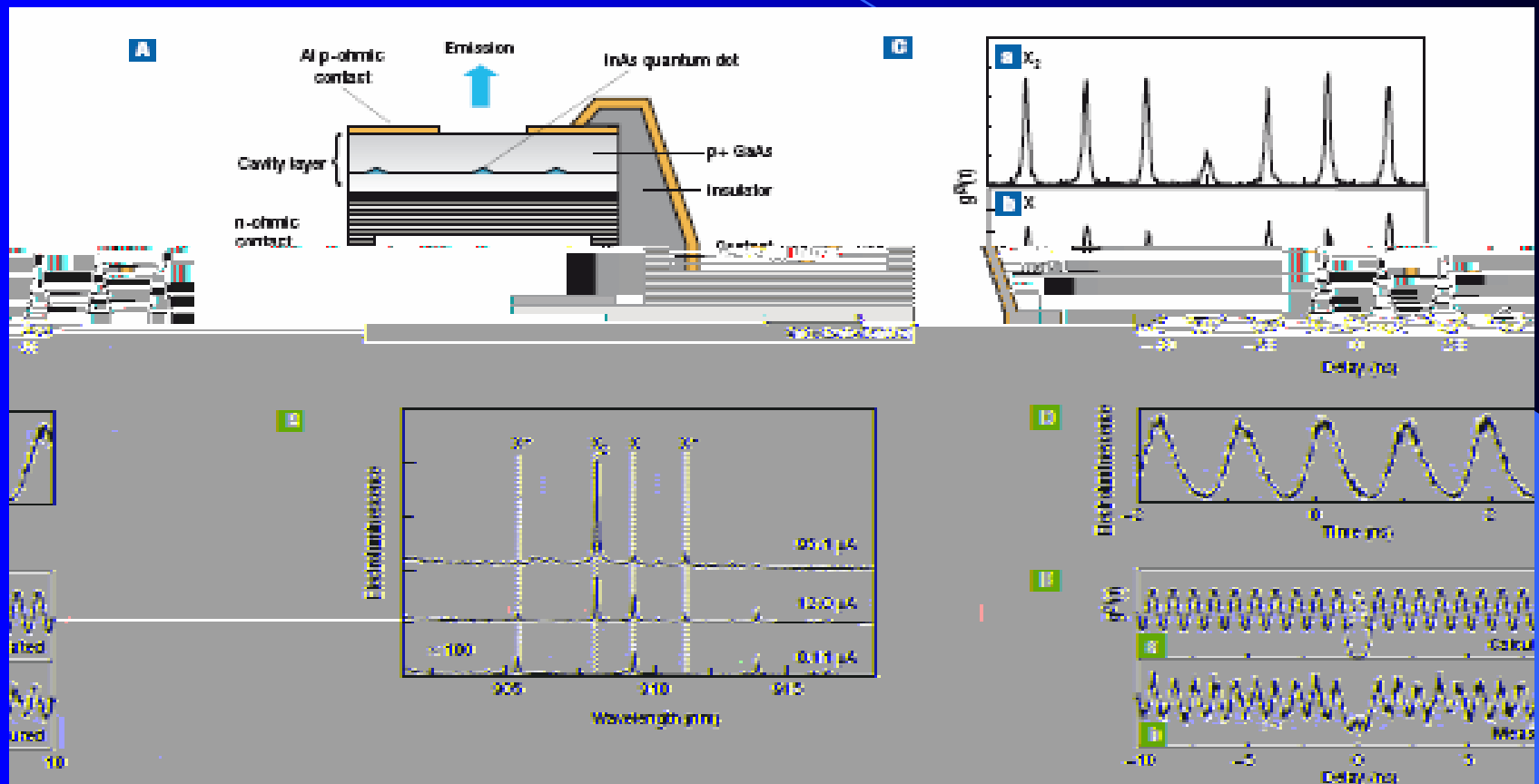
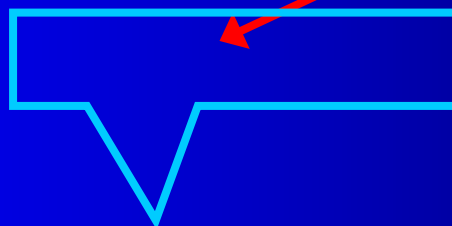
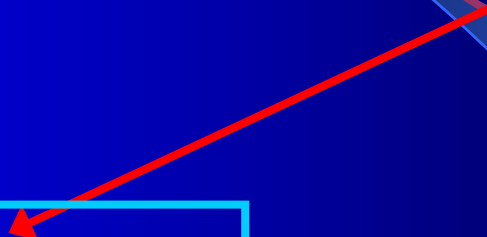
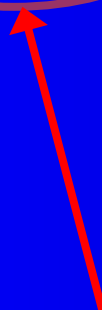
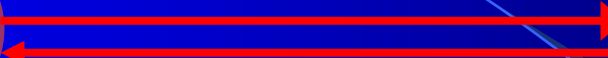
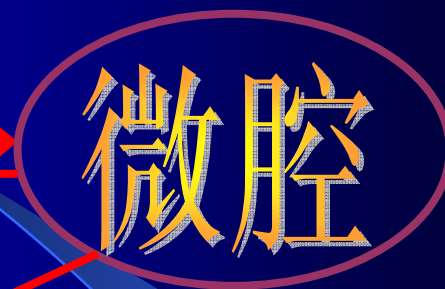
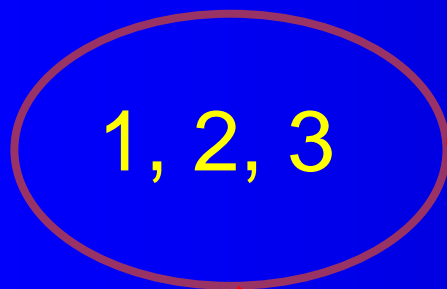
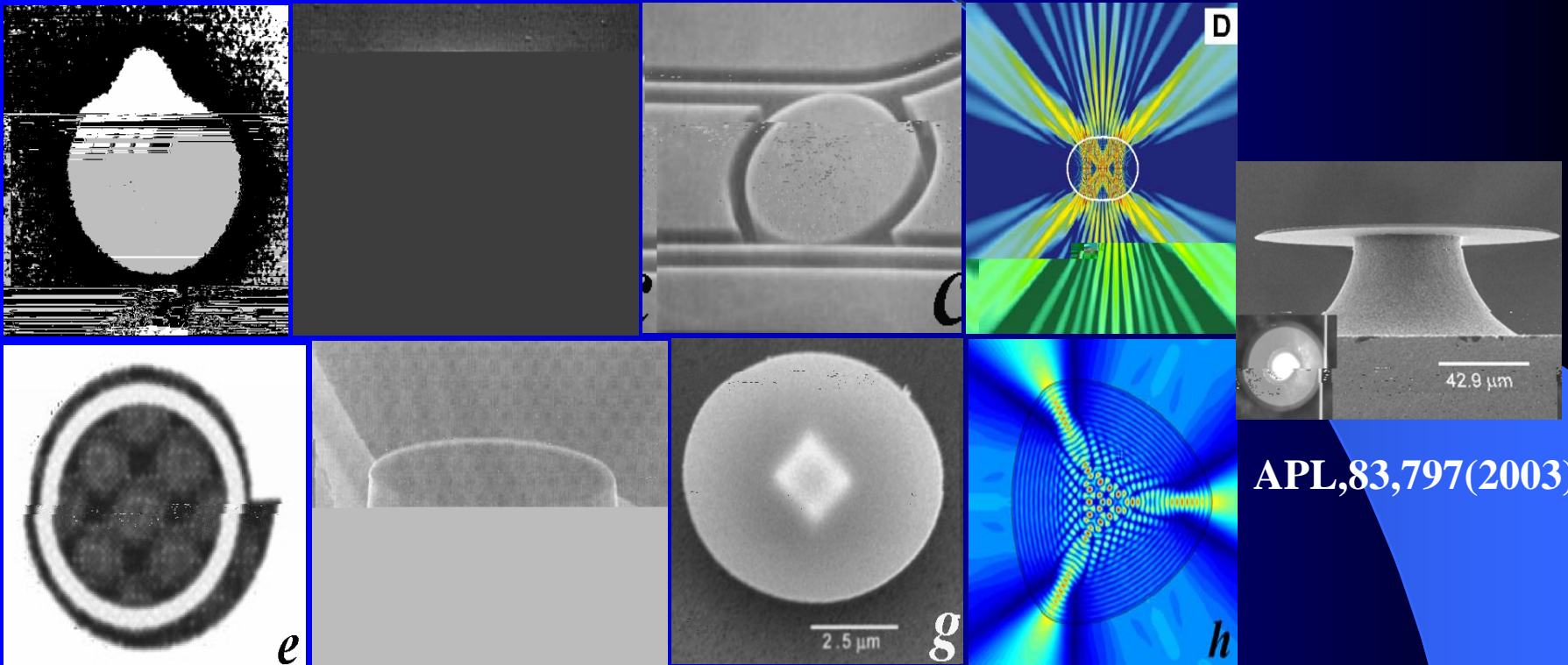


Figure 5.9 Self-exciton-polariton lasing emission. **A**, Schematic diagram of the device structure. **B**, Plot of $p(V)$ versus Delay (ps) showing self-exciton-polariton lasing emission. **C**, Plot of Electroluminescence versus Wavelength (nm) showing self-exciton-polariton lasing emission. **D**, Plot of Electroluminescence versus Time (ns) showing self-exciton-polariton lasing emission. **E**, Plot of $p(V)$ versus Delay (ps) showing self-exciton-polariton lasing emission.



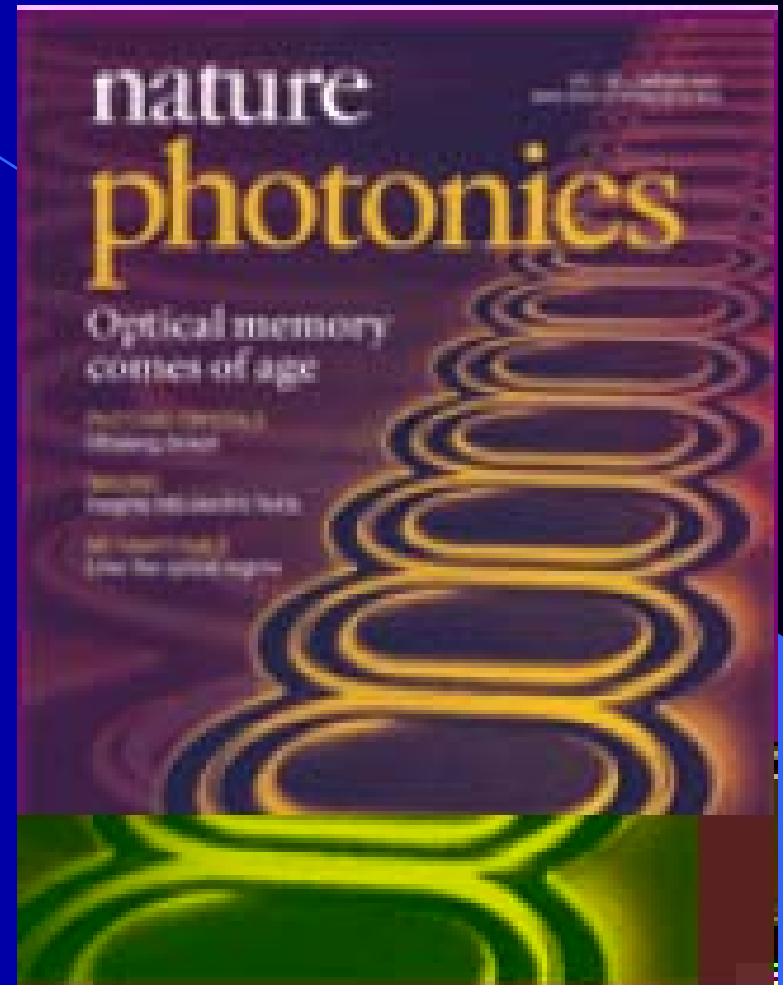
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Methods for obtaining directional emission



APL,83,797(2003)

Appl.Phys. Lett., (a)62, 561(1993), (b)65,3167(1994), (e)83, 1710(2003),(g)84, 861(2004); (c)J. Lightwave. Technol., 15, 2154(1997); (d) Science, 280, 1556(1998); (f) IEEE Photon. Technol. Lett., 15,1330(2003); (h) Phys. Rev. Lett., 93, 133902(2004)



VG

S.-Y.Lee, “Quasiscarred Resonances in a Spiral-Shaped Microcavity,”
Phys. Rev. Lett., vol.93, 164102(2004)

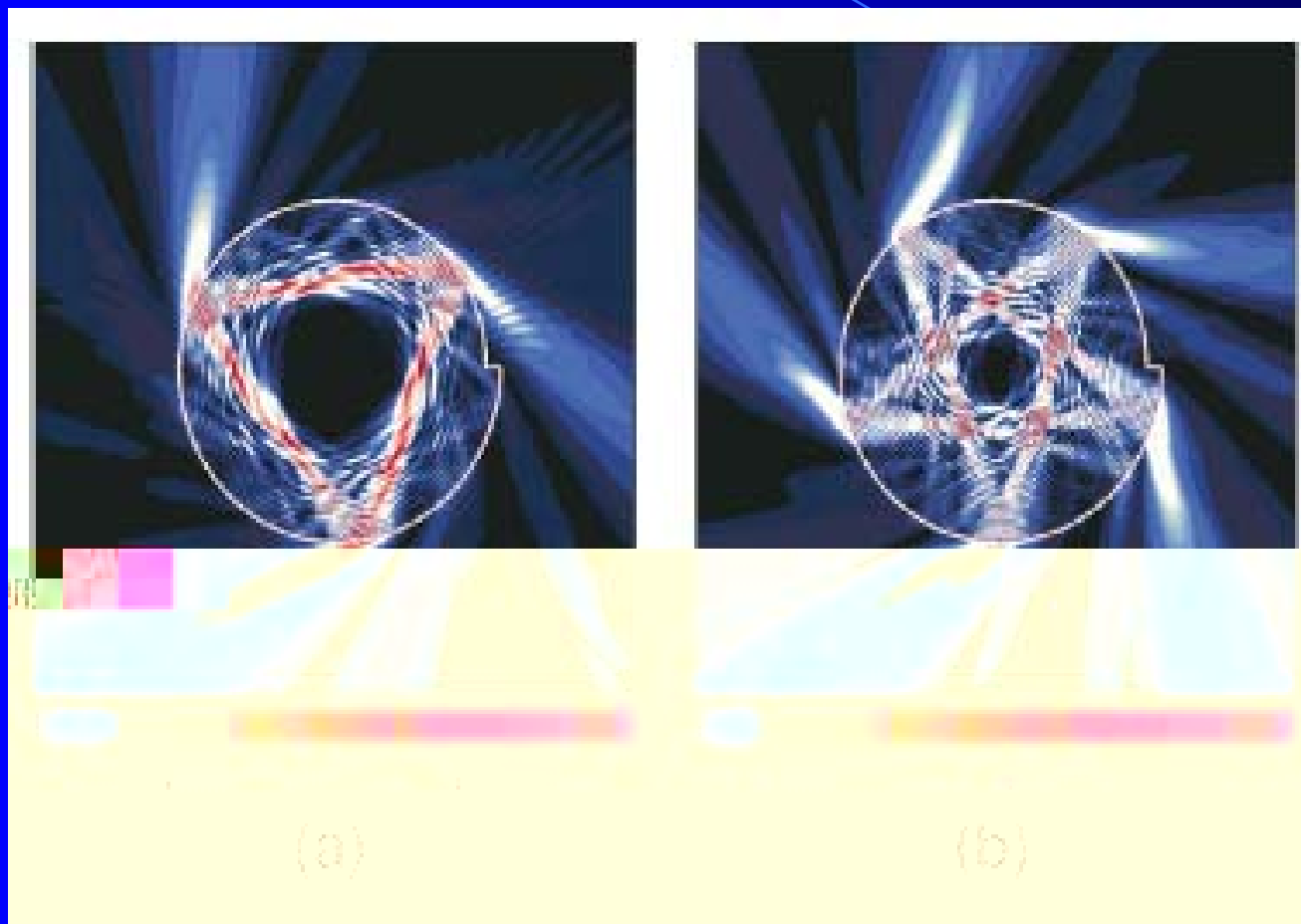
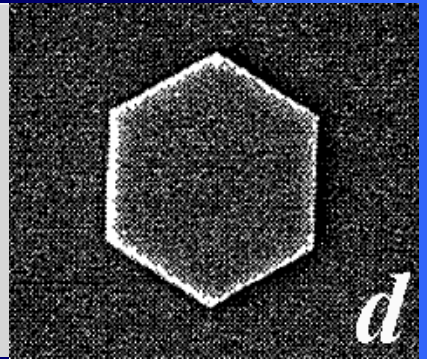
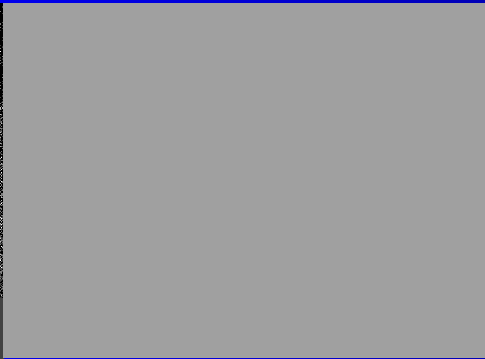
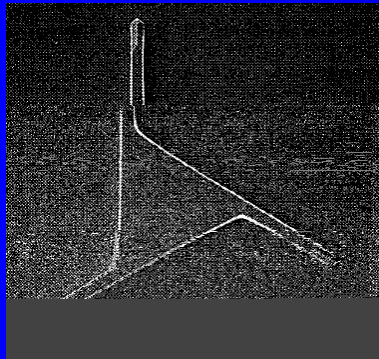
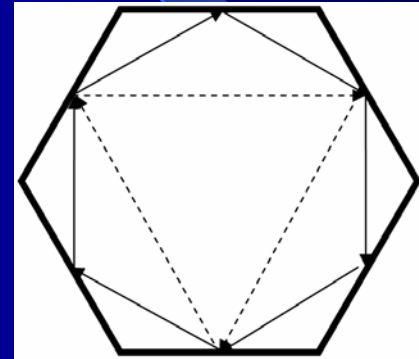
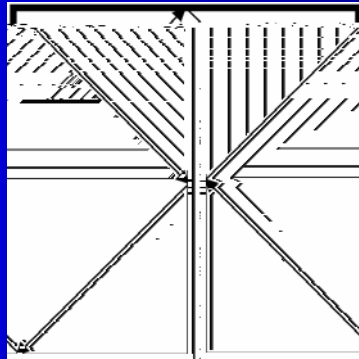
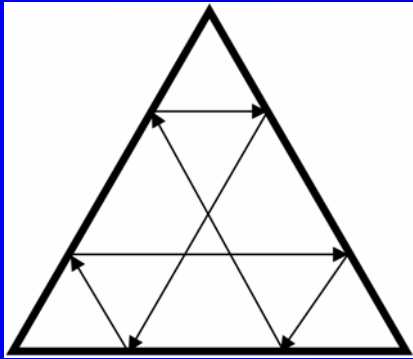


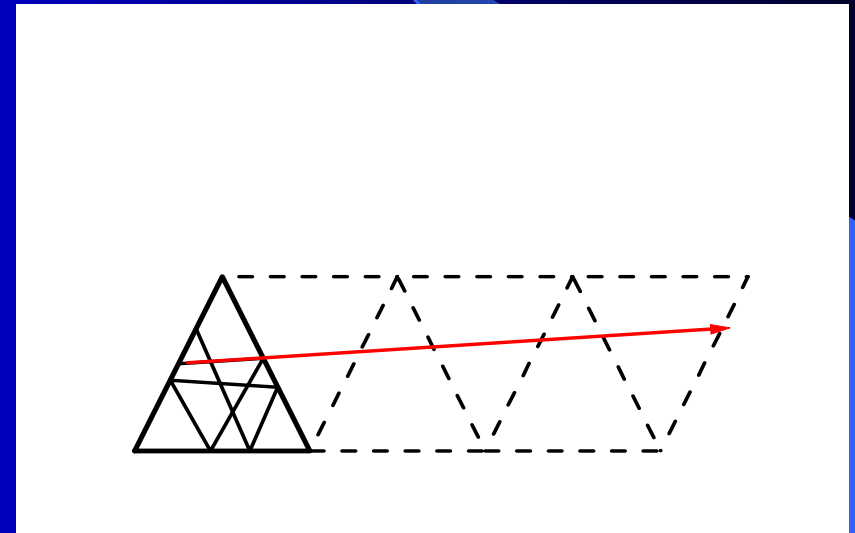
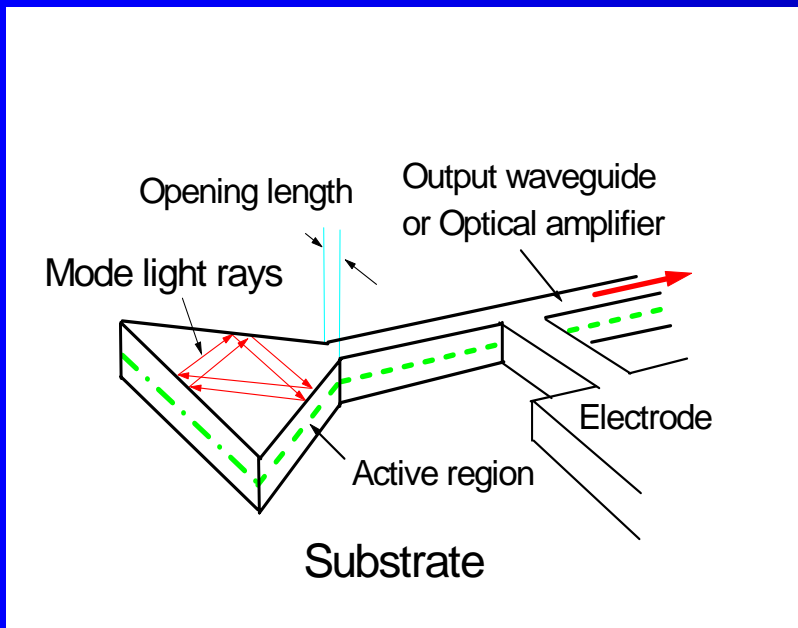
FIG. 3 (color). Field intensity plots of quasiscarred resonances in the spiral-shaped microcavity. (a) $n = 2$ and $nkR = (109.70, -0.1128)$. (b) $n = 3$ and $nkR = (109.59, -0.1127)$. In figures, the field intensity is normalized by scaling the maximum intensity as one.



II. Equilateral Triangle Resonators (ETR) Lasers

Special type of whispering-gallery cavity

Unfolding mode light ray, ETR is equivalent to a deformed Fabry-Perot cavity



Y.Z. Huang et al, IEEE J. Sel. Topics Quantum. Electron., vol. 12,
pp.59-65(2006)

Transverse and longitudinal eigenvalue equation

$$m \frac{\sqrt{3} a}{4} = \frac{(m+1)}{2}$$

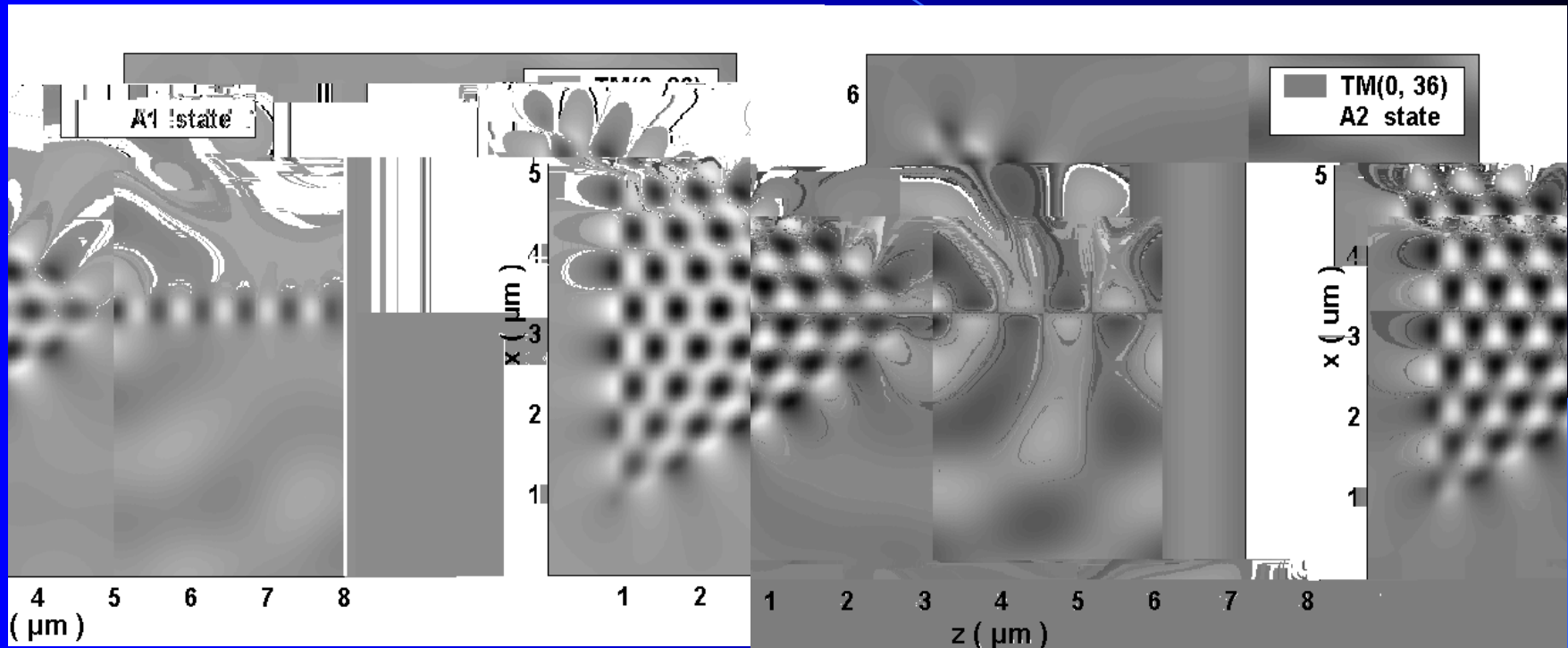
$$l \frac{3 a}{2} = 3 + 2 l$$

$$2 \tan^{-1} \left(\frac{\sqrt{3}}{2} \frac{l}{1} \right) = \frac{1}{2} (m+1)^2$$

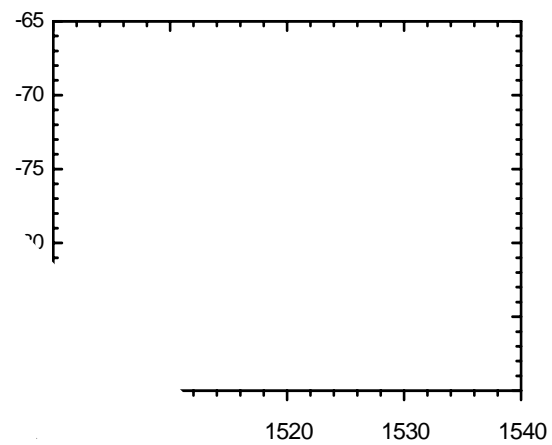
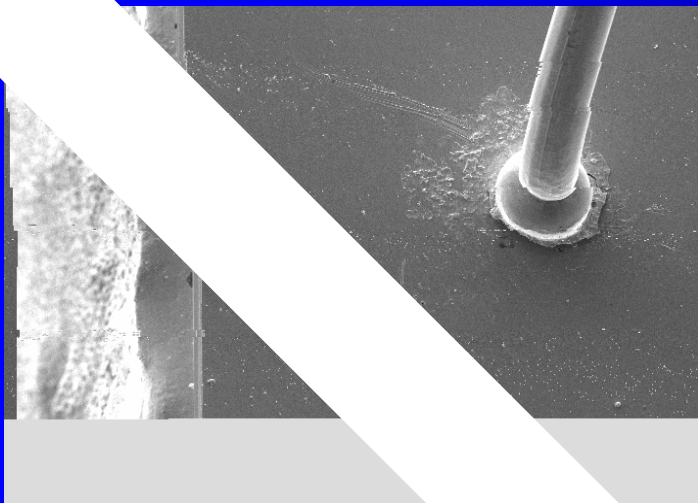
l and m are longitudinal and transverse mode numbers, and mode wavelength is:

$$\lambda_{m,l} = \frac{3Na}{\sqrt{(2l+3)^2 + 3(m+1)^2}}$$

Mode field intensity for an ETR lasers with output waveguide obtained by FDTD simulation



The side-length and inner refractive index of ETR is $5\mu\text{m}$ and 3.2 respectively. The width of output waveguide is $0.3\mu\text{m}$. The field intensity in the region of $z > 5\mu\text{m}$ is magnified 5 times.

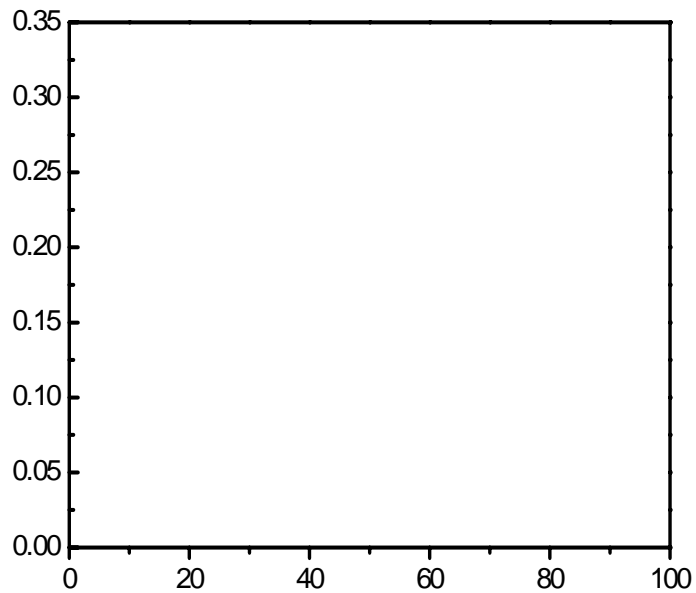


10 m

, 295K

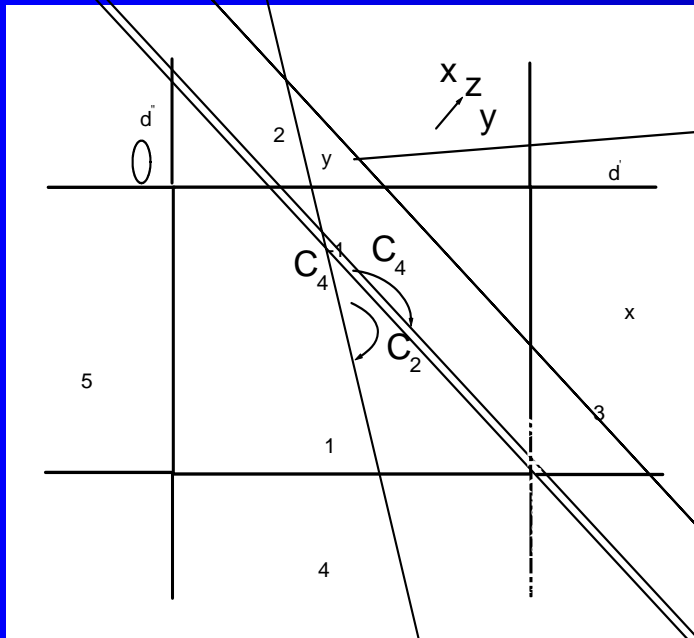
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III. Mode Confined in Rectangular Microresonator

1. Modes confined in square resonator with mode indices (p,q) denoting the numbers of wave nodes in the x and y directions



Mode field distribution and eigenvalue equations:

$$F_{zx}^p = \begin{cases} \cos\left(\frac{x}{a/2}\right) & |x| \leq a/2 \\ \cos\left(\frac{a/2}{a/2}\right) \exp\left[-\frac{x}{a/2}\right] & x > a/2 \\ \cos\left(\frac{a/2}{a/2}\right) \exp\left[\frac{x}{a/2}\right] & x < -a/2 \end{cases}$$

$$F_{zy}^q = \begin{cases} \cos\left(\frac{y}{b/2}\right) & |y| \leq b/2 \\ \cos\left(\frac{b/2}{b/2}\right) \exp\left[-\frac{y}{b/2}\right] & y > b/2 \\ \cos\left(\frac{b/2}{b/2}\right) \exp\left[\frac{y}{b/2}\right] & y < -b/2 \end{cases}$$

$$\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + n_1^2 k_0^2$$

$$= (n_1^2 - 1) k_0^2$$

$$\begin{cases} \tan\left(\frac{a/2}{a/2}\right) & x \\ \tan\left(\frac{b/2}{b/2}\right) & y \end{cases}$$

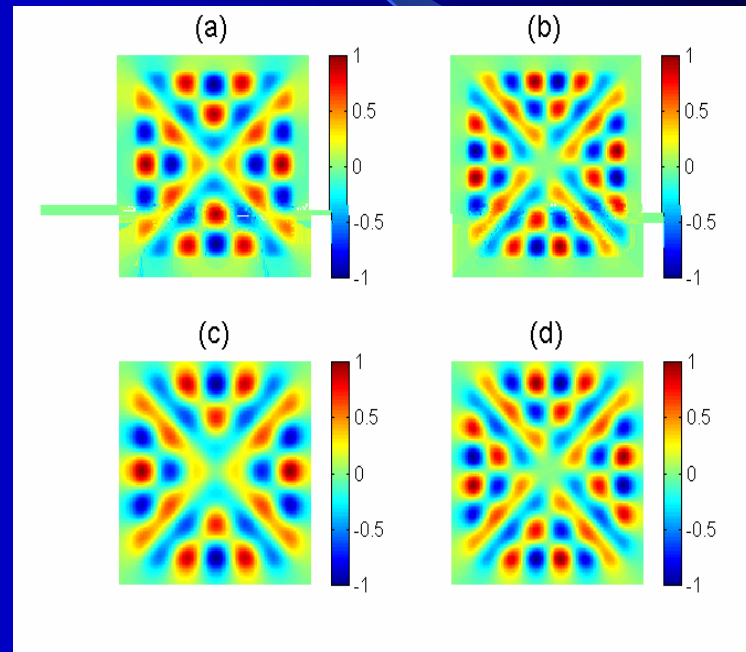
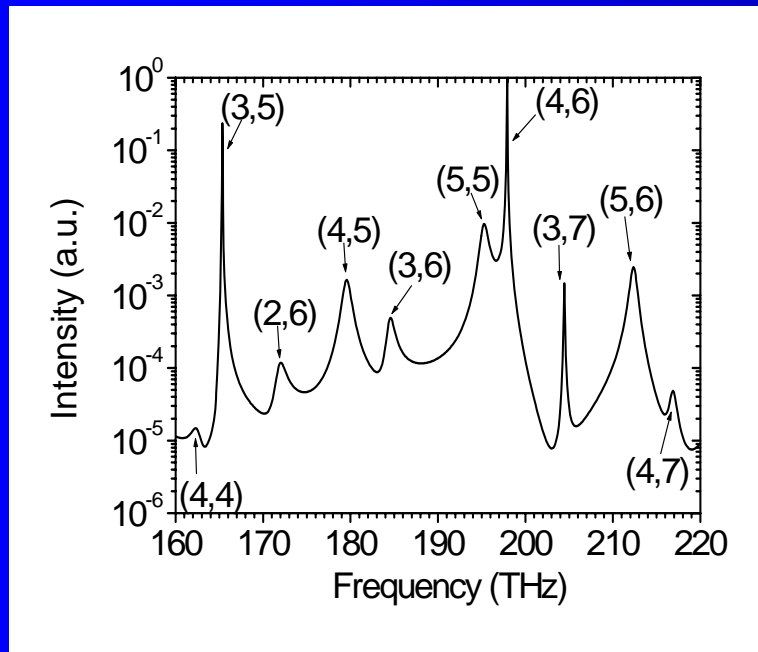
$= n_1^2/n_2^2$ for TE mode
 $= 1$ for TM mode, $v = x, y$

The total internal reflection limits the difference between k_x and k_y , $v = 0$ or $\pm 1/2$ as the corresponding p or q is even or odd number, respectively.

Mode intensity spectrum obtained by FDTD simulation and Pade approximation for a square resonator with sidelength of 2 μ m and $n=3.2$

TE_{0,14}

TE_{0,16}

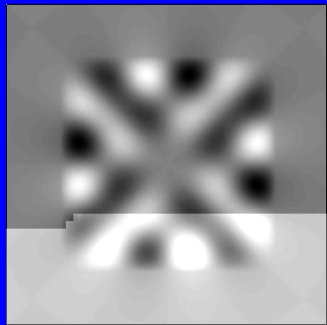


FDTD

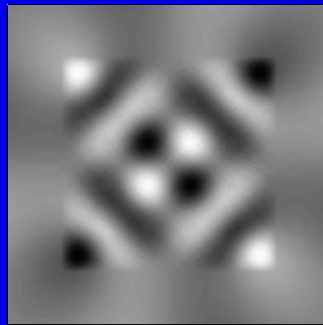
Analytical

Mode with same symmetry in x and y directions have high Q-factor.

Mode field pattern in a square resonator with $a = 2$ m and $n=3.2$.



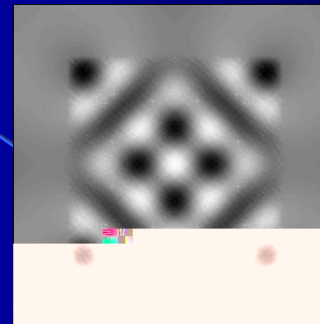
$TE^o(3,5)$



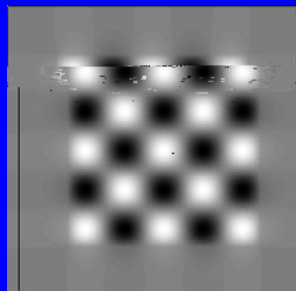
$TE^e(3,5)$



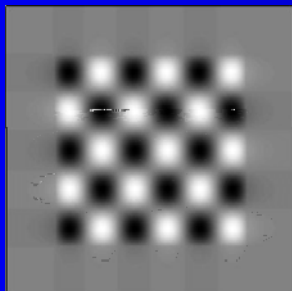
$TE^o(4,6)$



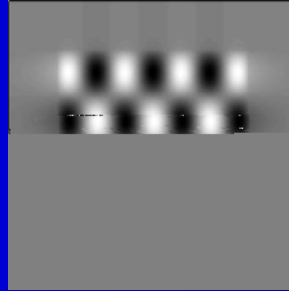
$TE^e(4,6)$



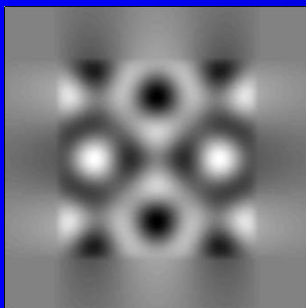
$TE(4,4)$



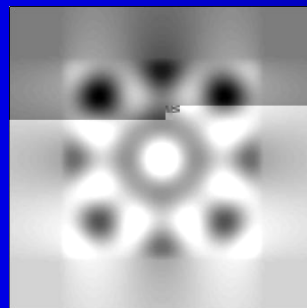
$TE(4,5)$



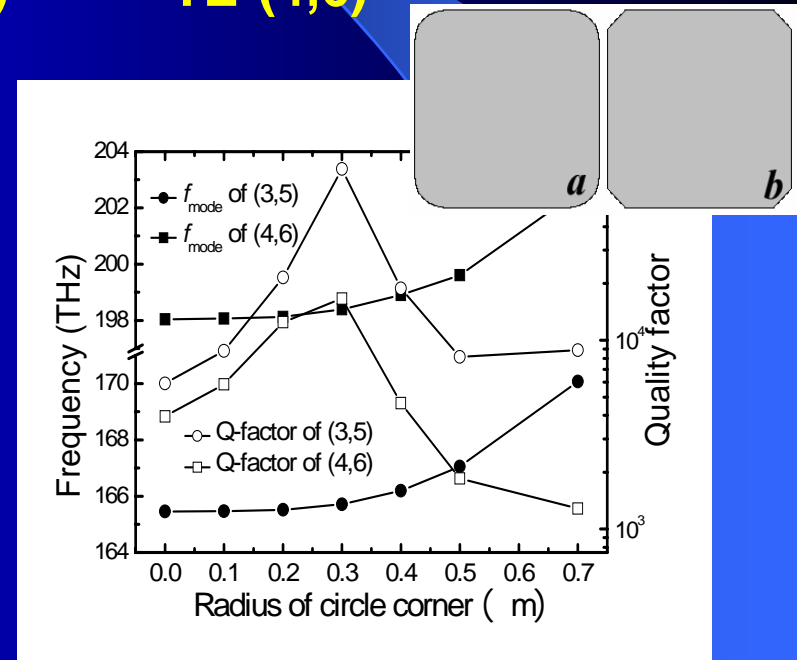
$TE(3,6)$



$TE^o(2,6)$

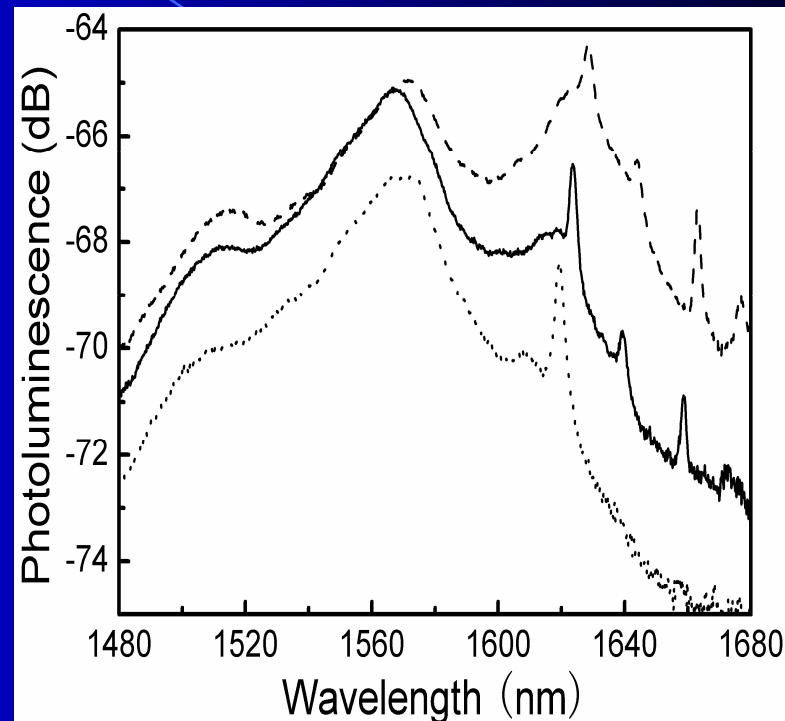
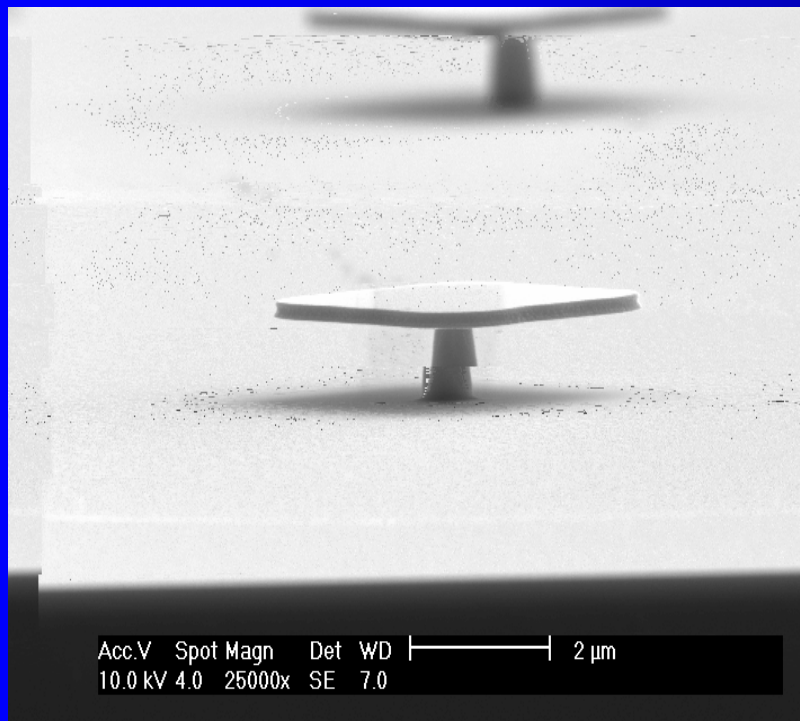


$TE^e(2,6)$



Mode Q-factors even increase in a square with circular corners.

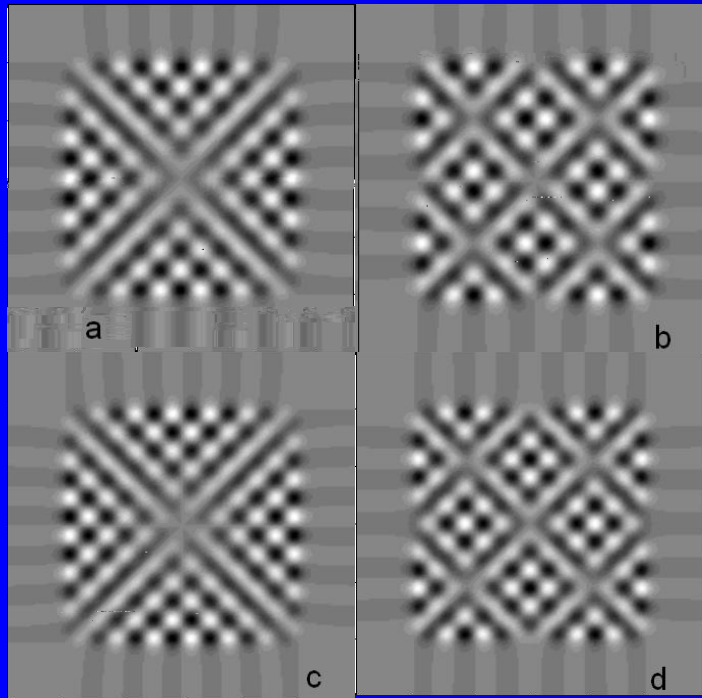
Square resonator fabricated by selected chemical etching technique.



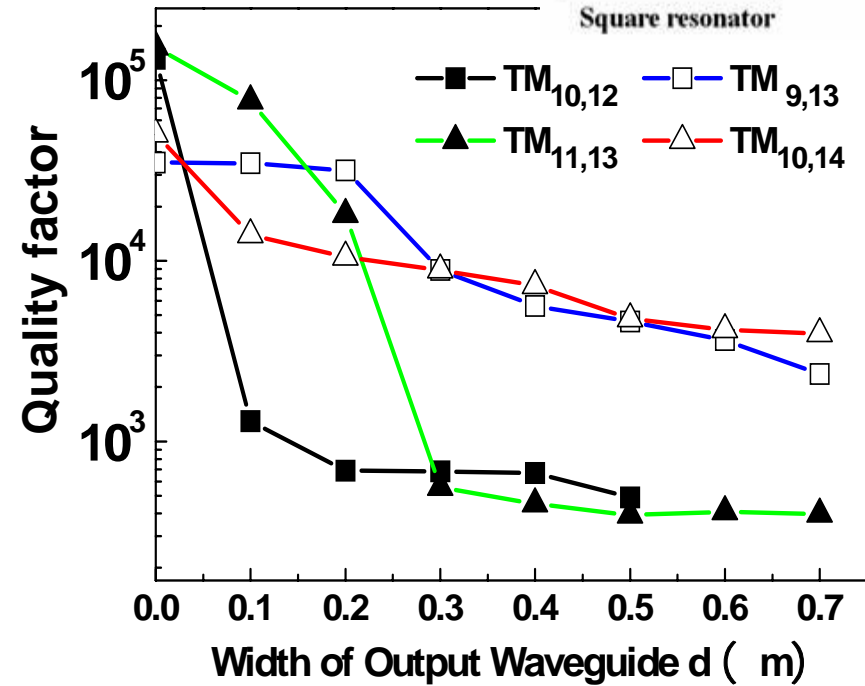
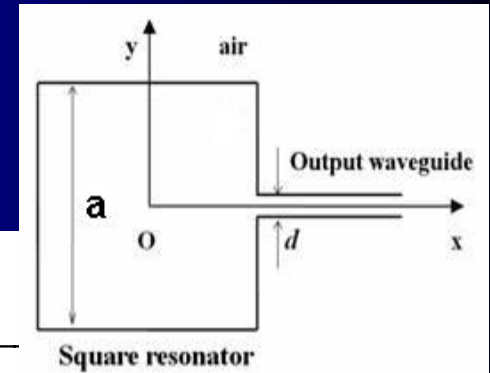
SEM picture and photoluminescence of a square with side length of 7 μm .

Y. Z. Huang et al, IEEE Photon. Technol. Lett., vol. 17, p.2589(2005)

Directional emission for square microlasers

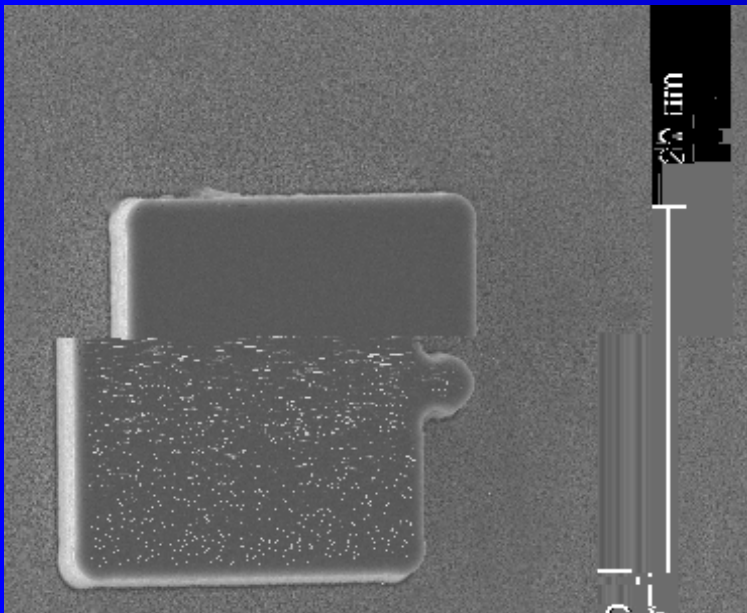


Field distribution of (a) $TM_{10,12}$,
(b) $TM_{9,13}$, (c) $TM_{11,13}$, (d) $TM_{9,13}$
in a square with sidelength of 4 μm
and refractive index 3.2.

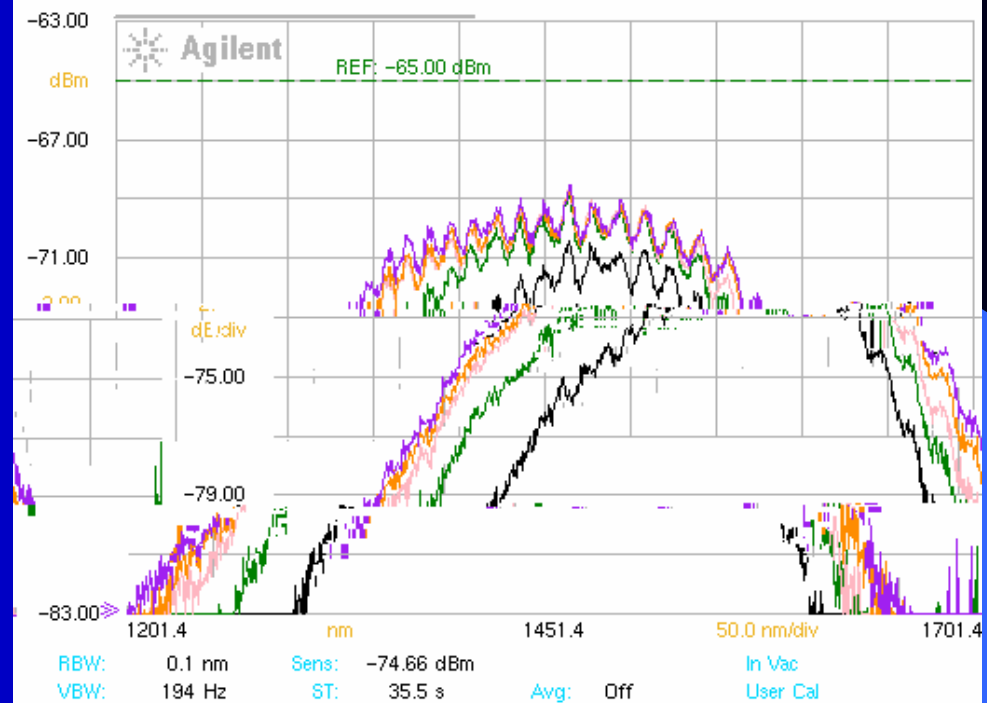


Mode Q-factor versus width of output waveguide

Directional Emission square InGaAsP laser with 20 μm side.



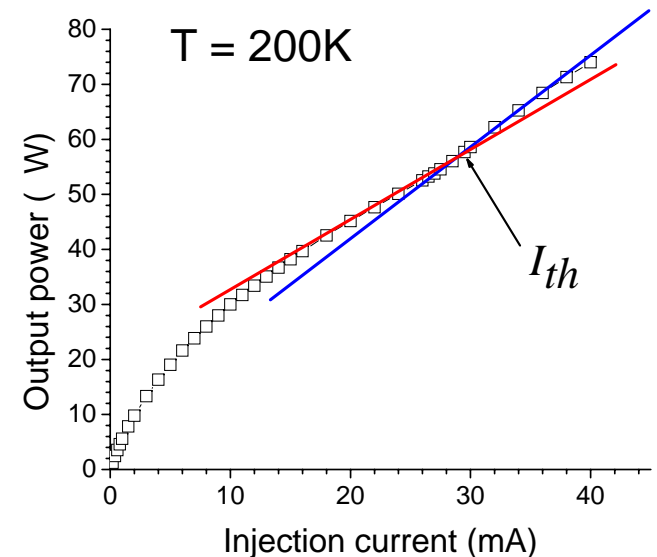
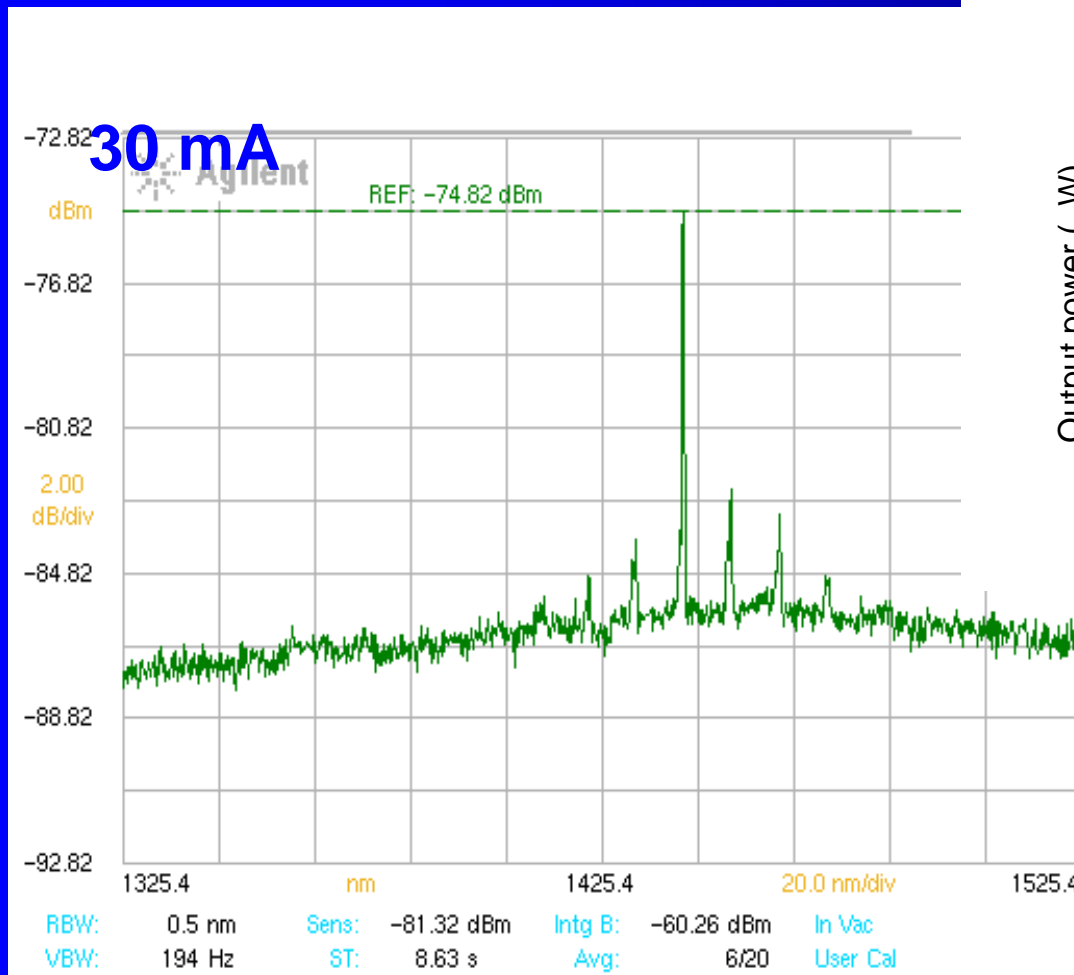
Output spectra at room temperature



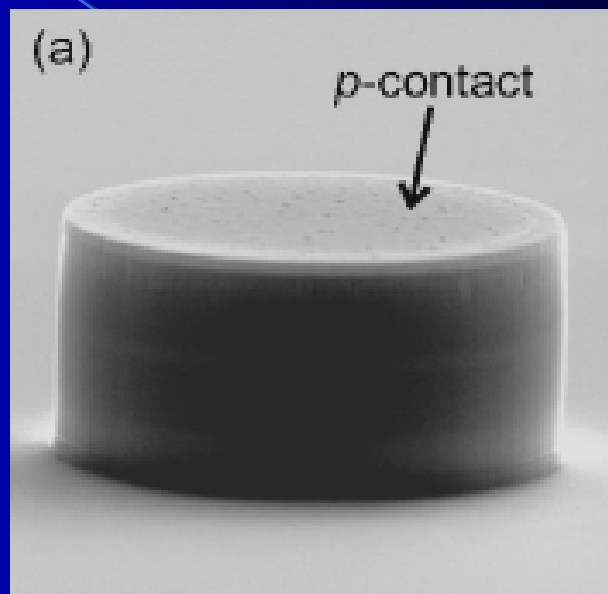
First run. CW electrically operation is realized at 200K.

Derivative resistor is one order larger than the ETR laser. (70~80 Ω)

Laser spectrum and output power-injection current curve of a InGaAsP/InP square laser with side length 20 μm at 200K.



四. 纵向弱波导三维微腔中的高Q值TM模

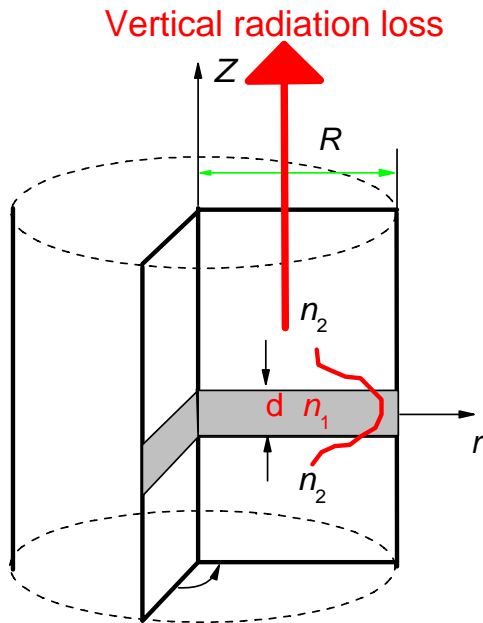


Q

?

Whispering-Gallery Modes (WGMs) in 3D microcylinder

TE and TM modes in 3D microcylinder How to get High-Q modes in microcylinders ?



3D finite difference time-domain (FDTD) simulation under circular symmetry 2D case

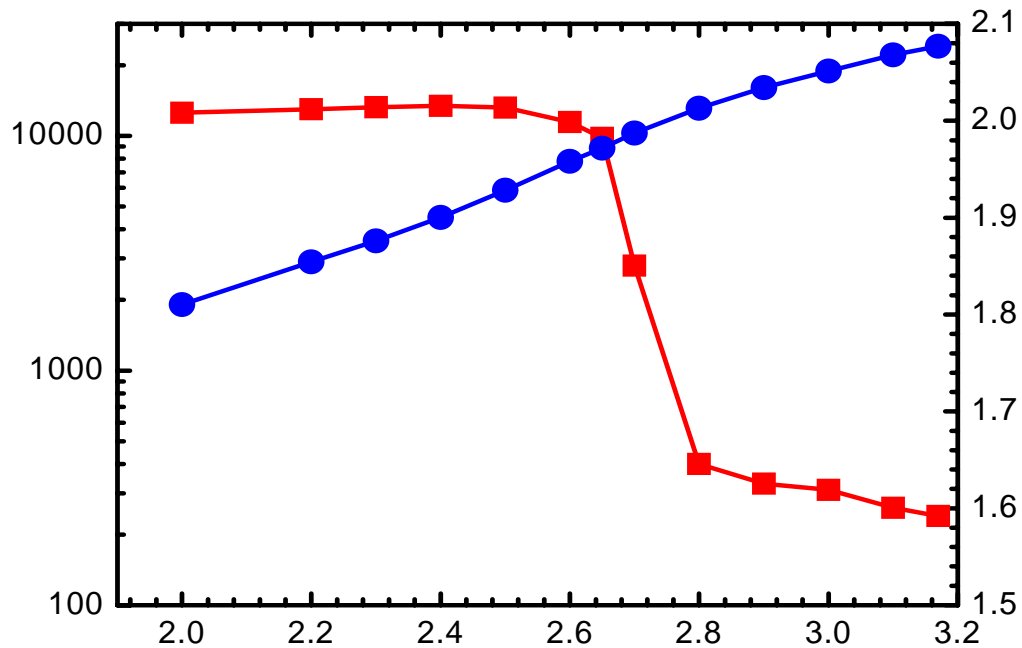
parameters $R = 1 \text{ } \mu\text{m}$, $d = 0.2 \text{ } \mu\text{m}$, $n_1 = 3.4$.

TE (TM) modes: magnetic (electric) field H_z (E_z) is symmetry to r - plane.

Mode Q-factor versus the refractive index of cladding layer n_2

Mode wavelengths and Q -factors for $TE_{7,1}$ and $TM_{7,1}$ WGMs versus n_2 . TM mode can have high Q -factor even vertical refractive indices are 3.4/3.2

1 m
TE TM Q
 n_2 TM Q
 $n_2/n_1=3.4, d=0.2$ m / n_2



Mode wavelengths of the WGMs under effective index approximation and cut-off wavelength of the same order radiation modes in the cladding layers obtained by the following eigenvalue equation:

$$J_\nu(knR)H_\nu^{(2)'}(kR) = J_\nu'(knR)H_\nu^{(2)}(kR)$$

(M. Hentschel et al, Phys. Rev. E66, 056207 (2002))

$n = n_{eff}$ for TE and TM WGMs

$n = n_2$ for HE_{off} and EH_{off}

radiation modes

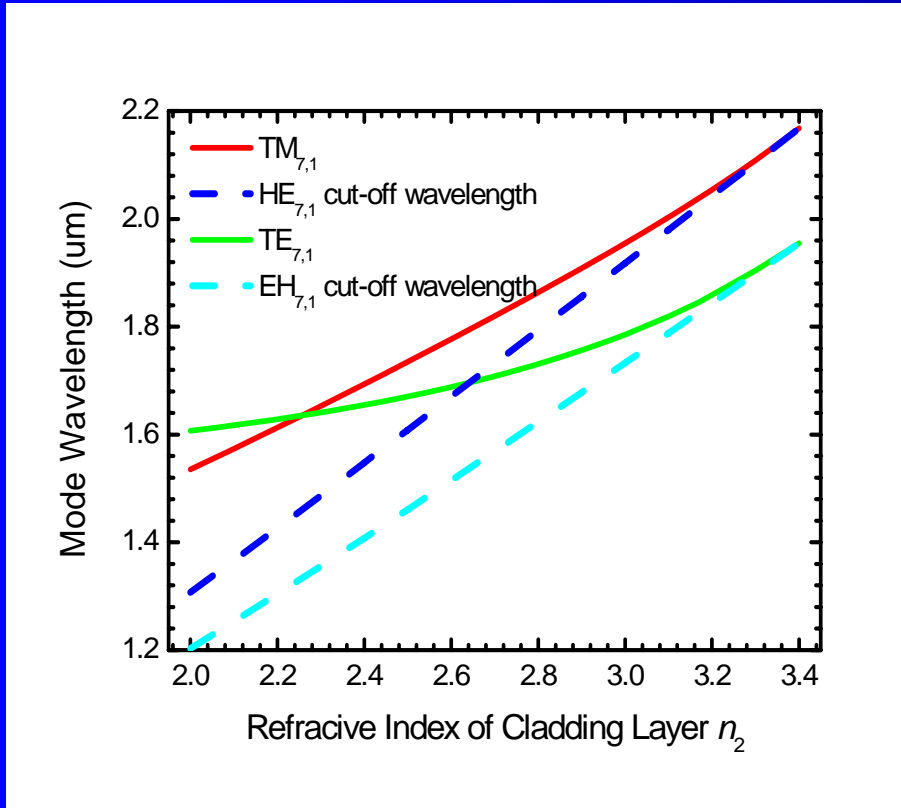
$= n$ for TM and HE_{off} modes

$= 1/n$ for TE and EH_{off} modes

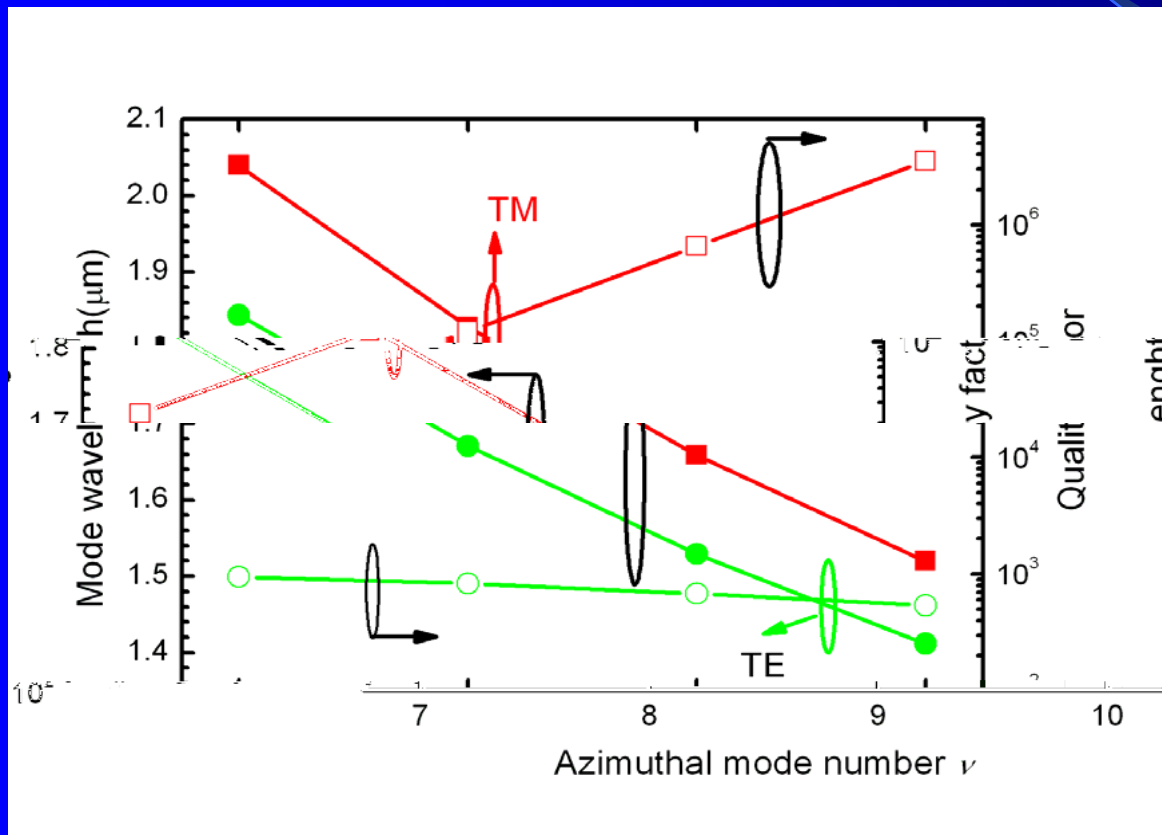
($R = 1$)

$m, d = 0.2 \quad m, n_2/3.4/n_2$

When $n_2 > 2.65$, $WGM(TE_{7,1}) < \text{radiation}(HE_{7,1})_{off}$ vertical radiation loss



Mode wavelengths and Q-factors of TE and TM WGMs versus azimuthal mode number obtained by FDTD simulation for the microcylinder with vertical refractive indices 3.4/3.17.



TE WGMs:
 $Q \sim 10^2$

TM WGMs:
 $Q \sim 10^4 - 10^6$

FDTD

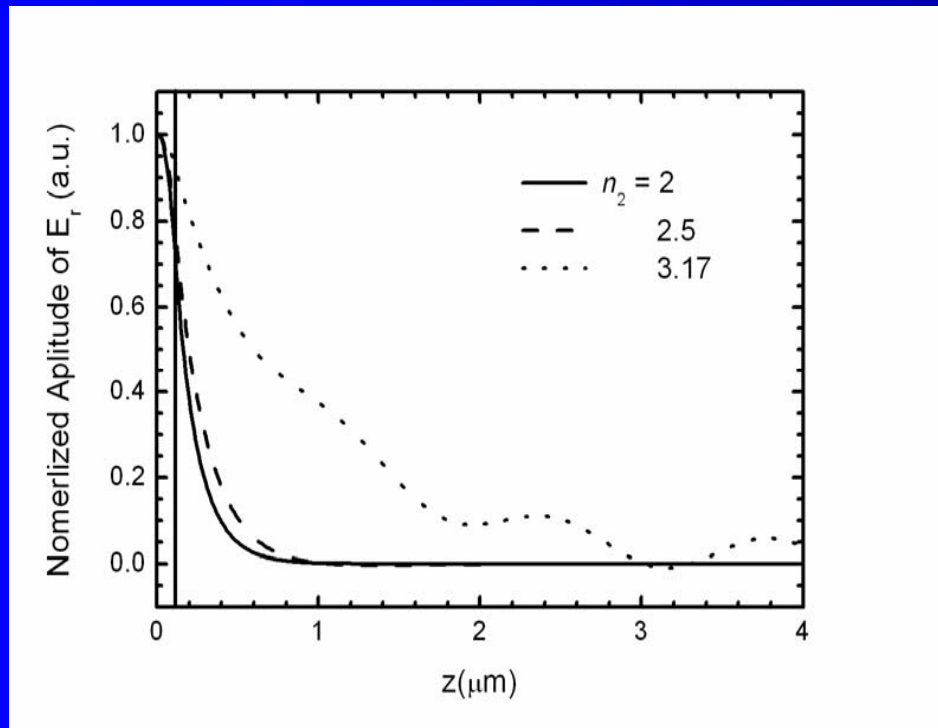
TE

TM

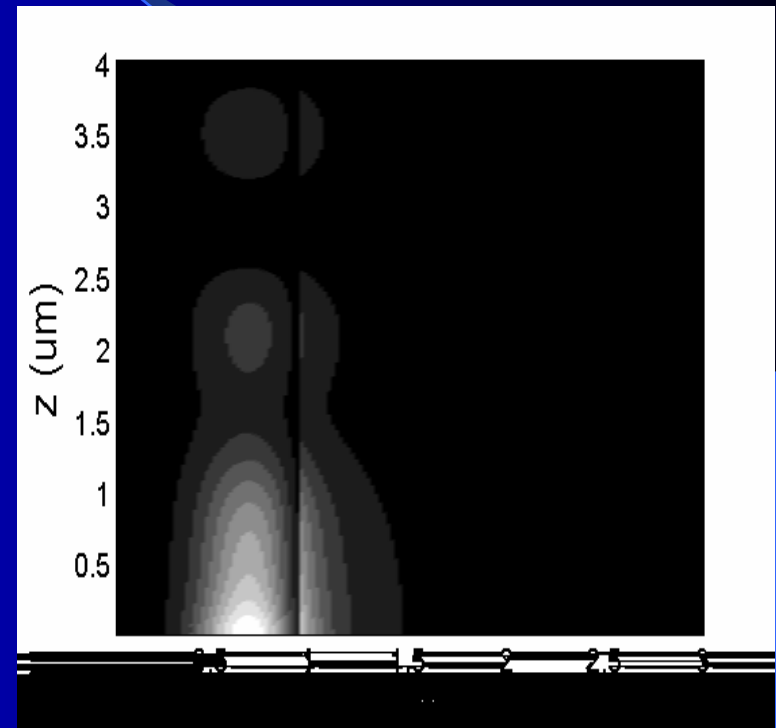
Q

ν

Vertical field distribution of TE_{7,1} WGM at $n_1 = 3.4$ and $n_2 = 2, 2.5$, and 3.17 obtained by FDTD simulation.

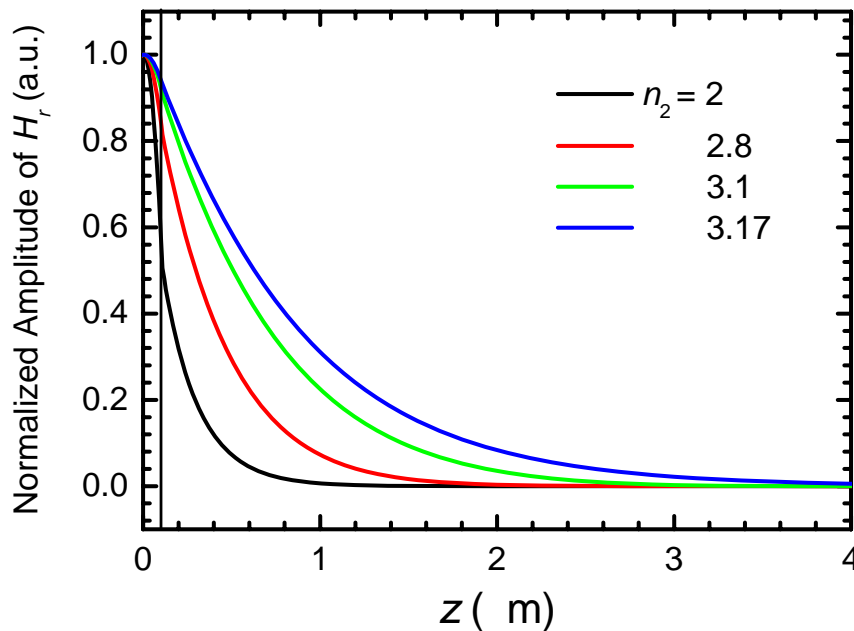


$$r = 0.84R$$

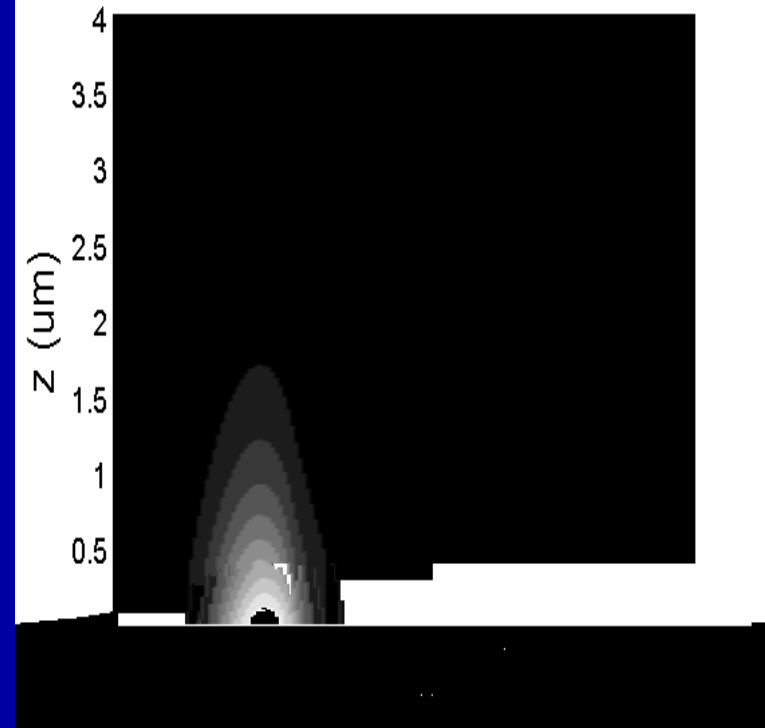


$$n_2 = 3.17$$

Vertical field distribution of $\text{TM}_{7,1}$ WGM at $n_1 = 3.4$ and $n_2 = 2, 2.8, 3.1$, and 3.17 obtained by FDTD simulation.



$$r = 0.84R$$



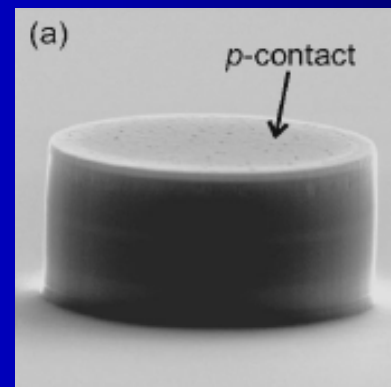
$$n_2 = 3.17$$

Mode wavelengths of **WGMs** and **radiation modes** for microcylinder with vertical refractive indices 3.4/3.17

R (μm)	1.0	2.0	3.0	4.0	5.0	6.0
<i>Mode index</i>	9	21	33	45	58	70
-TM WGM (μm)	1.658	1.589	1.584	1.586	1.565	1.574
-TE WGM (μm)	1.532	1.533	1.548	1.560	1.546	1.558
(HE_{off}) (μm)	1.641	1.572	1.566	1.569	1.548	1.556
(EH_{off}) (μm)	1.511	1.511	1.526	1.539	1.527	1.537
Q (TE)	680	470	580	870	$\sim 10^4$	$\sim 10^6$



T. Baba et al, IEEE
Photon. Technol. Lett., 9,



WG

, TM

WGM

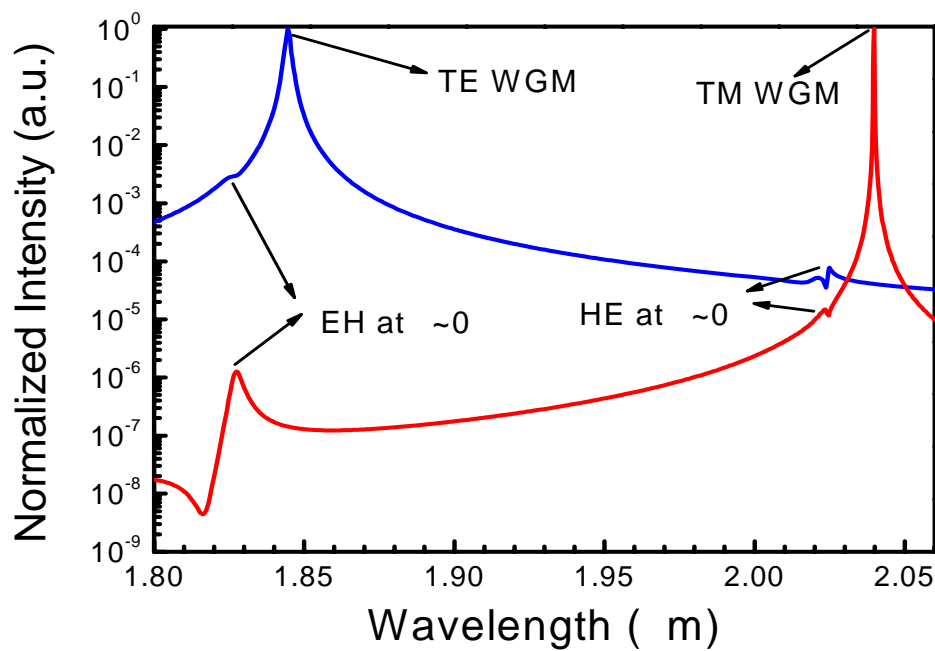
TE

WGM

TE

TM

WG



FDTD

TE

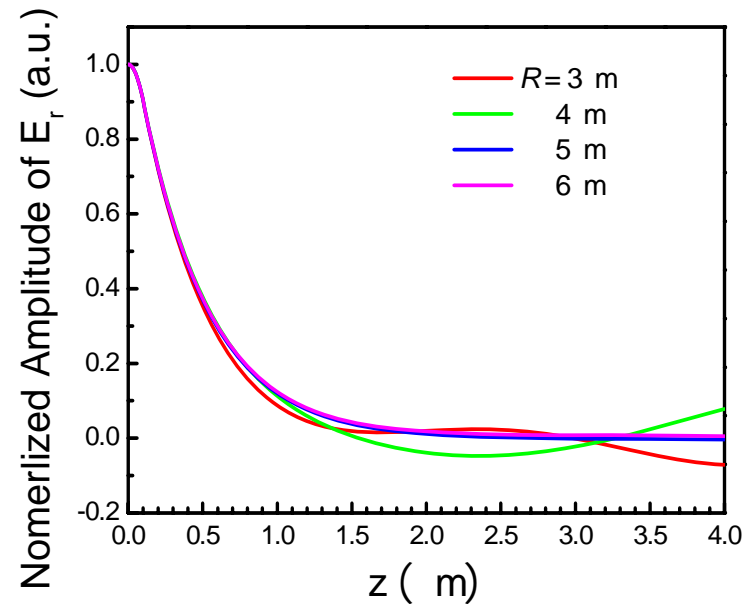
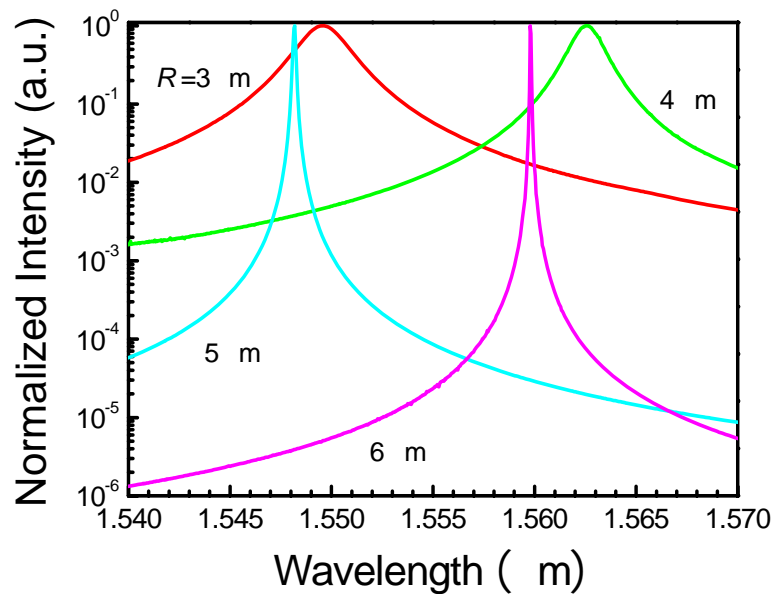
TM

WGM

EH

HE

TE WGM



TE

5~6 m,

TM

Phys. Rev. A Vol.75 013817 (2007)

IEEE Photonics Technology Letters 19, 1831(2007)

五. 结论

(10-30)
TM 1



Thank You !