

Laser Shaping of a Relativistic Intense, Short Gaussian Pulse by a Plasma Lens

H. Y. Wang,¹ C. Lin,^{1,*} Z. M. Sheng,² B. Liu,¹ S. Zhao,¹ Z. Y. Guo,¹ Y. R. Lu,¹ X. T. He,¹ J. E. Chen,¹ and X. Q. Yan^{1,†}

¹State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing 100871, China, and Key Lab of High Energy Density Physics Simulation, CAPT, Peking University, Beijing 100871, China

²Key Laboratory for Laser Plasmas (MoE) and Department of Physics, Shanghai Jiao Tong University, Shanghai 200240, China and Beijing National Laboratory of Condensed Matter Physics, Institute of Physics, CAS, Beijing 100190, China

(Received 17 September 2011; published 22 December 2011)

By 3D particle-in-cell simulation and analysis, we propose a plasma lens to make high intensity, high contrast laser pulses with a steep front. When an intense, short Gaussian laser pulse of circular polarization propagates in near-critical plasma, it drives strong currents of relativistic electrons which magnetize the plasma. Three pulse shaping effects are synchronously observed when the laser passes through the plasma lens. The laser intensity is increased by more than 1 order of magnitude while the initial Gaussian profile undergoes self-modulation longitudinally and develops a steep front. Meanwhile, a nonrelativistic prepulse can be absorbed by the overcritical plasma lens, which can improve the laser contrast without affecting laser shaping of the main pulse. If the plasma skin length is properly chosen and kept fixed, the plasma lens can be used for varied laser intensity above 10^{19} W/cm².

DOI: 10.1103/PhysRevLett.107.265002

PACS numbers: 52.38.Kd, 41.75.Jv, 52.35.Mw, 52.59.-f

The recent development of ultrashort-pulse high peak power laser systems enables us to investigate high field science under extreme conditions [1], which opened new and active research fields such as fast ignition of inertial confinement fusion [2], laboratory astrophysics [3], and development of a compact source of high-energy electrons and ions [4].

Generation of high-energy ions by ultraintense laser pulses has been intensively studied due to its wide range of applications [5,6]. Radiation pressure acceleration has been proposed as a promising route to obtain high-quality ion beams in a much more efficient way [7–13], compared to the target normal sheath acceleration [14–16]. In order to accelerate ions to a relativistic velocity in the radiation pressure acceleration regime, hole-boring effects [10],

[22]. The RSF of a linearly polarized laser beam in a near-critical plasma has been investigated by Pukhov and Meyer-ter-Vehn, which shows that the magnetic interaction plays an important role during RSF in the 3D simulations [23]. For near-critical plasma, the Raman instability that otherwise destroys the pulse is prohibited. RSPM can be very effective in this density region and results in a smooth pulse self-compression [24]. For relativistically strong ($|a| \geq 1$) laser pulses, however, the weak nonlinearity approximation is not valid anymore, because the nonlinear interactions can be rather complex and must be understood in conjunction with generation of a strongly nonlinear wakefield, erosion of the leading edge, and generation of the quasistatic magnetic field, etc. [1]. By means of 3D simulations we found that RSF, RSPM, and relativistic transparency effects are dynamically related together in laser interaction with the near-critical plasma. The laser pulse is focused to a smallest spot size and the focused intensity can be increased by a factor of 25. At the same time the initial Gaussian pulse becomes steepened, meanwhile a nonrelativistic prepulse can be absorbed by the overcritical plasma and the laser contrast is improved. For the proper chosen plasma lens parameters, the three lens effects above are effective for varied laser intensity above 10^{19} W/cm². Therefore the plasma slab can be used as a plasma lens to generate high intensity, high contrast, and steepened laser pulses, which is quite challenging for state of the art laser technology.

(7) Such a laser pulse is also promising for attosecond UV and x-ray sources from plasma surfaces of solid foil [18].

In this Letter we report on a laser-driven plasma lens that can transversely focus the laser beam to the sublaser wavelength in the radius and enhance the laser intensity by more than 1 order of magnitude, while temporally steepening the Gaussian pulse and improving the laser contrast. One fundamental nonlinear effect of laser-plasma interaction arises from the relativistic motion of the electrons in the intense laser field [19]. In particular, the transverse and axial profiles of the laser pulse can be changed by relativistic self-focusing (RSF) [20] and relativistic self-phase modulation (RSPM) [21]. Laser shaping by nonlinear interactions of an intense pulse in underdense plasma is discussed by weakly nonlinear theory and simulations

In the relativistic regime magnetic interaction appears to be due to the fact that electrons accelerated inside a self-focused laser pulse produce electric currents in the plasma and an associated quasistatic magnetic field. The electron velocity is limited by the velocity of light in vacuum, so the electron current density is approximately equal to $en_e c$,

where e , n_e , and c is the charge of electron, electron density, and speed of light in vacuum, respectively. Omitting the numerical factors, the quasistatic magnetic field at the distance r from the axis reads:

$$B_s = (en_e)2\pi r. \quad (1)$$

For a uniform plasma, the self-generated magnetic field vanishes at the channel axis and reaches a maximum at the channel edges. The quasistatic magnetic field pinches the relativistic electrons into a channel with a radius r

$y_0 = 10\lambda$ and $x_0 = 10\lambda$, where $T = 3.3$ fs is the laser period. The uniform carbon plasma of density $n_0 = 2.4n_c$ is placed between $3\lambda \leq z \leq 60\lambda$, where n_c is the critical plasma density. Each cell is filled with 8 quasiparticles. The initial temperature of the electrons and carbon ions is 5 eV.

The transverse pulse self-focusing process at $t = 72$ T is shown in Fig. 1. The incident beam first propagates through an unstable filamentary stage and then collapses into a single channel as shown in Fig. 1(a). The laser pulse is focused to a smallest spot size at $z = 24.1 \mu\text{m}$, corresponding to a laser self-focusing length of about $21.1 \mu\text{m}$. The normalized electric field E_y is 84.59 which is increased by a factor of 5 and the laser intensity is 25 times higher than the initial one. The (X, Y) section of E_y in Fig. 1(b) shows that the pulse self-focusing process is symmetrical. The laser retains its Gaussian radial profile within the channel with a radius of about 0.9λ as seen in Fig. 1(c), which is in good agreement with Equation. (3) (theory predicts 0.83λ). The coalescence of the filaments by magnetic interaction are well explained on the basis of the magnetic interaction by Askaryan *et al.* [26]. In Fig. 1(d), the (Z, Y) section of the quasistatic magnetic field B_x averaged over 2 laser periods is plotted. This field vanishes at the channel axis and reaches a maximum at the edges. The maximum magnetic field is about 6.7 at the edges, which agrees well with the theoretical prediction of 6.29 by Eq. (4).

Figure 2 shows how the pulse profile changes in the longitudinal direction by laser compression during its propagation through different plasma planes. It shows an efficient laser compression at $z = 24.1 \mu\text{m}$, where the laser propagates a plasma slab length that is the same as the self-focusing length. At the same time the laser pulse developed a steep front of about 8 T. This implies that a initial Gaussian profile is nearly transformed into a quasi-step function pulse. For a plasma length longer or shorter

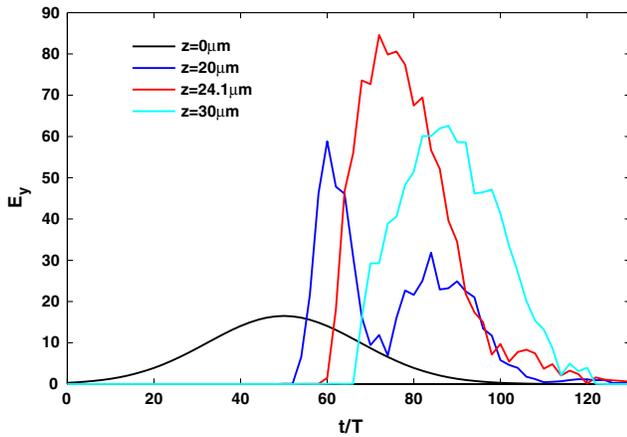


FIG. 2 (color online). Longitudinal pulse compression: On-axis envelope profile E_y at $z = 0 \mu\text{m}$, $z = 20 \mu\text{m}$, $z = 24.1 \mu\text{m}$, and $z = 30 \mu\text{m}$.

than the self-focusing length, the laser compression is less efficient.

We now study the optimistic parameters for the plasma lens. Considering laser shaping of an intense laser pulse, three typical parameters are critical for the process: (i) increase of the normalized vector potential on axis $f_0 = a_{\text{max}}/a_0$; (ii) laser rise time r_T ; (iii) laser transmission efficiency t_E . Figure 3(a) shows the influence of plasma density on these three parameters with $a_0 = 16.5$. The normalized vector potential on axis can be enhanced by a factor of 5 for plasma density varied from $1n_c$ to $5n_c$. We should note that the laser transmission efficiency t_E decreases with plasma density increasing, while the laser rise time r_T decreases rapidly to about 8 T at $n_e = 2.4n_c$ and becomes saturated. The laser transmission efficiency is about 30% at this point while it can be as high as 60% with plasma density of $n_e = 1.5n_c$ if the pulse rise time can be compromised. The quasistatic magnetic field B_s and the channel radius r observed in simulation are consistent with the theoretical value from Eqs. (3) and (4) as shown in Figs. 3(b) and 3(d). For a fixed plasma skin length $l_s/\lambda = \sqrt{an_c/n_e} = 2.6$, the enhancement of laser amplitude, laser rise time, transmission, and the channel radius r are nearly the same for varied laser intensity ranging from 10^{19} W/cm² to 10^{21} W/cm² as shown in Figs. 3(c) and 3(d).

This means that the plasma lens works for different laser intensities when keeping the plasma skin length fixed. As a result, if we choose a proper plasma density (satisfy $l_s/\lambda \sim 2.6$) and a proper plasma slab length (equal the self-focusing length), the laser focusing and compressing can be realized at the same time and same position. This provides an efficient way to generate a high intensity laser pulse with a sharp rising front by laser shaping in both the transverse and longitudinal directions.

The improvement of the laser pulse contrast (the intensity ratio between the main pulse and the prepulse) is

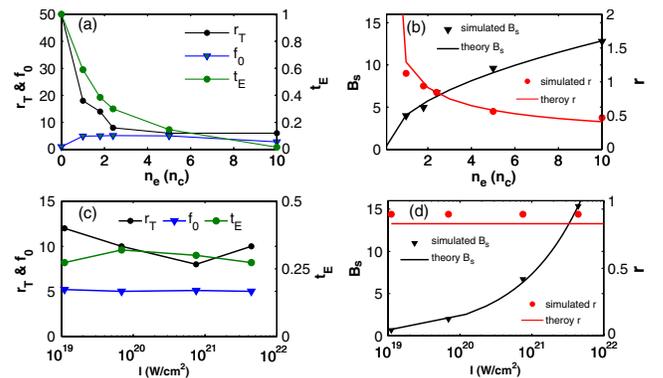


FIG. 3 (color online). Pulse shaping for varied plasma density and laser intensity (a) f_0 , r_T and t_E for varied plasma density at $a_0 = 16.5$; (b) B_s and r for varied plasma density at $a_0 = 16.5$; (c) f_0 , r_T and t_E for varied laser intensity with fixed plasma skin length $l_s/\lambda = \sqrt{an_c/n_e} = 2.6$; (d) B_s and r for varied laser intensity with fixed plasma skin length $l_s/\lambda = \sqrt{an_c/n_e} = 2.6$.

promising for various applications. Relativistic transparency provides a way to achieve laser pulse shaping and generate a high contrast laser pulse [27]. In particle-in-cell (PIC) simulations here, we study the prepulse absorbing process. We set a prepulse of $a = 1$, $\tau = 10 T$ and $r_0 = 6\lambda$, which is 40 T before the main pulse as shown in Fig. 4(a). It is observed that the prepulse can be absorbed in the plasma without affecting the shaping of the main pulse as shown in Fig. 4(b). This shows the plasma lens can also improve the contrast of laser pulse.

In summary we propose a scheme to make a high

- [16] J. Fuchs *et al.*, *Nature Phys.* **2**, 48 (2005).
- [17] F. Pegoraro and S. V. Bulanov, *Phys. Rev. Lett.* **99**, 065002 (2007).
- [18] C. D. Tsakiris *et al.*, *New J. Phys.* **8**, 19 (2006); Y. Nomura *et al.*, *Nature Phys.*, **5**, 124 (2008).
- [19] W. B. Mori, *IEEE J. Quantum Electron.* **33**, 1942 (1997), and references therein.
- [20] A. G. Litvak, *Zh. Eksp. Teor. Fiz.* **57**, 629 (1969) [*Sov. Phys. JETP* **30**, 344 (1970)]; P. Sprangle, C. M. Tang, and E. Esarey, *IEEE Trans. Plasma Sci.* **15**, 145 (1987); G.-Z. Sun *et al.*, *Phys. Fluids* **30**, 526 (1987); X. L. Chen and R. N. Sudan, *Phys. Rev. Lett.* **70**, 2082 (1993); E. Esarey *et al.*, *IEEE J. Quantum Electron.* **33**, 1879 (1997), and references therein.
- [21] C. Max, J. Arons, and A. B. Langdon, *Phys. Rev. Lett.* **33**, 209 (1974); C. J. Mackinstrie and R. Bingham, *Phys. Fluids B* **4**, 2626 (1992).
- [22] C. Ren *et al.*, *Phys. Rev. E* **63**, 026411 (2001); S. S. Bulanov *et al.*, *Phys. Plasmas* **17**, 043105 (2010).
- [23] A. Pukhov and J. Meyer-ter-Vehn, *Phys. Rev. Lett.* **76**, 3975 (1996).
- [24] O. Shorokhov, A. Pukhov, and I. Kostyukov, *Phys. Rev. Lett.* **91**, 265002 (2003).
- [25] Z. M. Sheng *et al.*, *Phys. Rev. Lett.* **94**, 095003 (2005).
- [26] G. A. Askar'yan *et al.*, *JETP Lett.* **60**, 251 (1994).
- [27] A. V. Vshivkov *et al.*, *Nucl. Instrum. Methods Phys. Res., Sect. A* **410**, 493 (1998); A. V. Vshivkov *et al.*, *Phys. Plasmas* **5**, 2727 (1998).