

Materials dependence of the spin-transfer torques on DW

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Outline

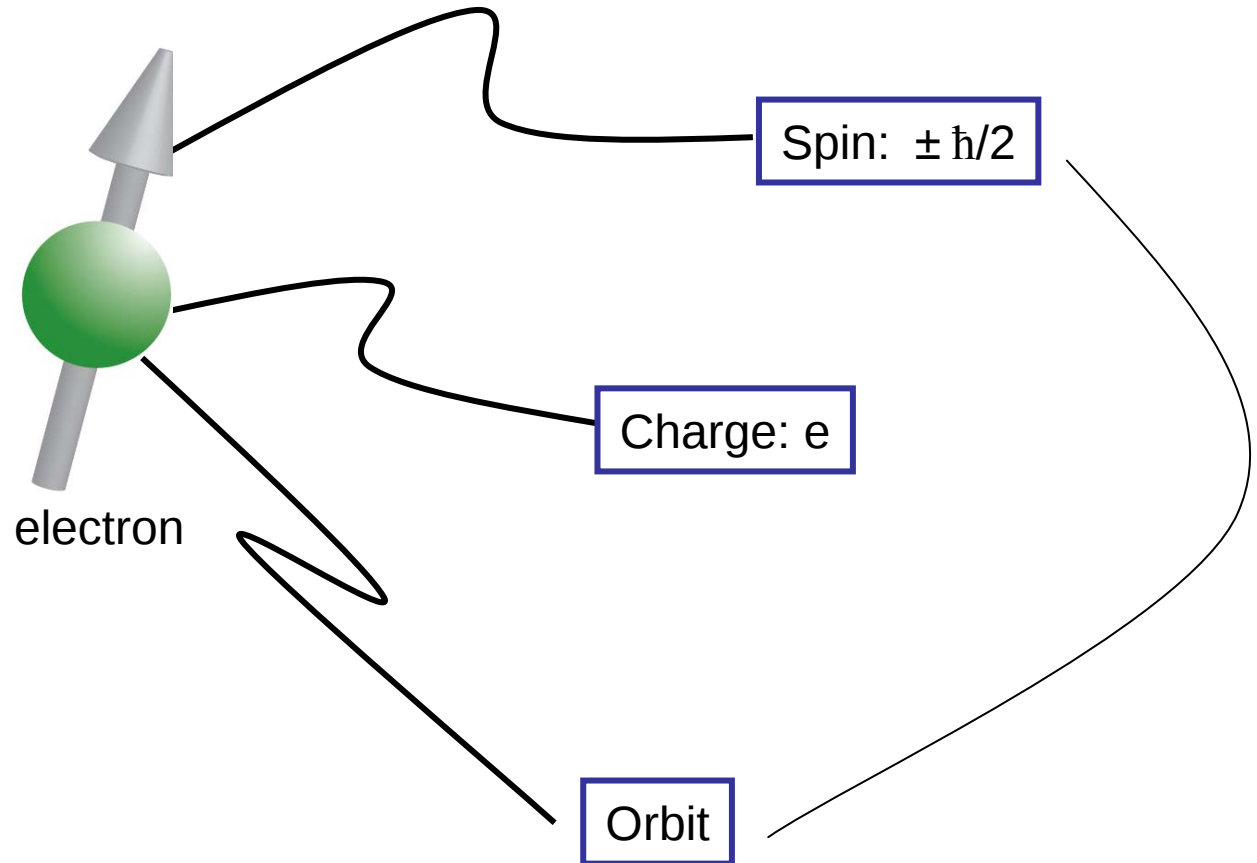
- Introduction
- Two approaches to STT
- STT in spin valves
- Gilbert Damping
- Summary

Dirac equation

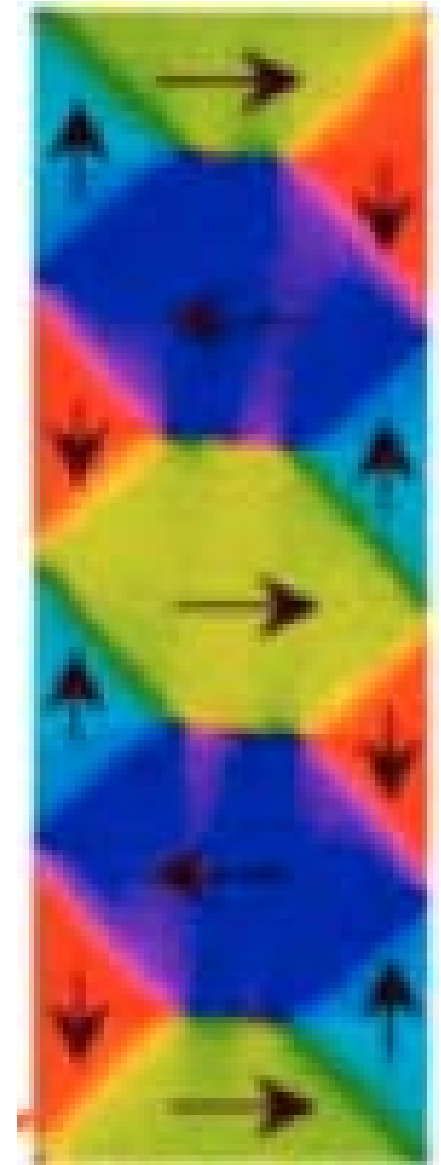
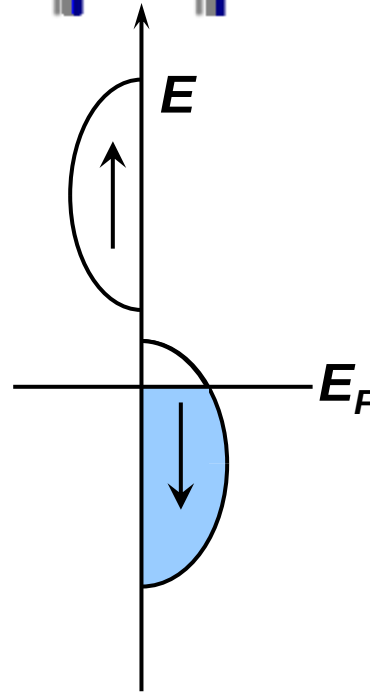
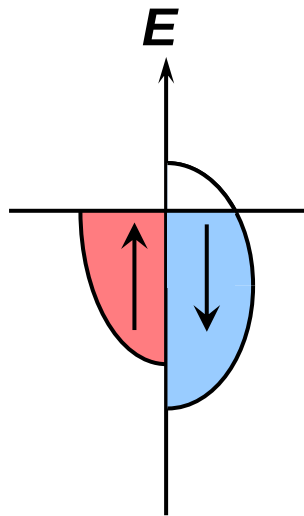
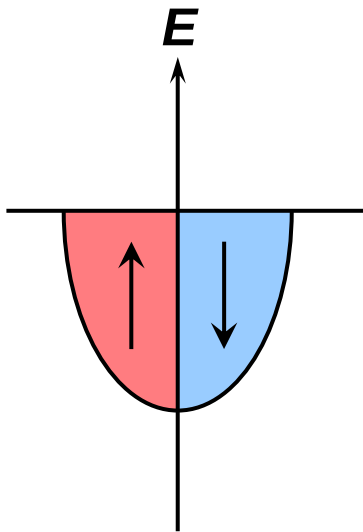
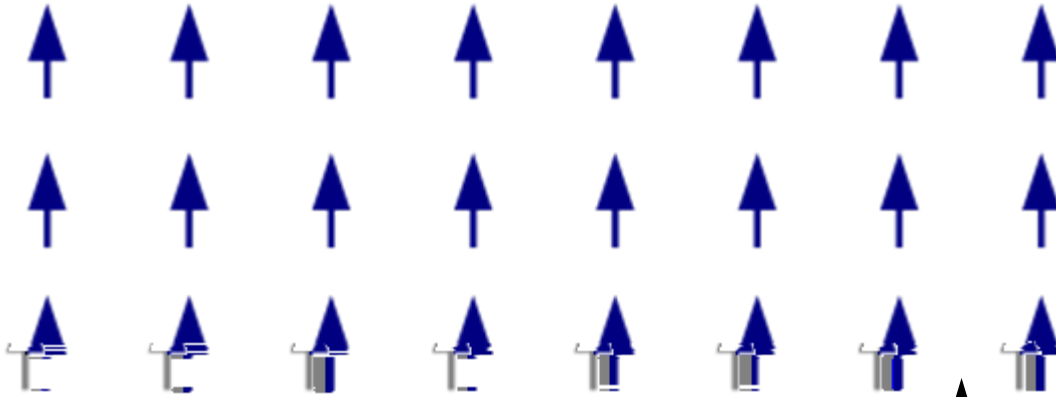
Electron should have “spin.” (1928)



P.A.M. Dirac



Ferromagnetism



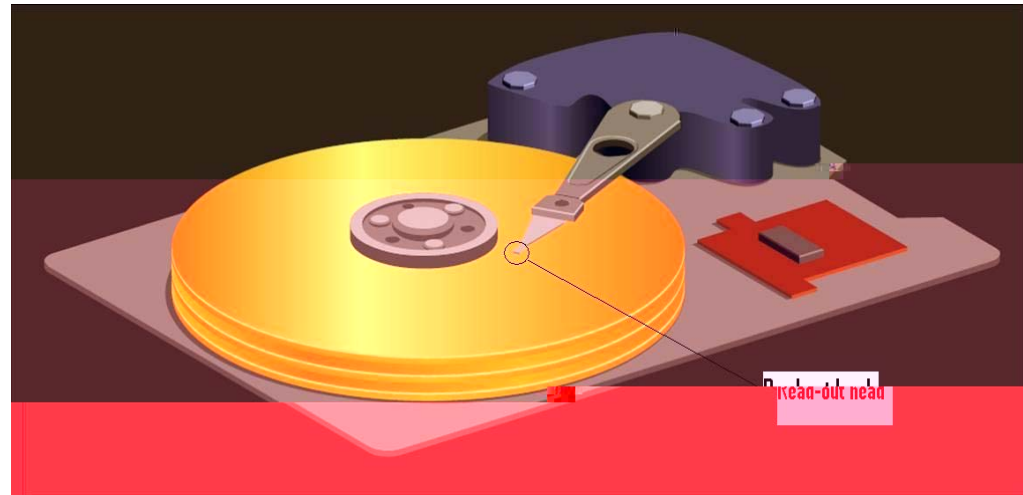
Faraday effect---Maxwell Equation (1865)



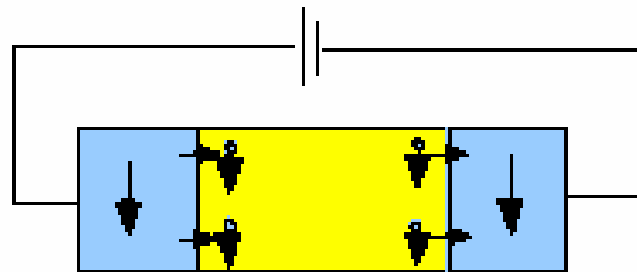
M. Faraday

Faraday's law:

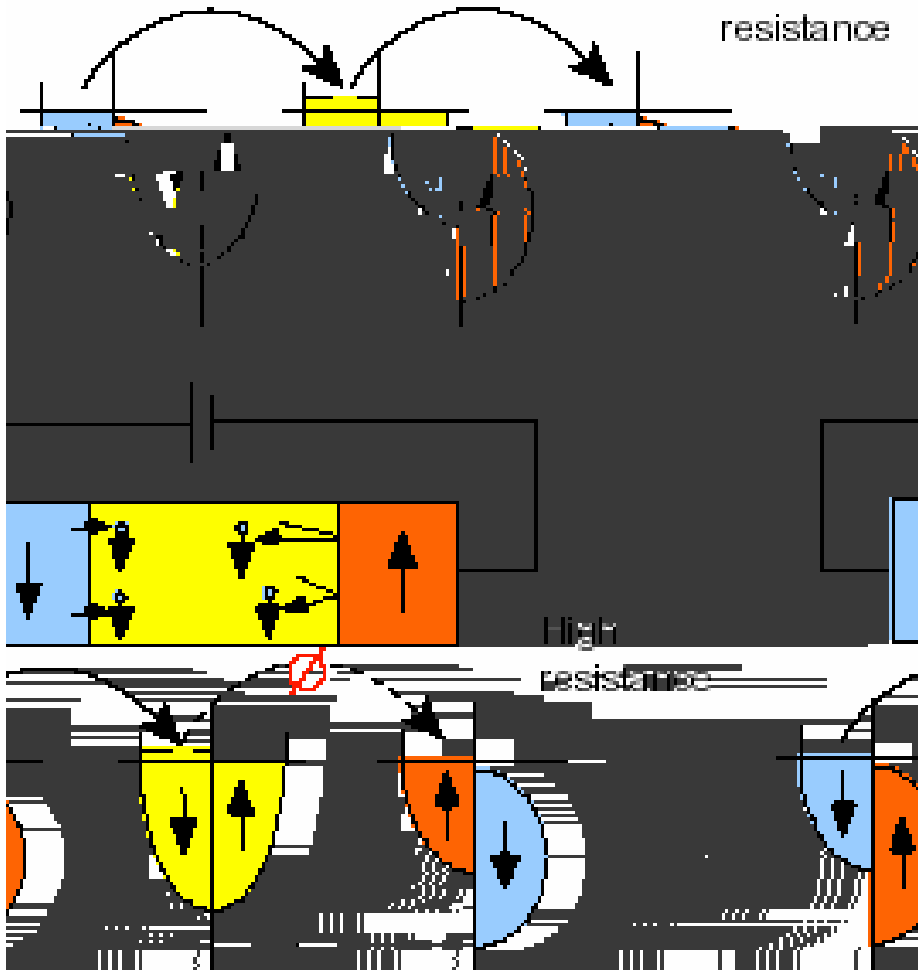
$$\mathcal{E} = -\frac{d\Phi}{dt} \quad (1831)$$



Spin bottleneck magnetoresistance



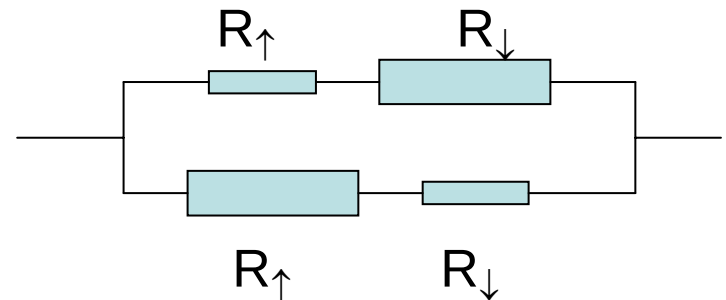
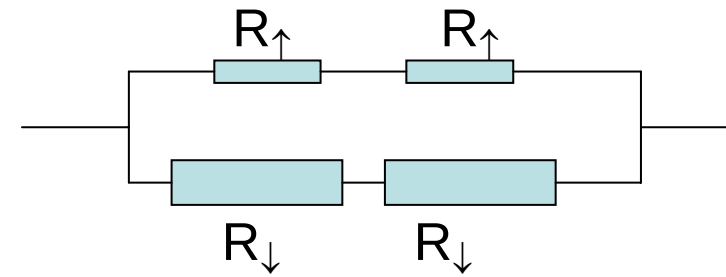
Low
resistance



High
resistance

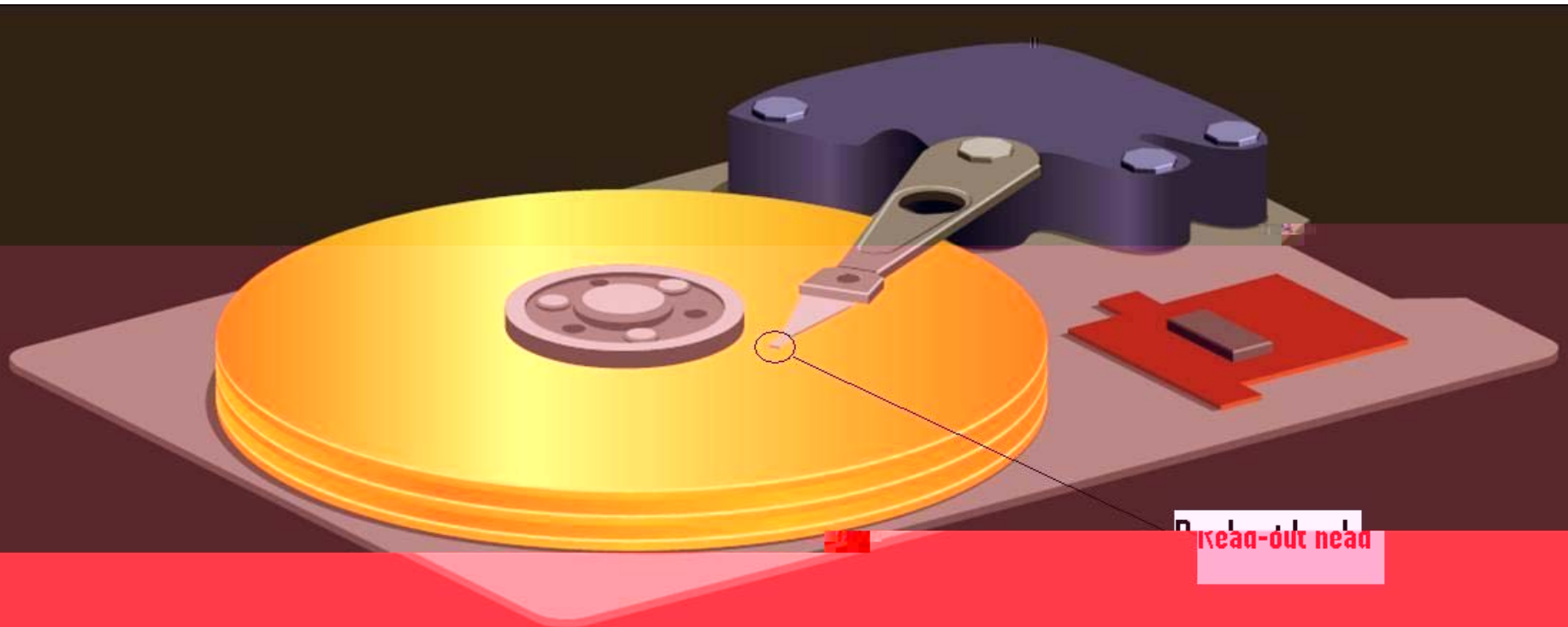
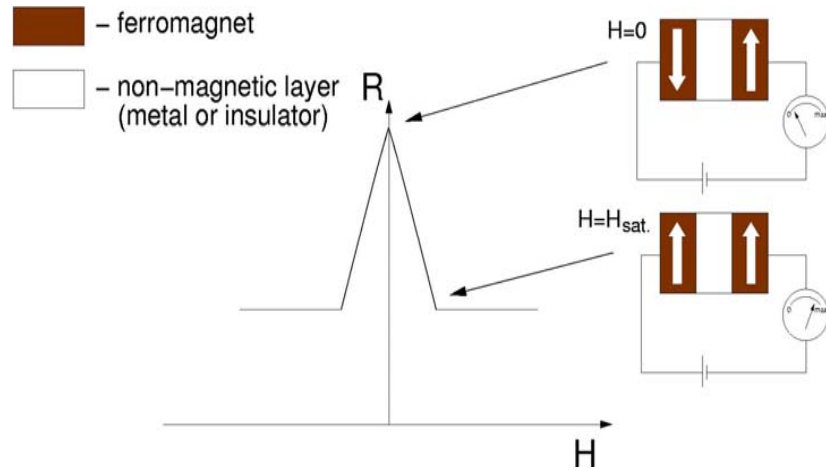
$$MR = \frac{R^{AP} - R^P}{R^P} = \frac{(R_{\uparrow} - R_{\downarrow})^2}{4R_{\uparrow}R_{\downarrow}}$$

spin



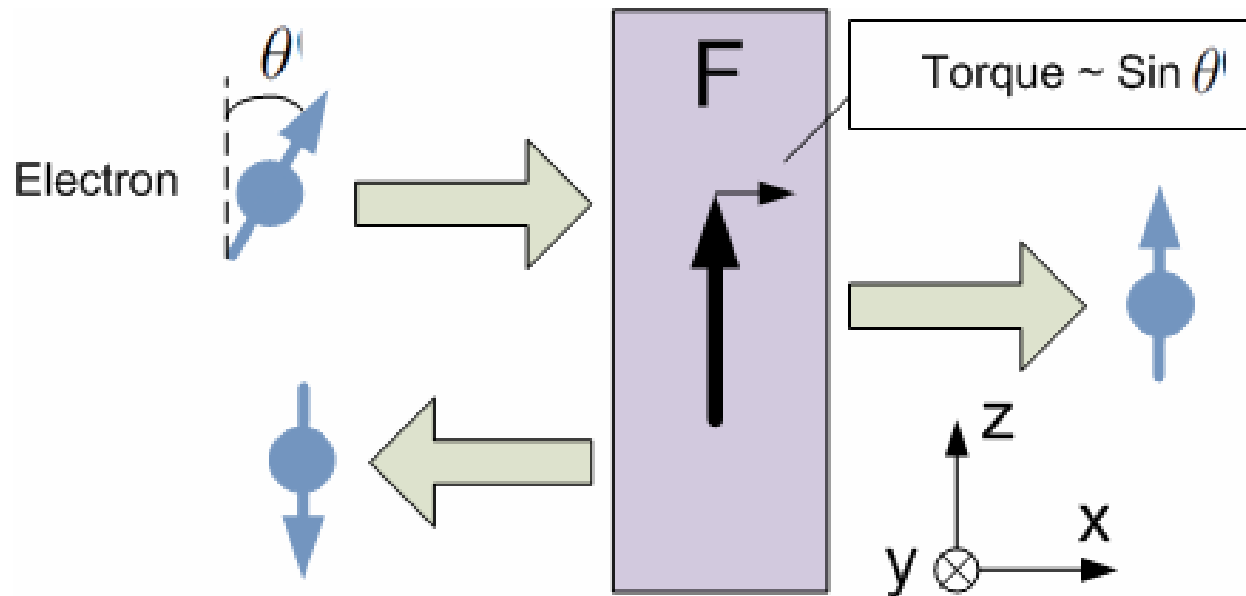
---GMR

-GMR



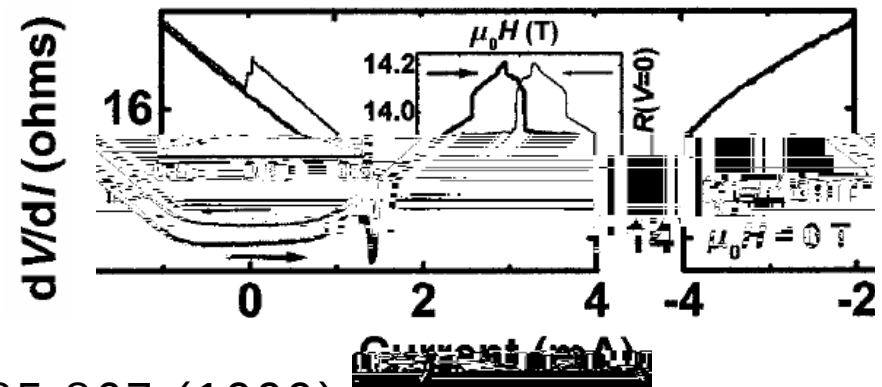
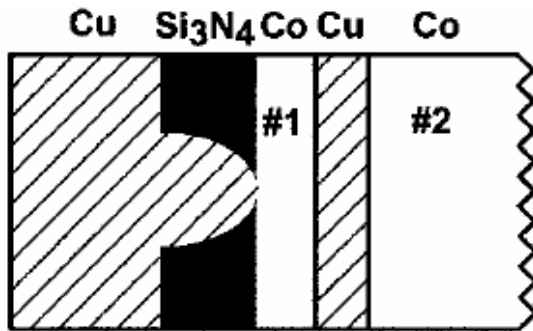
Schematic of exchange torque generated by spin-filtering

$$|\psi_{in}\rangle = \frac{e^{ik_{\uparrow}x}}{\sqrt{k_{\downarrow}}} \cos\left(\frac{\theta}{2}\right) |\uparrow\rangle + \frac{e^{ik_{\downarrow}x}}{\sqrt{k_{\downarrow}}} \sin\left(\frac{\theta}{2}\right) |\downarrow\rangle$$

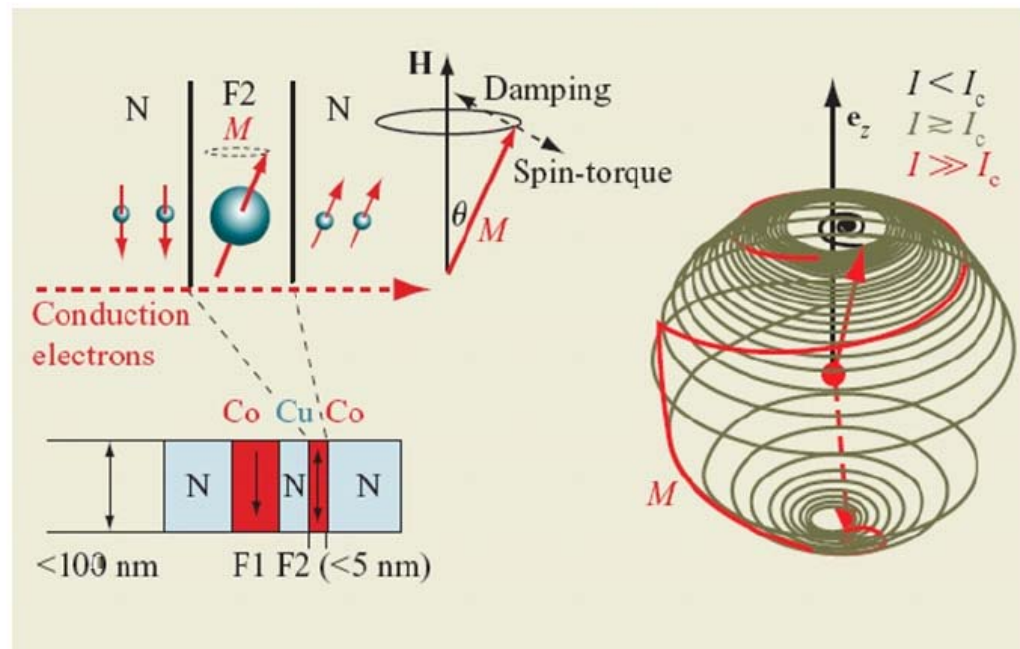


$$|\psi_t\rangle = \frac{e^{ik_{\uparrow}x}}{\sqrt{k_{\uparrow}}} \cos\left(\frac{\theta}{2}\right) |\uparrow\rangle$$

Spin-transfer torques effects (1999)



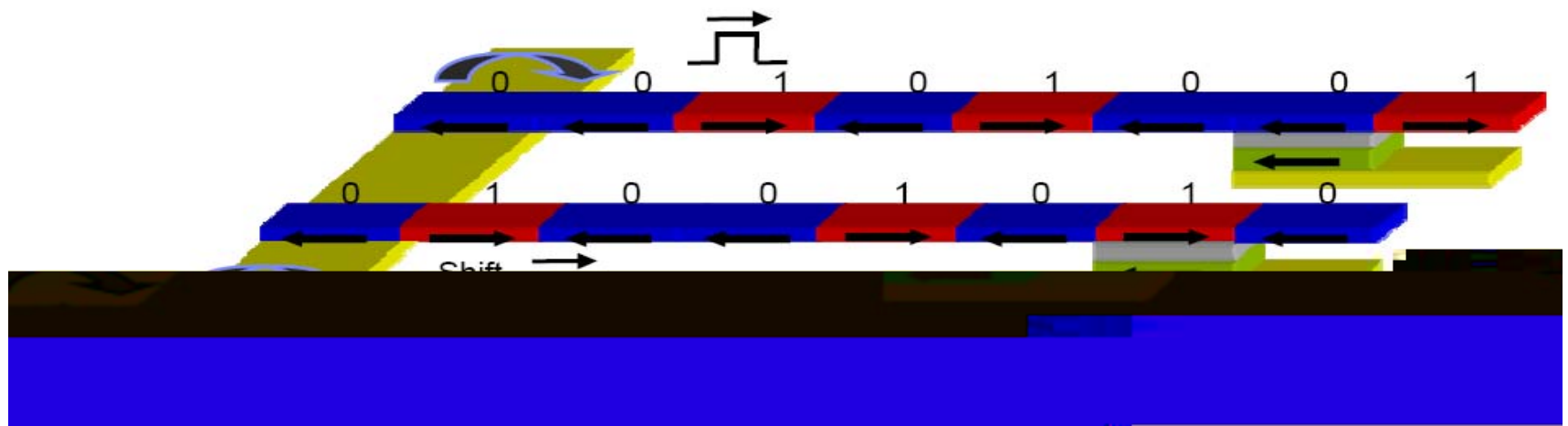
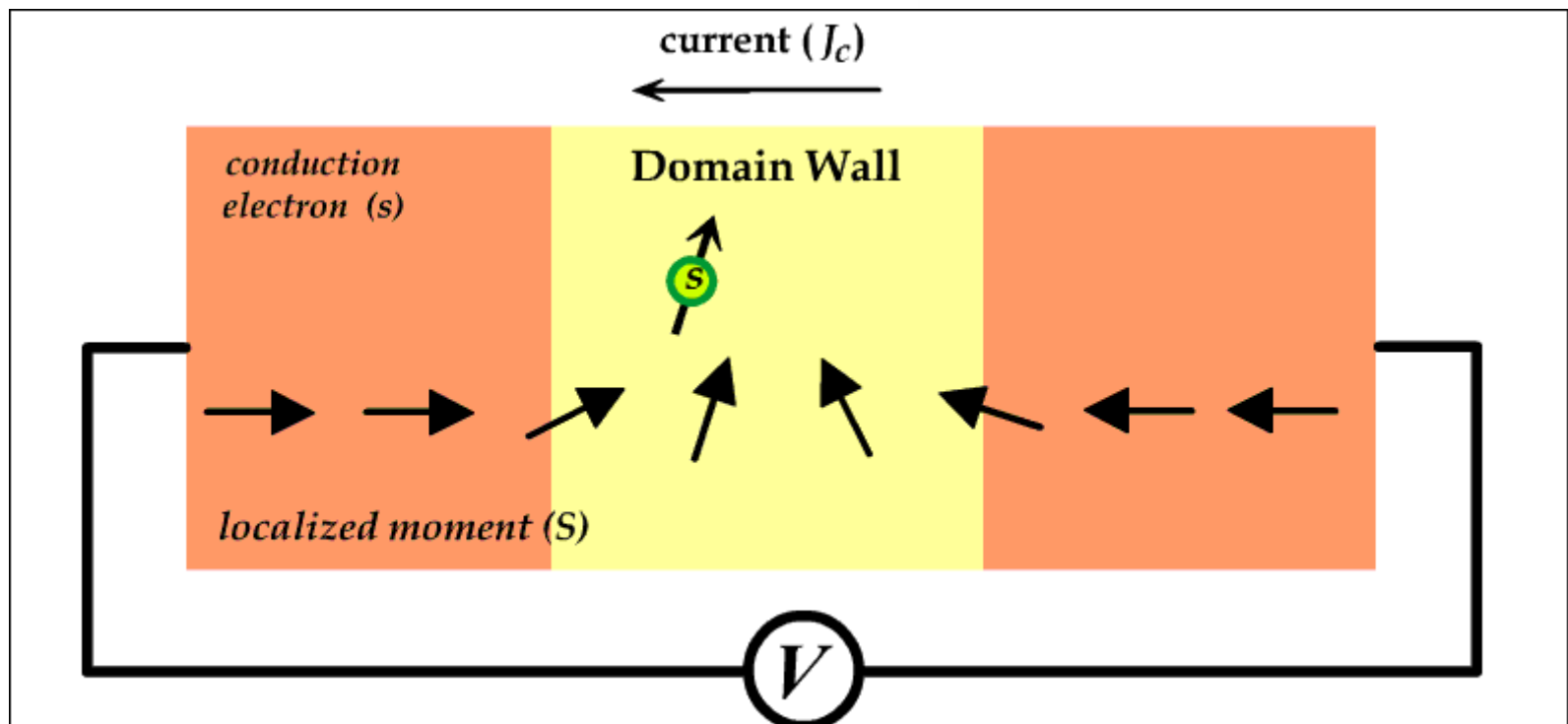
Myers, et al., Science 285,867 (1999)



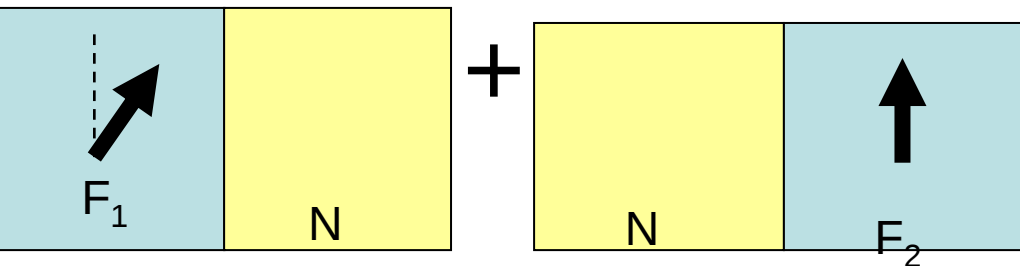
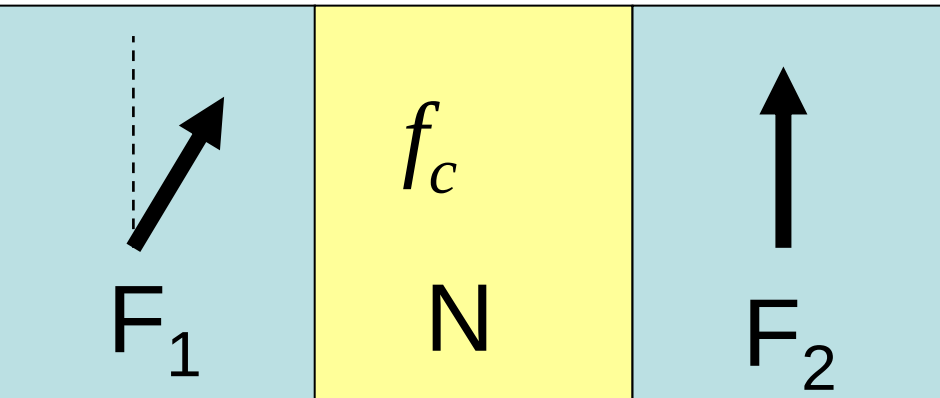
Sun, IBM J. Res. & Dev. 50, 81(2006)

Current-driven domain wall motion:

$$\theta = 2 \cot^{-1} e^{-(z-z_0)/w}$$



Circuit theory_(Batraas2001)



Boundary condition

Charge current

$$I_1 \quad I_2$$

Spin current

$$\mathbf{I}_s \quad \mathbf{I}_s$$



Charge accumulation f_c

Spin accumulation

In-plane torque $\tau = \frac{\hbar}{2e} (\mathbf{I}_{s1} - \mathbf{I}_{s1} \cdot \mathbf{m}_2)$

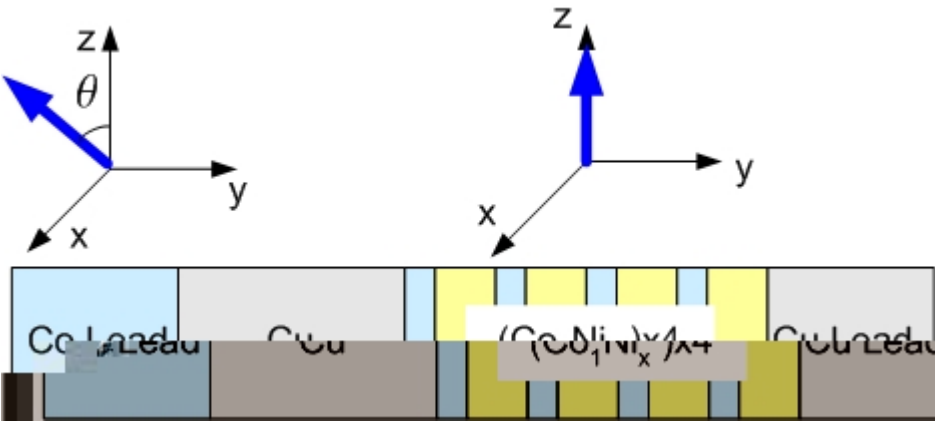
Current and spin current for F_1/N

$$I_1 = (G^\uparrow + G^\downarrow) (f_c^{F1} - f_c^N) + (G^\uparrow - G^\downarrow) (f_s^{F1} - \mathbf{m}_1 \cdot \mathbf{s} f_s^N)$$

$$\begin{aligned} \mathbf{I}_{s1} = & (G^\uparrow + G^\downarrow) (f_c^{F1} - f_c^N) \mathbf{m}_1 \\ & + (2\text{Re}G^{\uparrow\downarrow} - G^\uparrow - G^\downarrow) \mathbf{m}_1 \cdot \mathbf{s} f_s^N \mathbf{m}_1 \\ & - 2\text{Re}G^{\uparrow\downarrow} \mathbf{s} f_s^N + 2\text{Im}G^{\uparrow\downarrow} f_s^N \mathbf{m}_1 \times \mathbf{s} \end{aligned}$$

Methods

First principles approach to spin transfer torques



- First-principles tight-binding LMTO
- Green function method for layered systems.
- Large system with the number of atoms > 1000

Spin current:

$$\hat{\mathcal{J}} \equiv \frac{1}{2} \left[\hat{\sigma} \otimes \hat{\mathbf{V}} + \hat{\mathbf{V}} \otimes \hat{\sigma} \right]$$

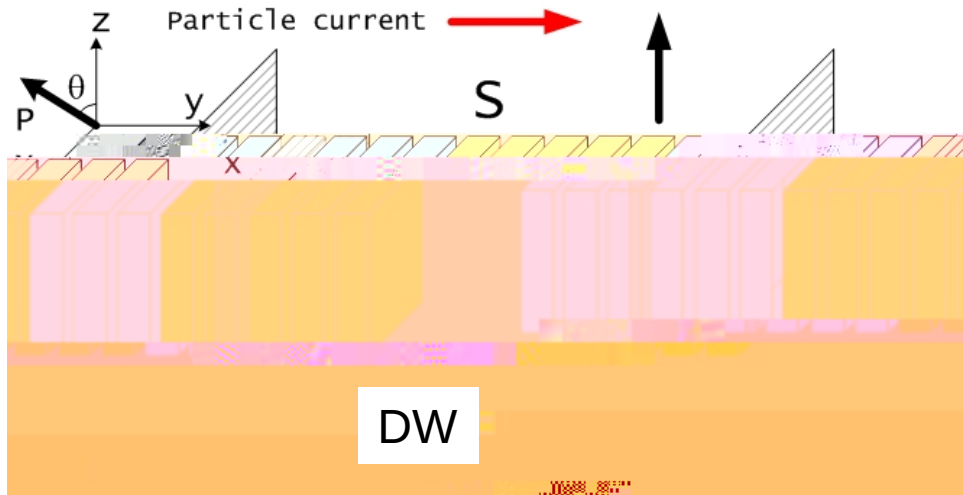
Spin torque from one lead:

$$\left\langle \hat{\mathbf{T}}_{\mathbf{R}}^s(\mathbf{k}_{\parallel}) \right\rangle = \sum_{\mathbf{R}' \in I-1, I} \left\langle \hat{\mathcal{J}}_{\mathbf{R}', \mathbf{R}}^s(\mathbf{k}_{\parallel}) \right\rangle - \sum_{\mathbf{R}' \in I, I+1} \left\langle \hat{\mathcal{J}}_{\mathbf{R}, \mathbf{R}'}^s(\mathbf{k}_{\parallel}) \right\rangle$$

Spin torque on atom R:

$$\mathbf{T}_{\mathbf{R}} = \left(\frac{\hbar}{2} \right) \frac{e}{2h} \frac{1}{N_{\parallel}} \sum_{s, \mathbf{k}_{\parallel}} \left[\left\langle \hat{\mathbf{T}}_{\mathbf{R}}^s(\mathbf{k}_{\parallel}) \right\rangle_{\mathcal{L}} - \left\langle \hat{\mathbf{T}}_{\mathbf{R}}^s(\mathbf{k}_{\parallel}) \right\rangle_{\mathcal{R}} \right] V_b$$

First principles approach to spin transfer torques

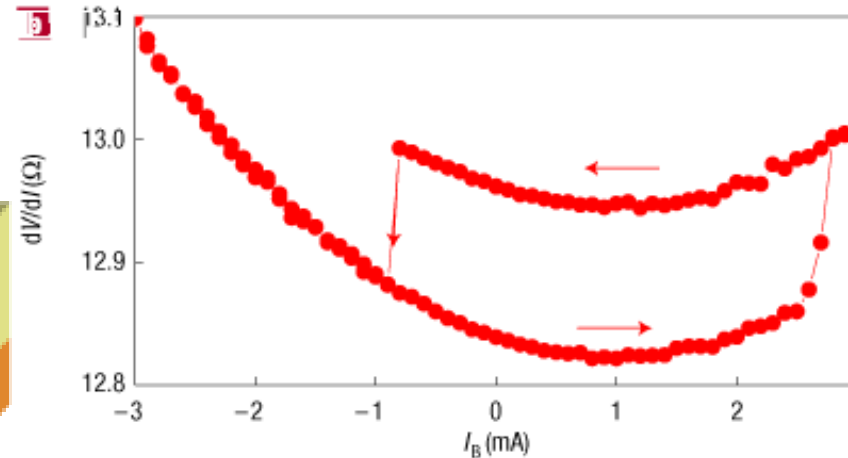
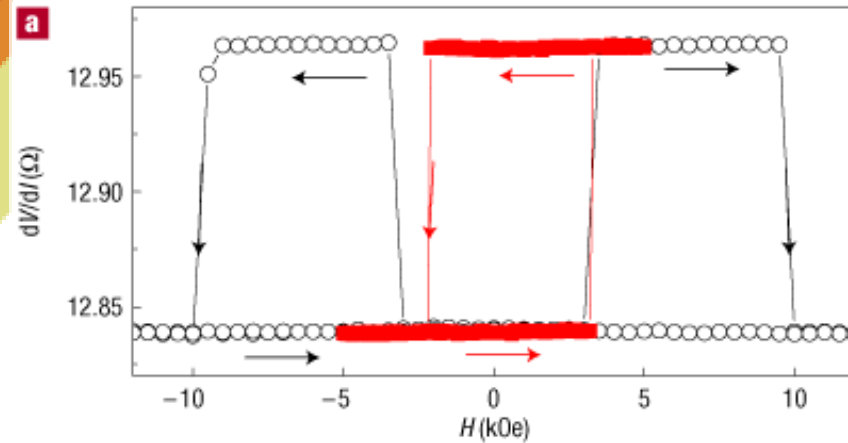
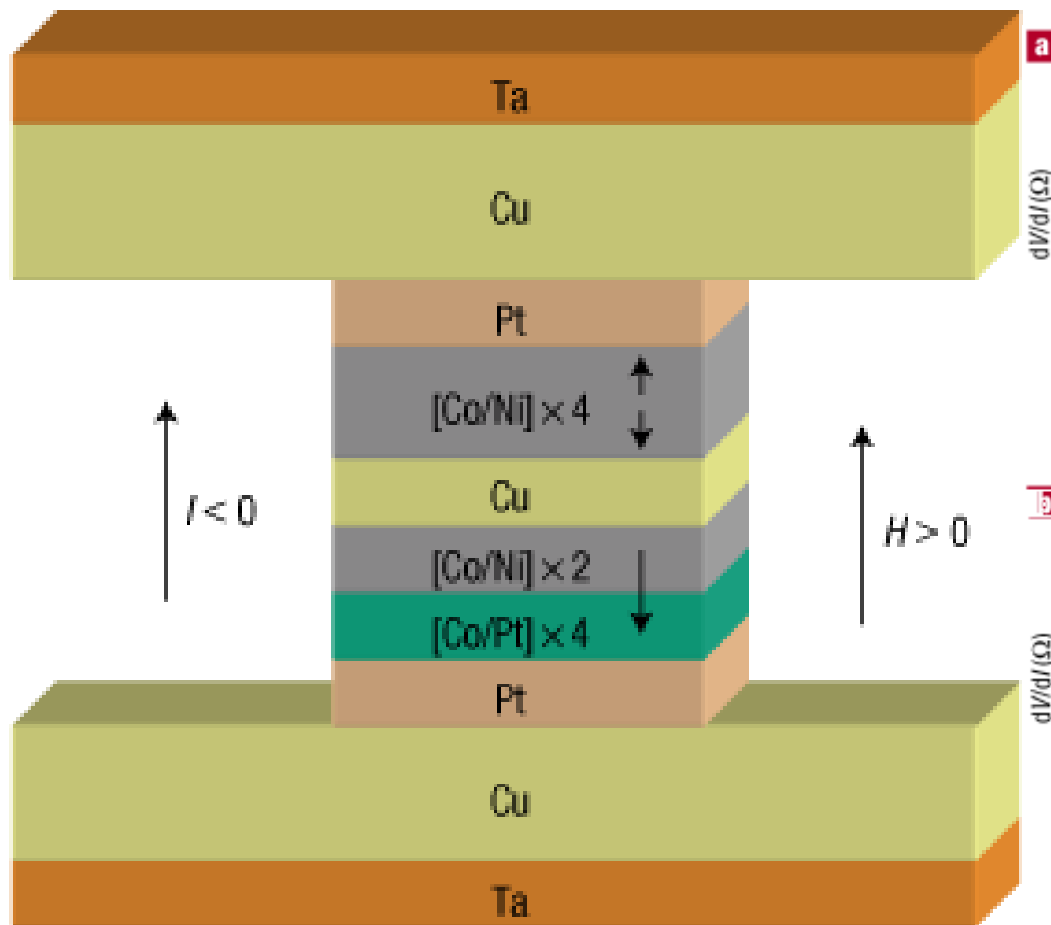


$$\tau \propto \langle \vec{s} \rangle \times \dot{\vec{M}}$$

- TB LMTO
- Green function method
- NEGF if necessary
- Order& disorder

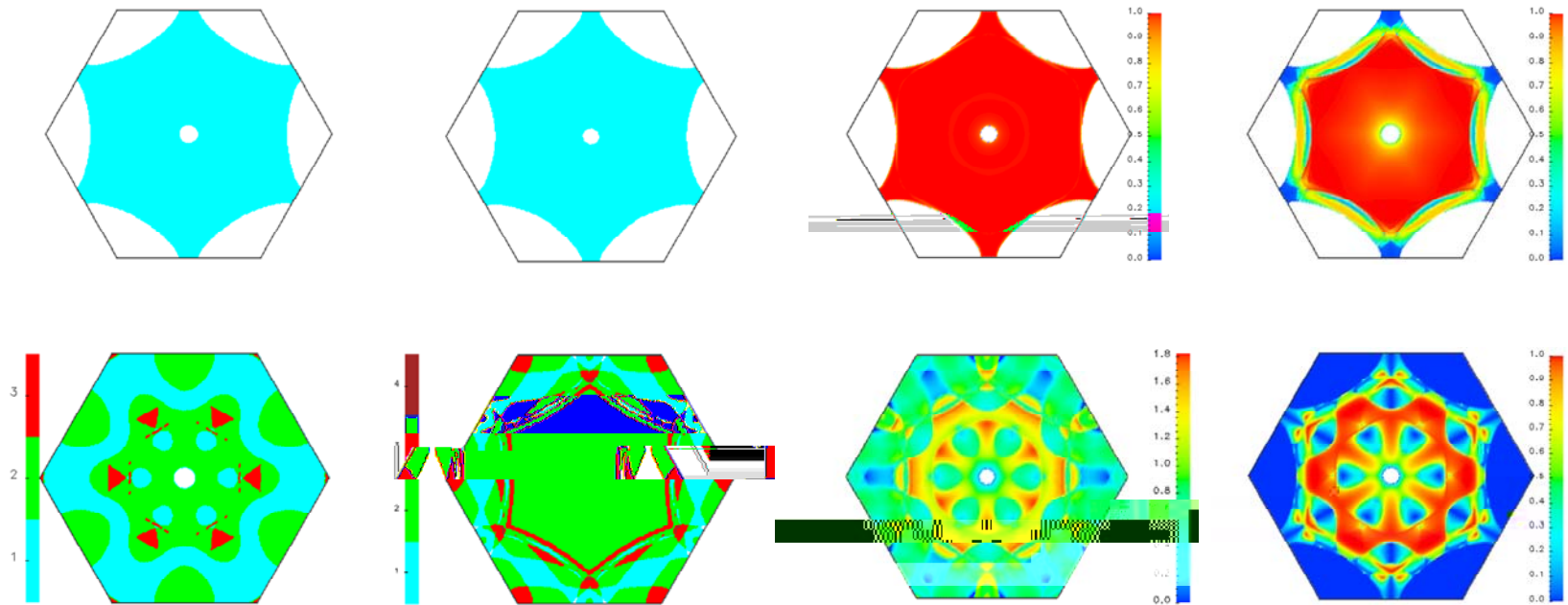
Linear equations of system

$$\begin{pmatrix} \mathbf{C}_0 \\ \mathbf{C}_1 \\ \mathbf{C}_2 \\ \dots \\ \mathbf{C}_N \\ \mathbf{C}_{N+1} \end{pmatrix} = (\mathbf{U}\mathbf{P}\mathbf{U}^+ - \tilde{\mathbf{S}})^{-1} \begin{pmatrix} \mathbf{S}_{0,-1}[\mathbf{F}_L^{-1}(+) - \mathbf{F}_L^{-1}(-)]\mathbf{C}_0(+) \\ 0 \\ 0 \\ \dots \\ 0 \\ 0 \end{pmatrix}$$



S.MANGIN et.al, Nature materials vol5,210, (2006) , D.Ravelosona, et.al, APL 90,072508 (2007), D.Ravelosona, et.al, PRL 96,186604(2006), D.Ravelosona, et.al, J.Phys.D: Appl.Phys.40,1253(2007)

Co|Ni interface

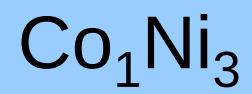


Interface resistance for Co|Ni(111)

AR unit $\text{f}^{-1}\Omega^{-1}\text{m}^{-2}$

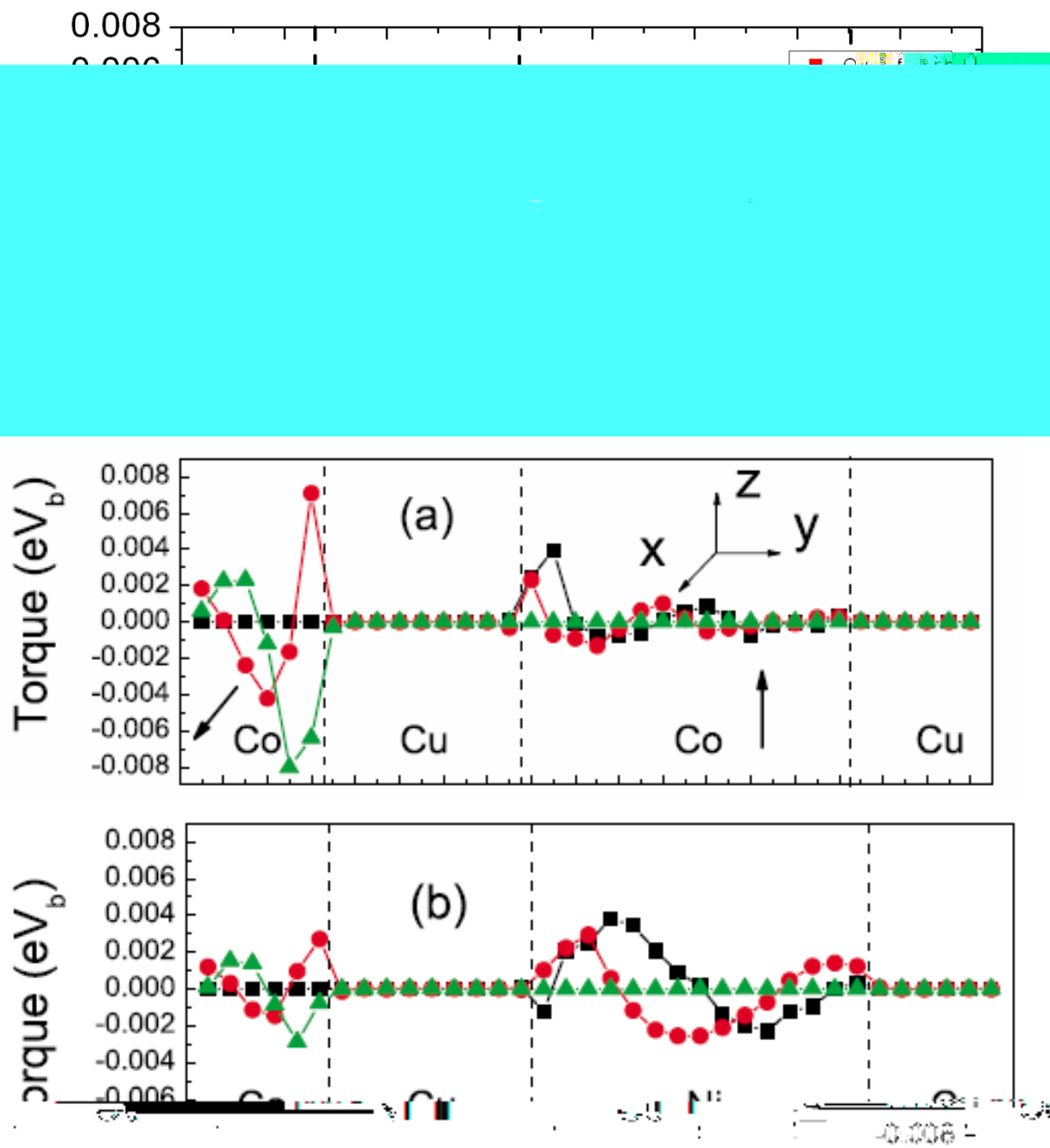
$$\Gamma = \frac{AR_{\downarrow} - AR_{\uparrow}}{AR_{\uparrow} + AR_{\downarrow}} \quad \text{Gamma}$$

Lattice constant		AR(maj.)	AR(min.)	Gamma
Co	3.54 ₉	0.014664	0.725067	0.960353
Ni	3.52 ₄	0.0241504	0.727603	0.935749
1/2(Co+Ni)	3.53 ₇	0.0186835	0.730984	0.950155



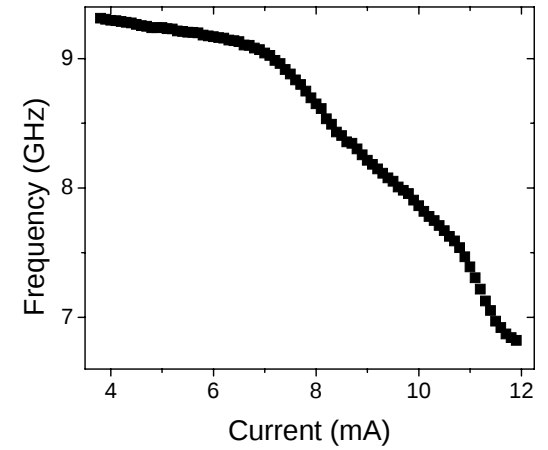
Co

Ni

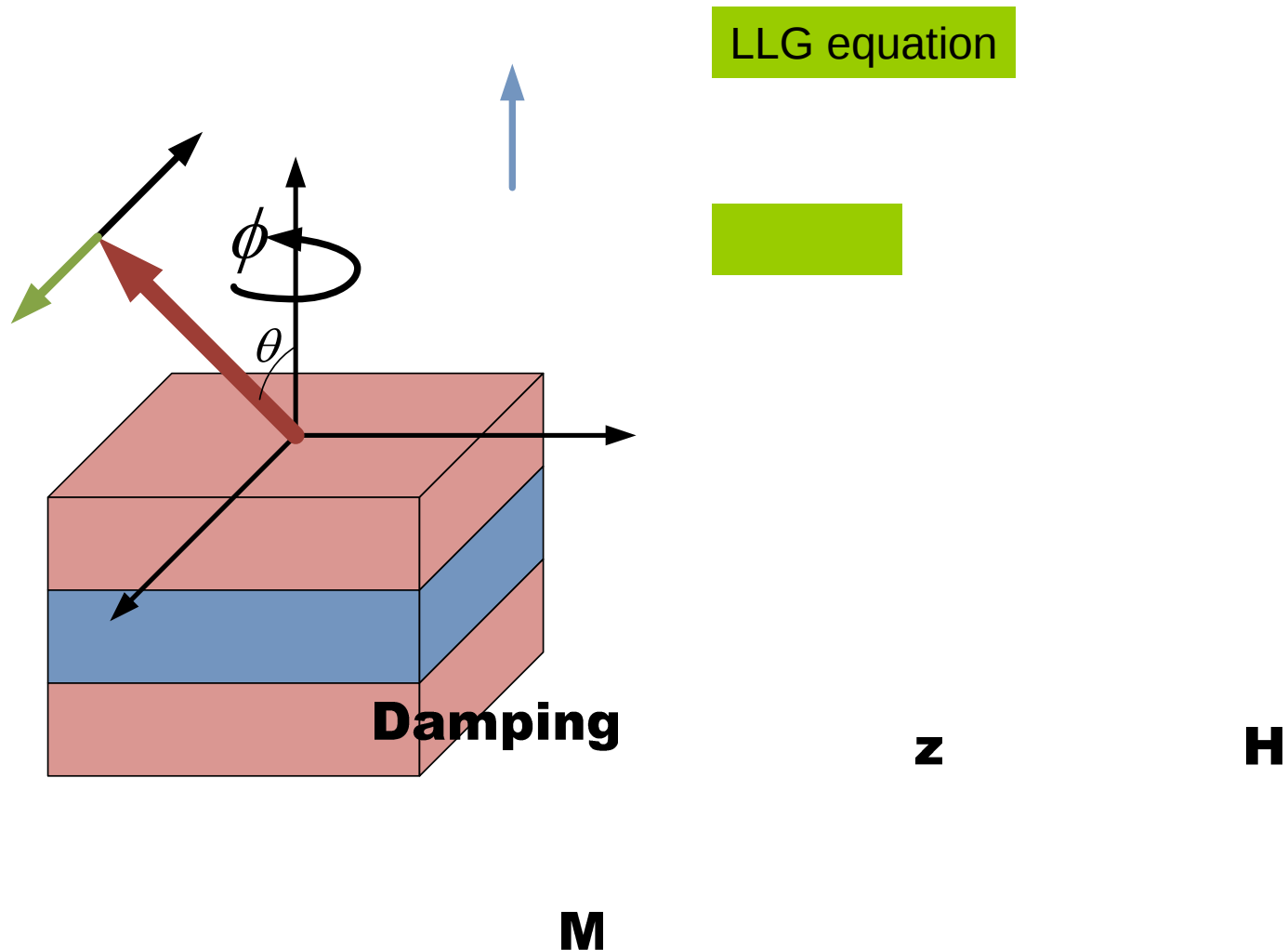


substrate|Ta(3)|Cu(15)|Co₉₀Fe₁₀(20)

|Cu(4.5)|[Co(0.2)|Ni(0.4)]^{x5}|Co(0.3)|Cu(3)|Ta(3)



Spin transfer nanocontact oscillator devices(STNO)



g factor [1]

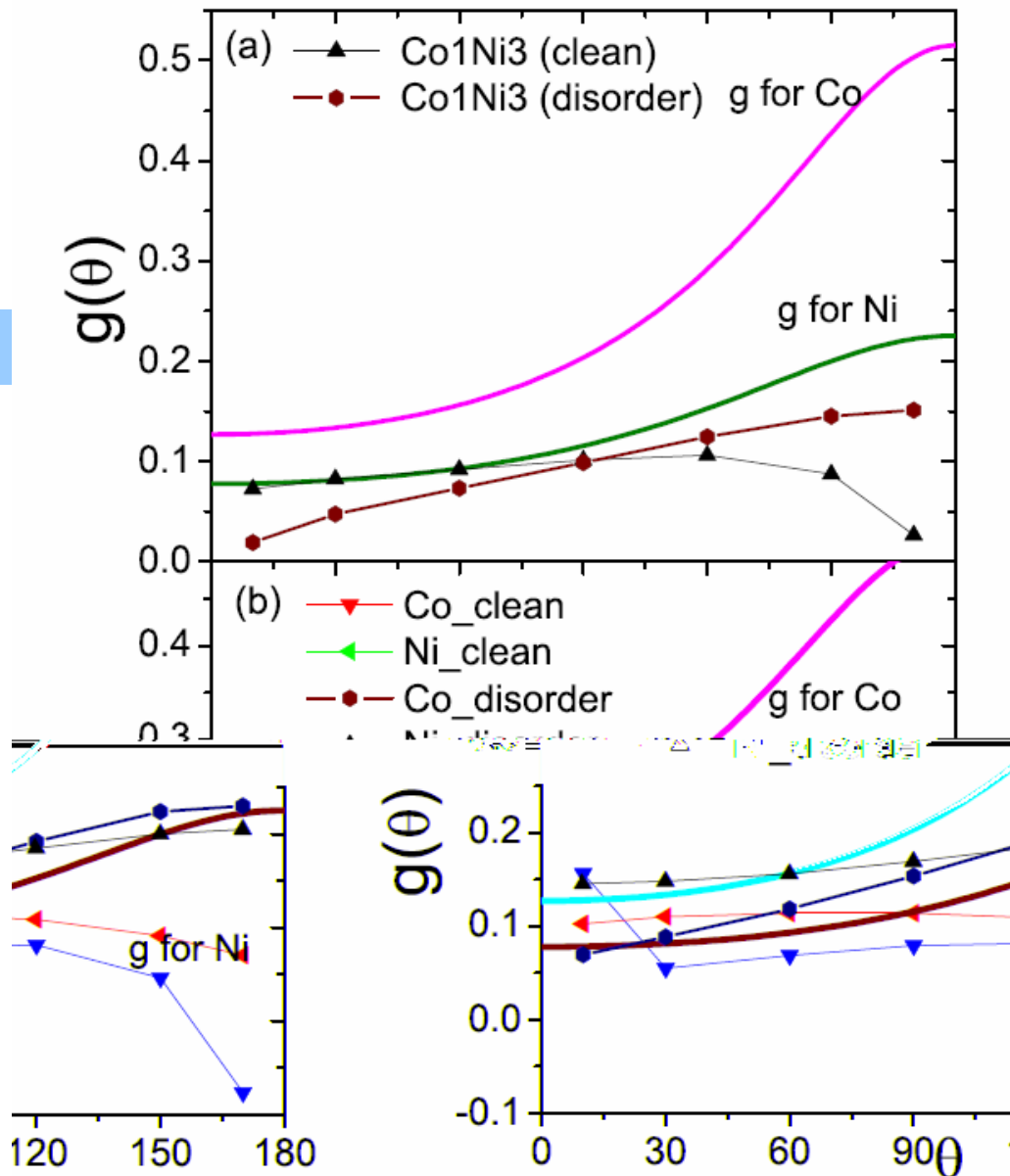
G factor

$$g = \left[-4 + \frac{(1 + P)^3 (3 + \hat{s}_1 \cdot \hat{s}_2)}{4P^{3/2}} \right]^{-1}$$

Here Co P=0.35 Ni P=0.23

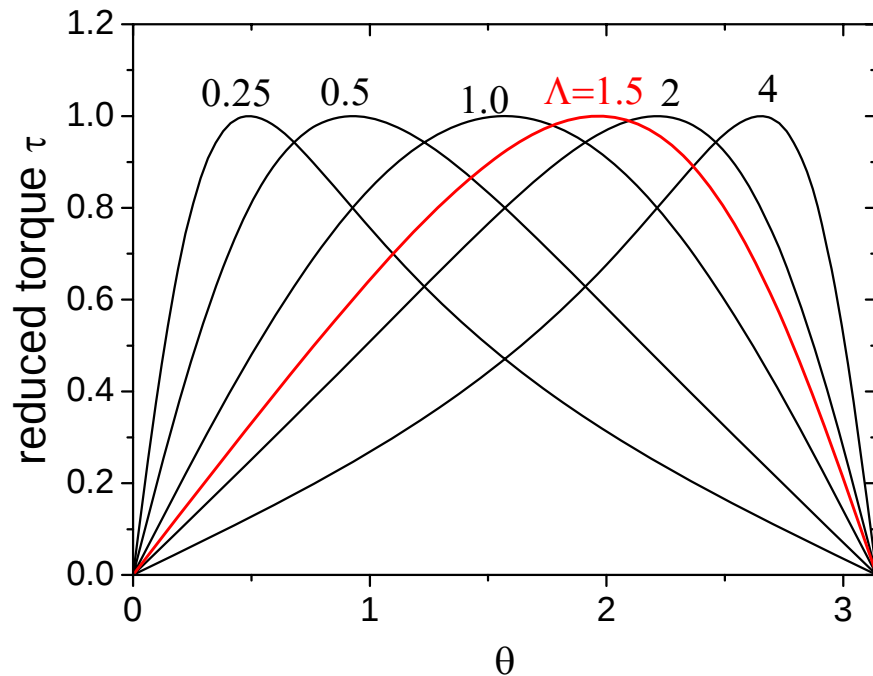
$$g(\theta) = \frac{\text{torque}(\theta)}{I(\theta) \sin(\theta)}$$

G factor can be enhanced by disorder effect.



Reduced torque

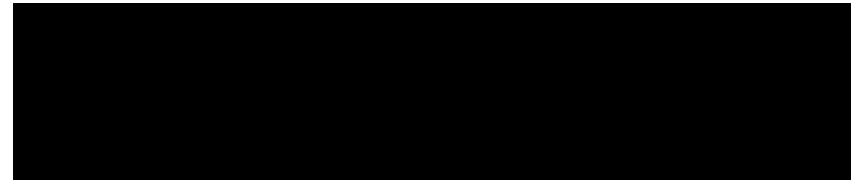
$$\Lambda = 1.5$$

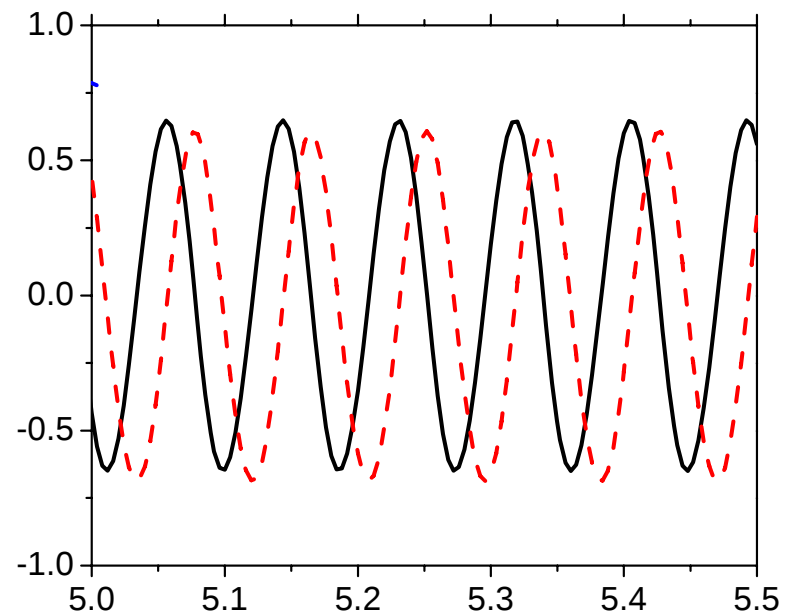


Torques

$$L = \hbar I P_r \Lambda \tau(\theta) / 4 A e$$

Reduced torques

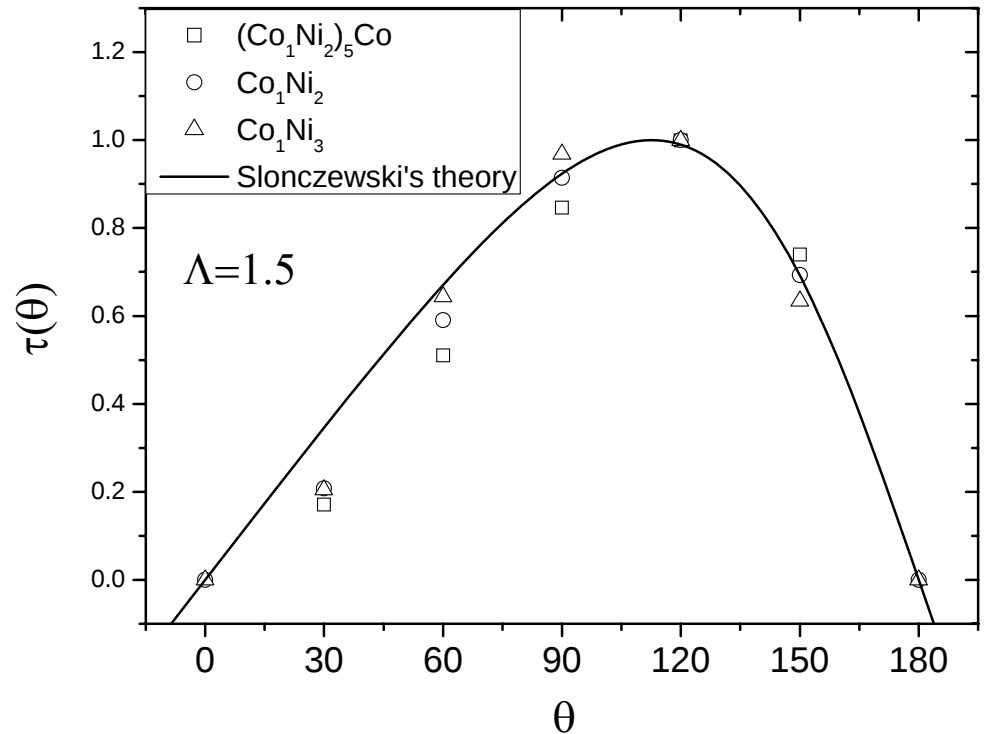




Cu/Co/Cu/(Co₁Ni₂)₅Co/Cu

Reduced torque

$$\tau(\theta) = \frac{t(\theta) / I(\theta)}{(t / I)_{\max}}$$



Experiment $\Lambda = 1.5$

Gilbert Damping In the Presence of Andreev Reflection

Spin Current Induced Dynamics

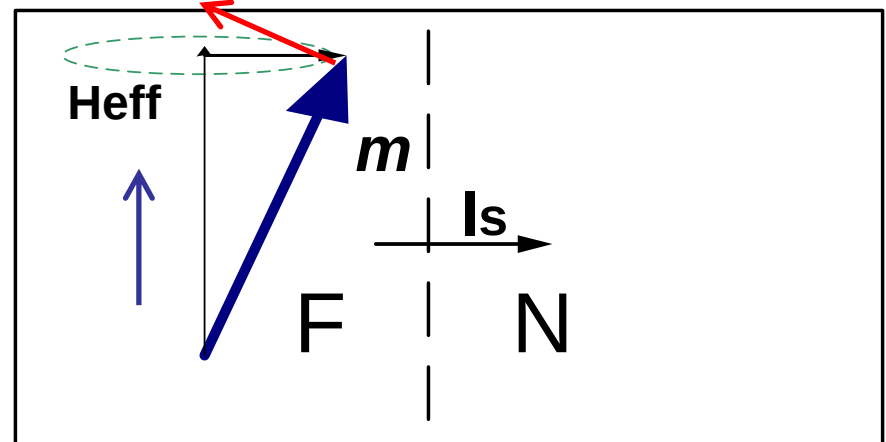
$$\dot{\vec{m}} = \underbrace{\gamma_0 \vec{H}_{eff} \times \vec{m}}_{\text{Precession}} + \underbrace{\alpha_0 \dot{\vec{m}} \times \vec{m}}_{\text{Damping}} + \left. \frac{\partial \vec{m}}{\partial t} \right|_{\text{torque}}$$

Spin Transfer Torque
from current I_s

$$I_s = \frac{\hbar}{4\pi} \left(\text{Re } \mathcal{A}_{eff}^{\uparrow\downarrow} \mathbf{m} \times \frac{d\mathbf{m}}{dt} + \text{Im } \mathcal{A}_{eff}^{\uparrow\downarrow} \frac{d\mathbf{m}}{dt} \right)$$

$\mathcal{A}_{eff}^{\uparrow\downarrow}$

Ferromagnet/Normal Metal



Spin Dependent Scattering Matrix

$$\hat{S} = S^\uparrow u^\uparrow + S^\downarrow u^\downarrow \quad u^{\uparrow/\downarrow} = \frac{1}{2}(\hat{I}_0 \pm \hat{\sigma} \cdot \vec{m})$$

$$\hat{S} = \frac{S^\uparrow + S^\downarrow}{2} \hat{I}_0 + \frac{S^\uparrow - S^\downarrow}{2} \hat{\sigma} \cdot \vec{m}$$

$$\frac{\partial \hat{S}}{\partial X} = S^\uparrow \frac{\partial u^\uparrow}{\partial X} + S^\downarrow \frac{\partial u^\downarrow}{\partial X} = (S^\uparrow - S^\downarrow) \hat{\sigma} \cdot \frac{\partial \vec{m}}{\partial X}$$

EMISSION

$$\frac{d\hat{n}_l}{dX} = \left(\frac{1}{4\pi i} \sum_{nn'l'} \frac{\partial \hat{S}_{nn',ll'}}{\partial X} \hat{S}_{nn',ll'}^\dagger \right) + \text{H.c.}$$

F/N Spin Pump

Current $\hat{I}_{F/N} = e \frac{\partial \hat{N}_{F/N}}{\partial X} \frac{\partial X}{\partial t} = \frac{1}{2} I_C \cdot \hat{i}_0 - \frac{e}{\hbar} \hat{\sigma} \cdot \hat{I}_{F/N}^S$

Precession induced current $\hat{I}_{F/N}^S = \frac{\hbar}{4\pi} \left(\text{Re } A^{\uparrow\downarrow} \vec{m} \times \frac{\partial \vec{m}}{\partial t} + \text{Im } A^{\uparrow\downarrow} \frac{\partial \vec{m}}{\partial t} \right),$

$$I_C = 0.$$

Mixing Conductance (Oshinouchi model)

LLG equation in the presence of spin current pump



$$\frac{\partial \vec{m}}{\partial t} = \gamma_0 \vec{H}_{eff} \times \vec{m} + \alpha_0 \frac{\partial \vec{m}}{\partial t} \times \vec{m} + \frac{\gamma \hbar}{4\pi M_s V} (A_r^{\uparrow\downarrow} \vec{m} \times \frac{\partial \vec{m}}{\partial t} + A_i^{\uparrow\downarrow} \frac{\partial \vec{m}}{\partial t})$$

Effective Damping Enhancement

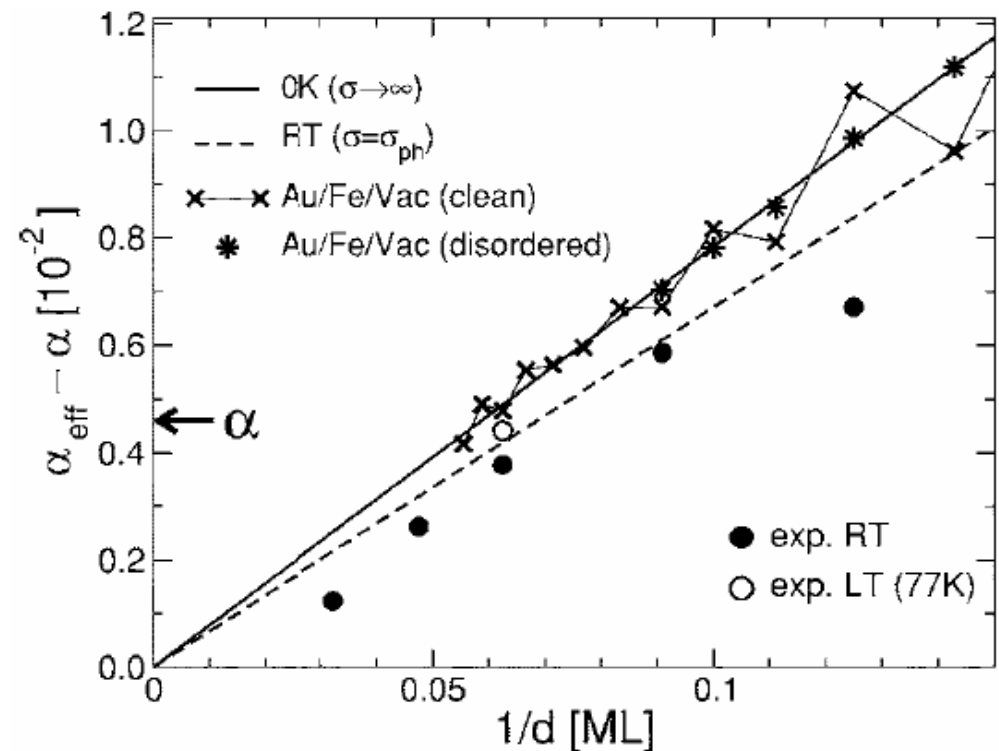
$$\frac{\partial}{\partial t} \vec{m} = -\gamma_{eff} \vec{m} \times \vec{H}_{eff} + \alpha_{eff} \vec{m} \times \frac{\partial}{\partial t} \vec{m}$$

$$\frac{\gamma}{\gamma_{eff}} = 1 - \frac{\gamma \hbar}{4\pi M_s V} A_i^{\uparrow\downarrow}$$

$$\alpha_{eff} = \frac{\alpha + \frac{\gamma \hbar}{4\pi M_s V} A_r^{\uparrow\downarrow}}{1 - \frac{\gamma \hbar}{4\pi M_s V} A_i^{\uparrow\downarrow}}$$

Tserkovnyak, Y. et al

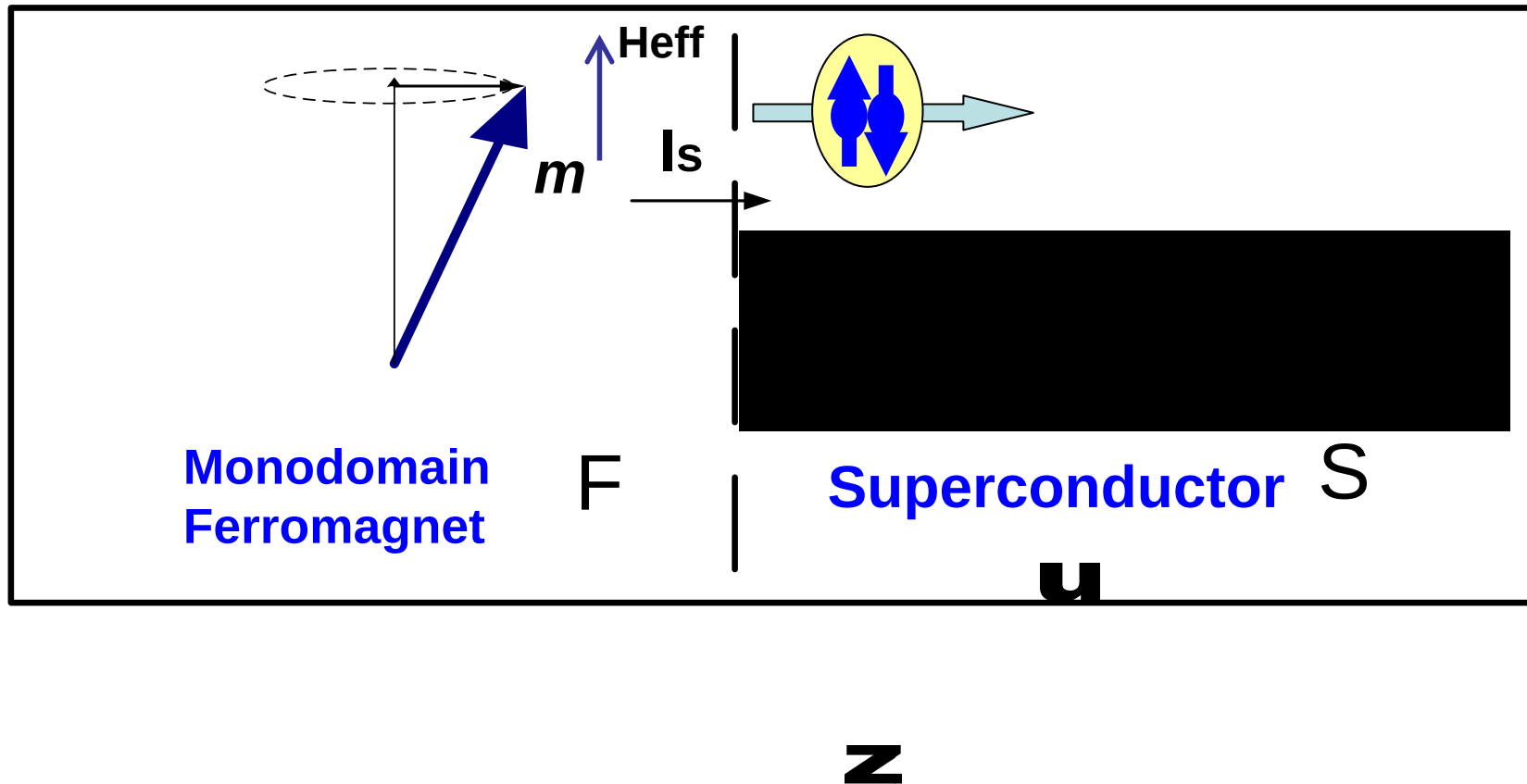
Rev. Mod. Phys. ,77 ,4(2005)



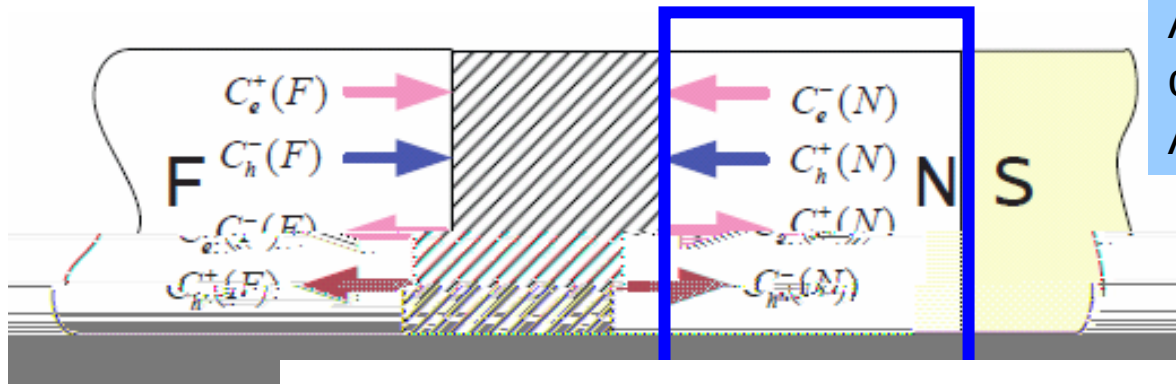
Urban. R et al Phys. Rev. Lett. 87, 217204(2001)

Heinrich, B. et al, J. Appl. Phys. 93,7545(2003)

Spin Pump at F/S Contacts



F/N/S Interface Approach



At N|S interface we consider there is only Andreev reflection.

At F/N Interface

$$\begin{pmatrix} c_e^-(F) \\ c_e^+(N) \end{pmatrix} = \begin{pmatrix} r_{11}^e & t_{12}^e & 0 & 0 \\ t_{21}^e & r_{22}^e & 0 & 0 \\ 0 & 0 & r_{11}^h & t_{12}^h \\ 0 & 0 & t_{21}^h & r_{22}^h \end{pmatrix} \begin{pmatrix} c_e^+(F) \\ c_e^-(N) \\ c_h^-(F) \\ c_h^+(N) \end{pmatrix}$$

We are interested in wave functions in the *F* layer

Spin Current in the Presence of Andreev Reflection

Linear Response & Circuit Theory



Spin current and Damping

Current $\hat{I}_{F/S} = \frac{1}{2} I_C \cdot \hat{i}_0 - \frac{e}{\hbar} \hat{\sigma} \cdot \hat{I}_{F/S}^S \quad I_C = 0,$

$$\hat{I}_{F/S}^S = \frac{\hbar}{4\pi} \int d\varepsilon \left(-\frac{\partial f}{\partial \varepsilon} \right) \left(\text{Re } G^{\uparrow\downarrow}(\varepsilon) \vec{m} \times \frac{\partial \vec{m}}{\partial t} + \text{Im } G^{\uparrow\downarrow}(\varepsilon) \frac{\partial \vec{m}}{\partial t} \right)$$

Effective Damping

$$\alpha_{eff} = \frac{\alpha_0 + \frac{\gamma \hbar}{4\pi M_S V} \int d\varepsilon \left(-\frac{\partial f}{\partial \varepsilon} \right) \text{Re } G_{F/S}^{\uparrow\downarrow}(\varepsilon)}{\gamma_0 - \frac{\gamma \hbar}{4\pi M_S V} \int d\varepsilon \left(-\frac{\partial f}{\partial \varepsilon} \right) \text{Im } G_{F/S}^{\uparrow\downarrow}(\varepsilon)}$$

Mixing Conductance and Andreev Reflection

$$G^{\uparrow\downarrow}(\varepsilon) \equiv \left(N_{\text{Sharvin}} - |R_{he}^{\uparrow\uparrow}(\varepsilon)|^2 - |R_{he}^{\uparrow\downarrow}(\varepsilon)|^2 - |R_{he}^{\downarrow\uparrow}(\varepsilon)|^2 - |R_{he}^{\downarrow\downarrow}(\varepsilon)|^2 \right) - R_{ee}^{\uparrow\uparrow}(\varepsilon) R_{ee}^{\downarrow\downarrow\dagger}(\varepsilon)$$

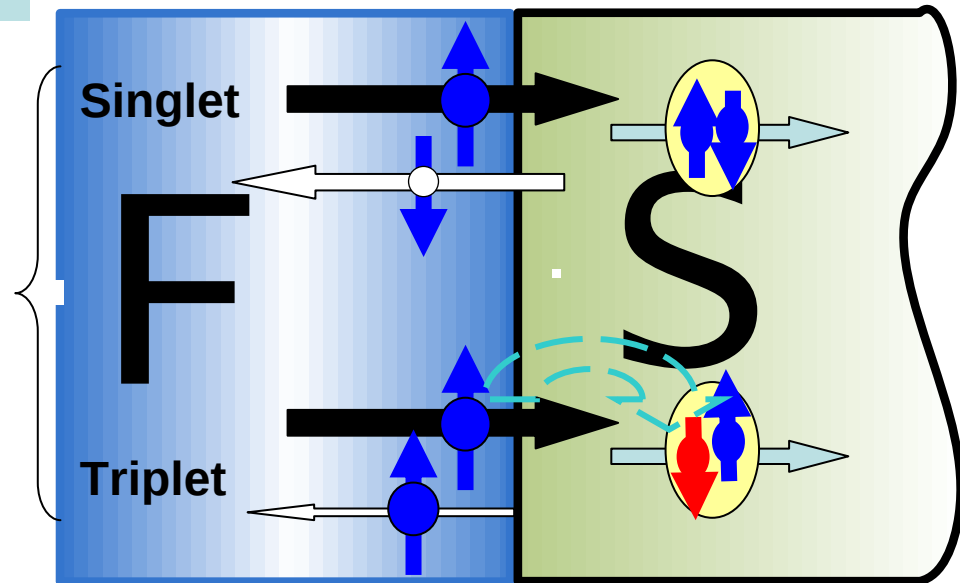
Normal Reflection

$$+ R_{he}^{\downarrow\uparrow}(\varepsilon) R_{he}^{\uparrow\downarrow\dagger}(\varepsilon) + R_{he}^{\uparrow\uparrow}(\varepsilon) R_{he}^{\downarrow\downarrow\dagger}(\varepsilon)$$

Singlet

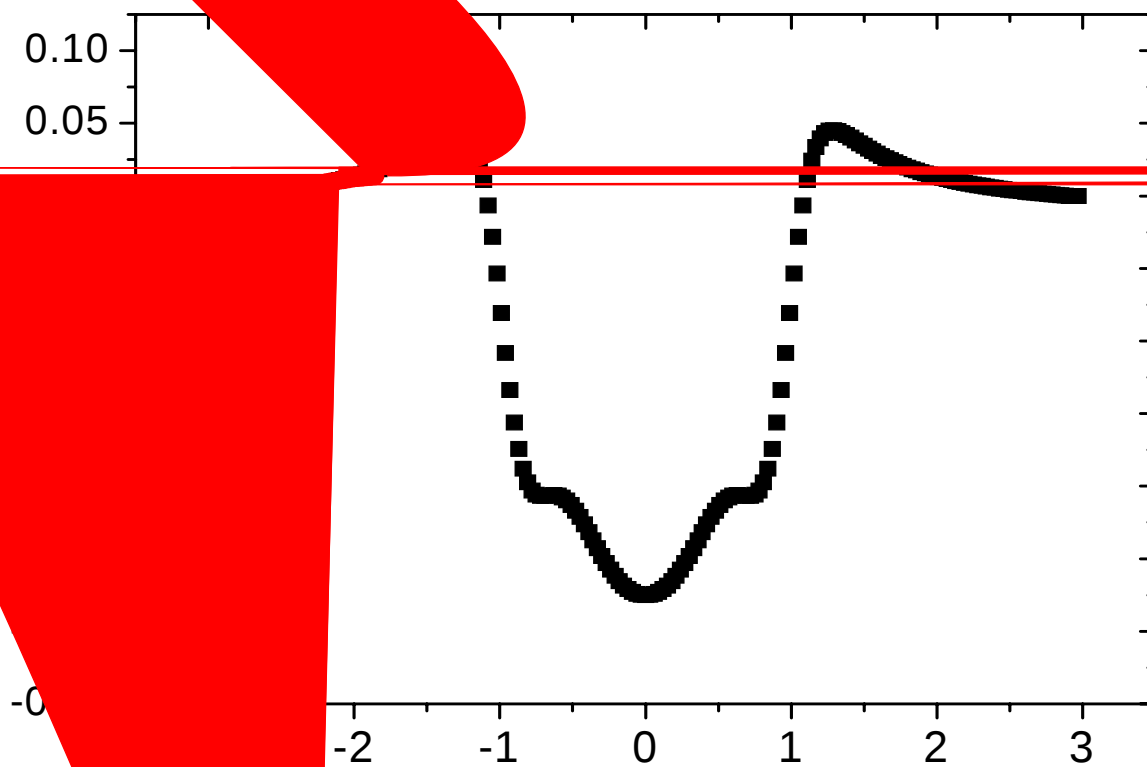
Triplet

R_{he}



Andreev Reflection

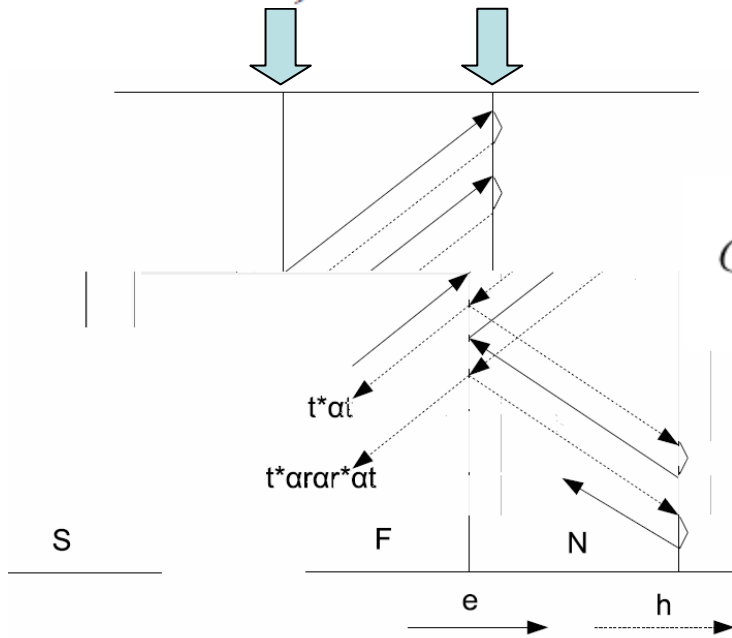
Charge Conductance Spectrum



$$r'_{\uparrow(\downarrow)} = |r'_{\uparrow(\downarrow)}| e^{i\phi_{\uparrow}(\phi_{\downarrow})}$$

$$\hat{t}, \hat{r} \alpha = e^{-i \arccos(\varepsilon / \Delta_0)} r_{he} = t^* \alpha t + t^* \alpha r \alpha r^* \alpha t + t^* \alpha [r \alpha r^* \alpha]^2 t + \dots$$

$$= t^* \alpha [1 - r \alpha r^* \alpha]^{-1} t$$



$$G_0 = \frac{2e^2}{h} |t_{\uparrow}|^2 |t_{\downarrow}|^2, \quad R^2 = |r'_{\uparrow}| |r'_{\downarrow}|$$

$$G_{FS}(\varepsilon) = \frac{G_0}{1 + R^4 - 2R^2 \cos \left(-2 \arccos \frac{\varepsilon}{\Delta_0} + \phi_{\uparrow} - \phi_{\downarrow} \right)}$$

$$\varepsilon / \Delta_0 = \cos \frac{\phi_{\uparrow} - \phi_{\downarrow}}{2}$$

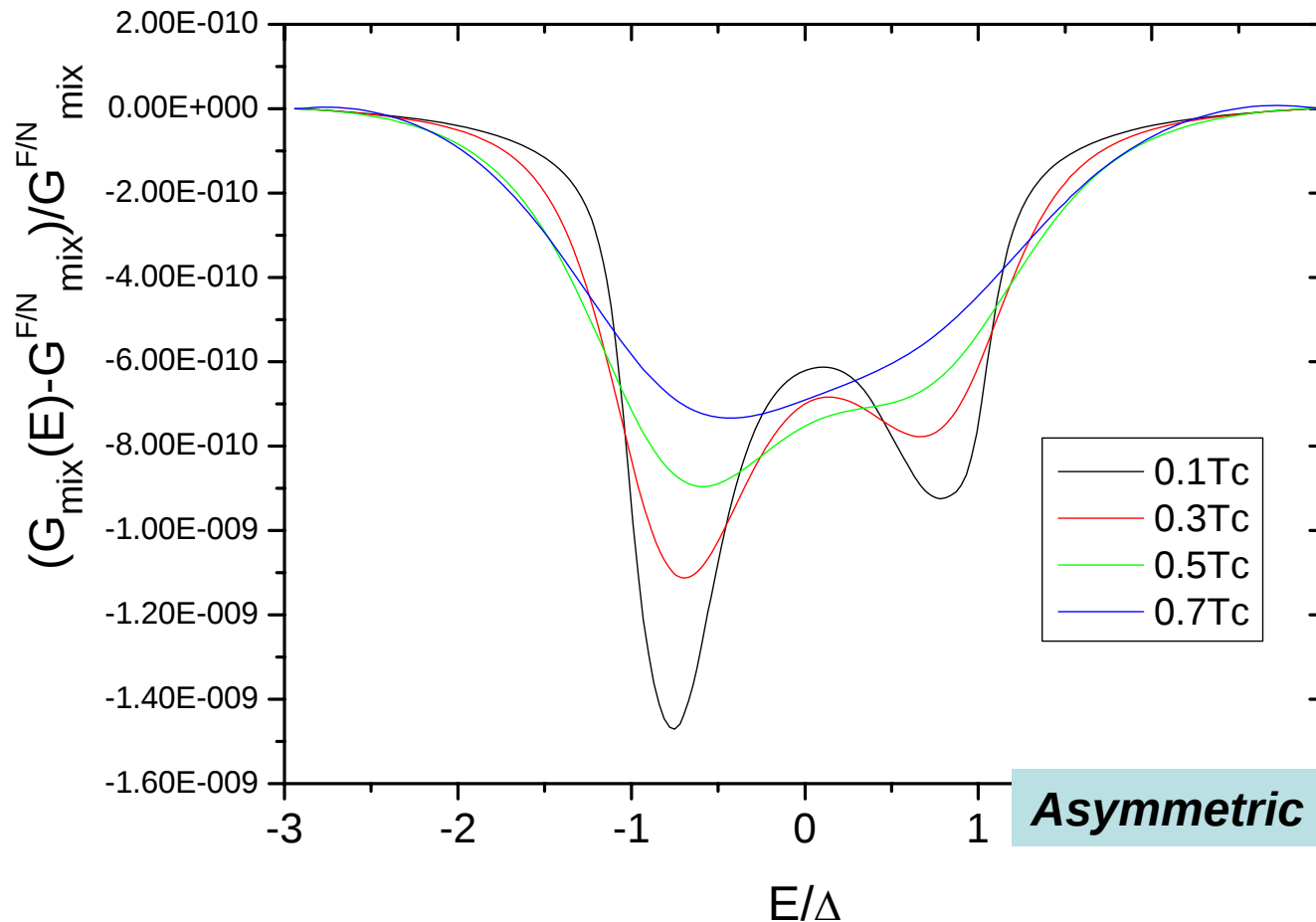
F/N

$$\langle G_{FS}(\varepsilon) \rangle = \frac{G_0}{\left| \frac{1}{2\varphi} \int_{-\varphi}^{\varphi} \left(1 - R^2 e^{-i2 \arccos \frac{\varepsilon}{\Delta_0}} e^{i\delta} \right) d\delta \right|^2}$$

$$\delta = \phi_{\uparrow} - \phi_{\downarrow}$$

Mixing Conductance Spectrum

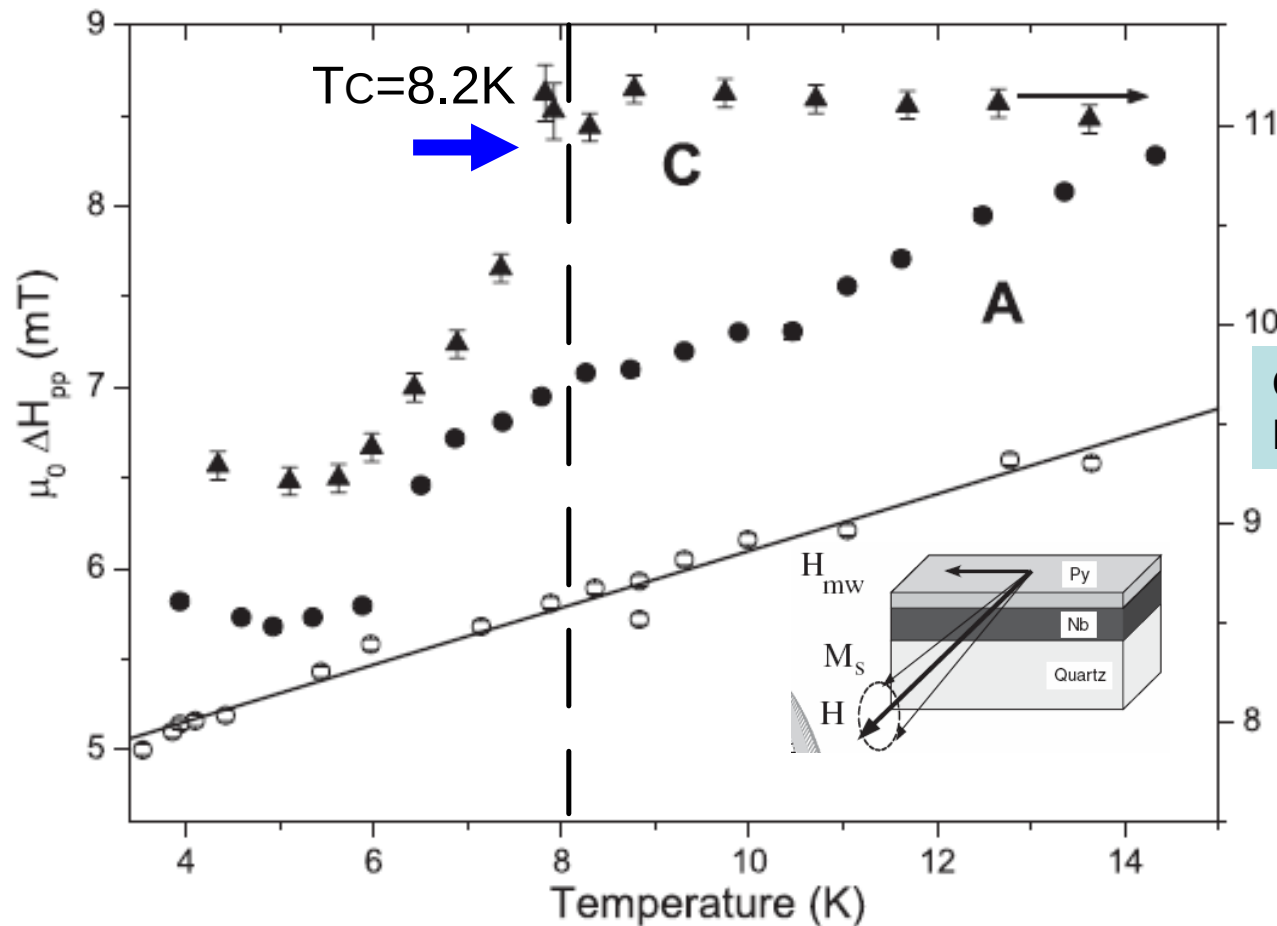
$$G_{ee}^{\uparrow\downarrow} = G_{ne}^{\uparrow\downarrow} + G_{n\bar{e}}^{\uparrow\downarrow \text{singlet}} + G_{n\bar{e}}^{\uparrow\downarrow \text{triplet}}$$



Asymmetric Peaks below the gap

Temperature Dependence of Gilbert Damping Enhancement

Experiment: FMR linewidth



Sample A,C
Superconductor

Sample B

Non-superconductor

C. Bell J. Aarts *et al*
Phys.Rev.Lett.100,047002(2008)

Temperature Dependence of Gilbert Damping Enhancement

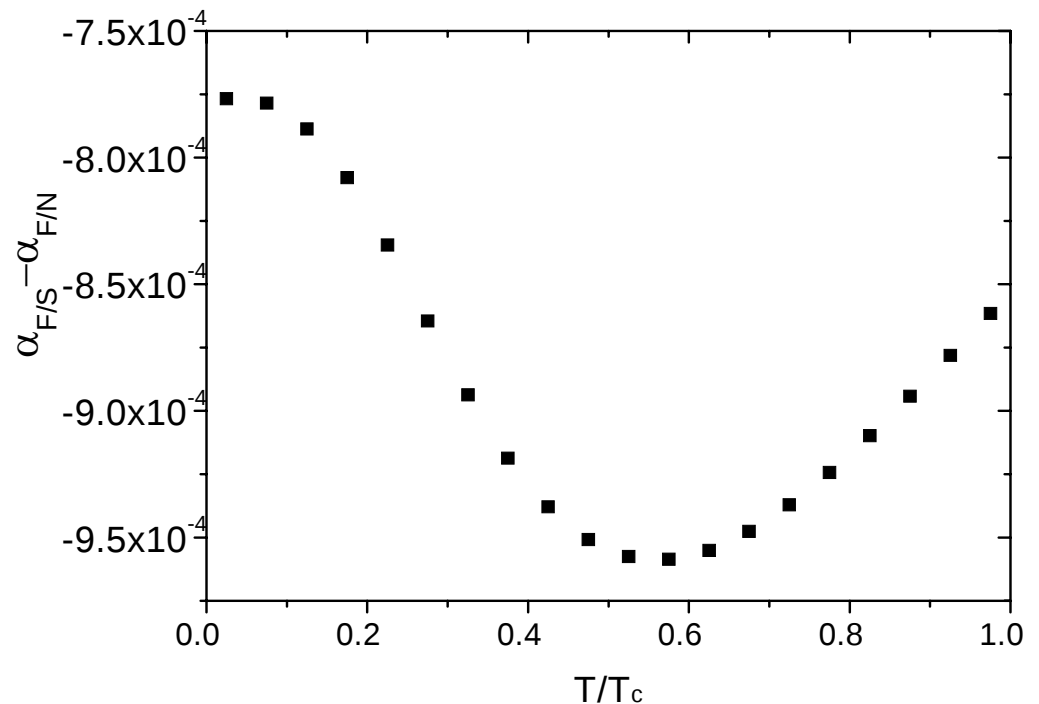
$T \rightarrow T_c, \Delta(T) \rightarrow 0, R_{he} \rightarrow 0, \delta\alpha_{F/S}(T)$ reduces to

$$\delta\alpha_{F/S} = N_{\text{eff}} \frac{\partial f}{\partial \varepsilon} - T \text{Tr} \left(R^{\uparrow\uparrow} R^{\downarrow\downarrow\dagger} \right)$$

$\frac{\partial f}{\partial \varepsilon} = \frac{1}{4\pi M_s V} \frac{\partial f}{\partial \varepsilon}$

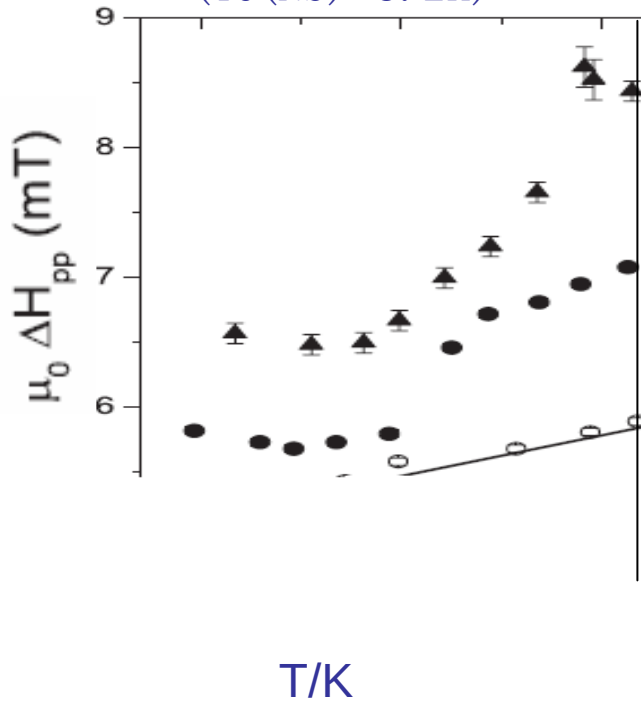
For $\mu_{\text{Fe}} = 2.2\mu_B$

(Thickness of F layer is 10ML)



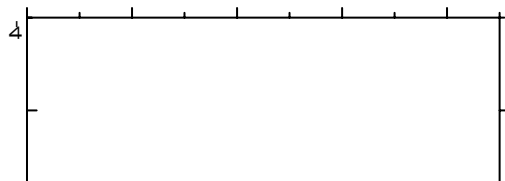
Temperature Dependence of Gilbert Damping Enhancement

FMR Experiment
($T_c(\text{Nb}) = 8.2\text{K}$)

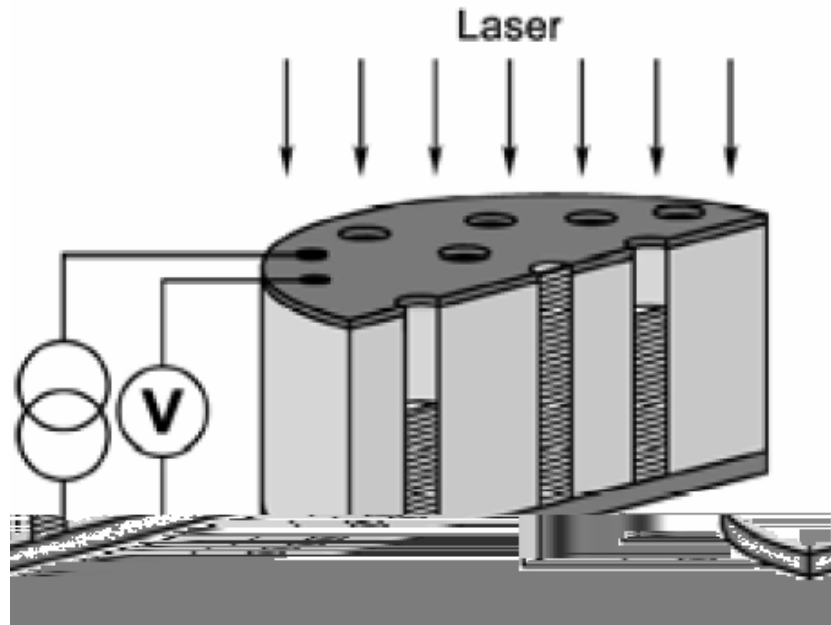
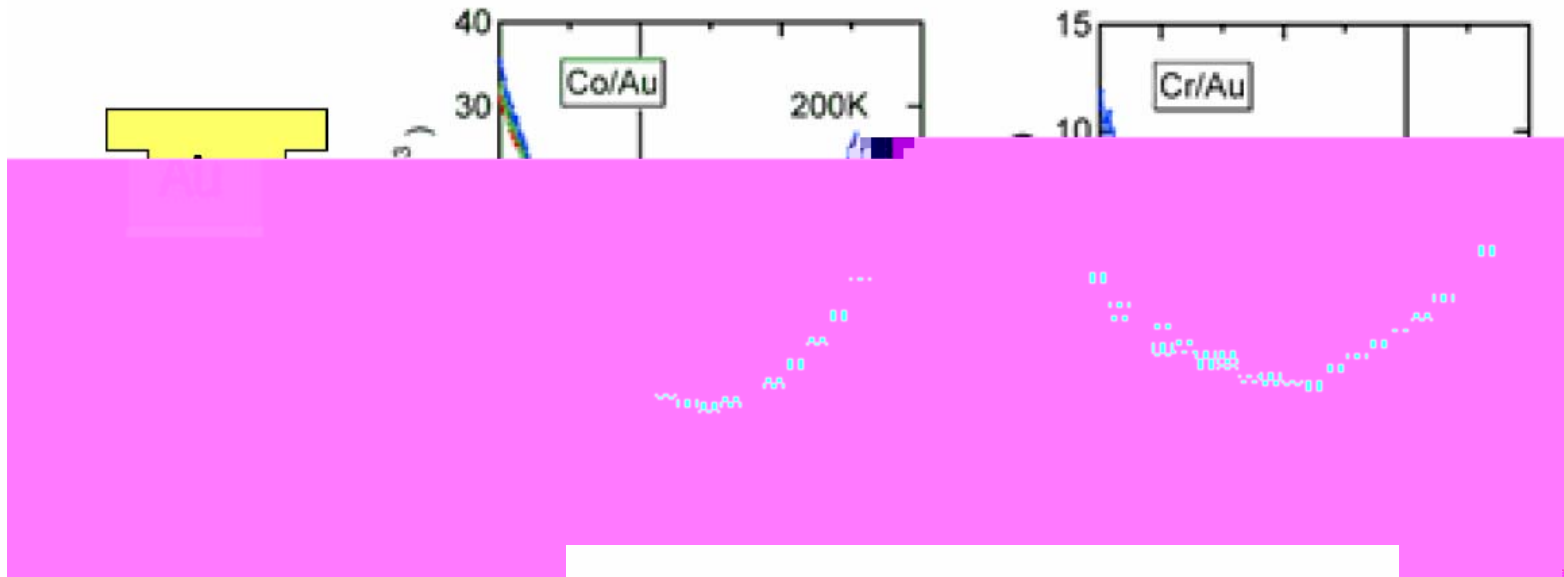


-7.5×10^{-4}
 -8.0×10^{-4}
 -8.5×10^{-4}
 -9.0×10^{-4}
 -9.5×10^{-4}

0.4 0.6 0.8 1.0

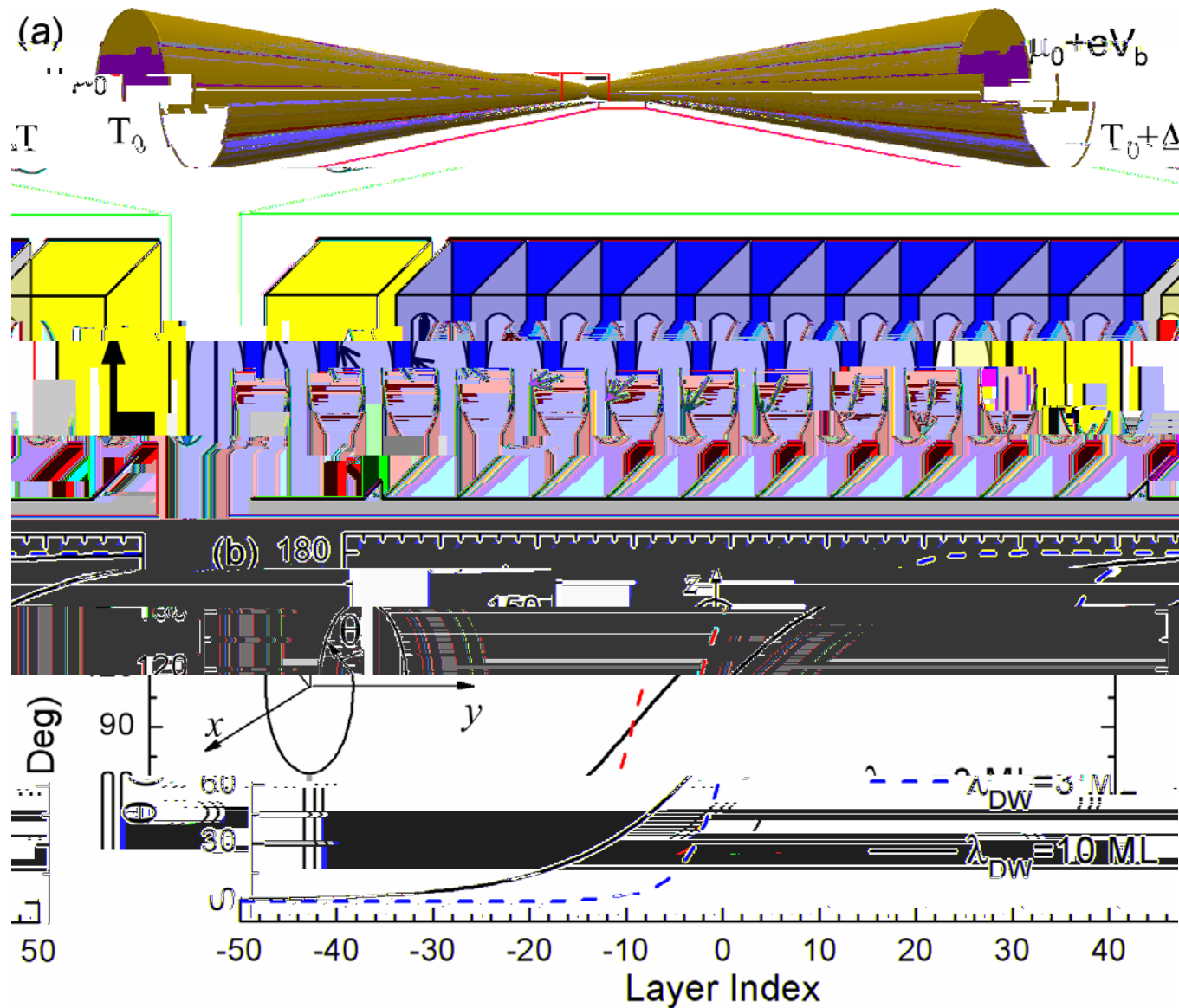


Metallic nanopillars (Fukushima et al., 2005)



L. Gravier et al. (2005).

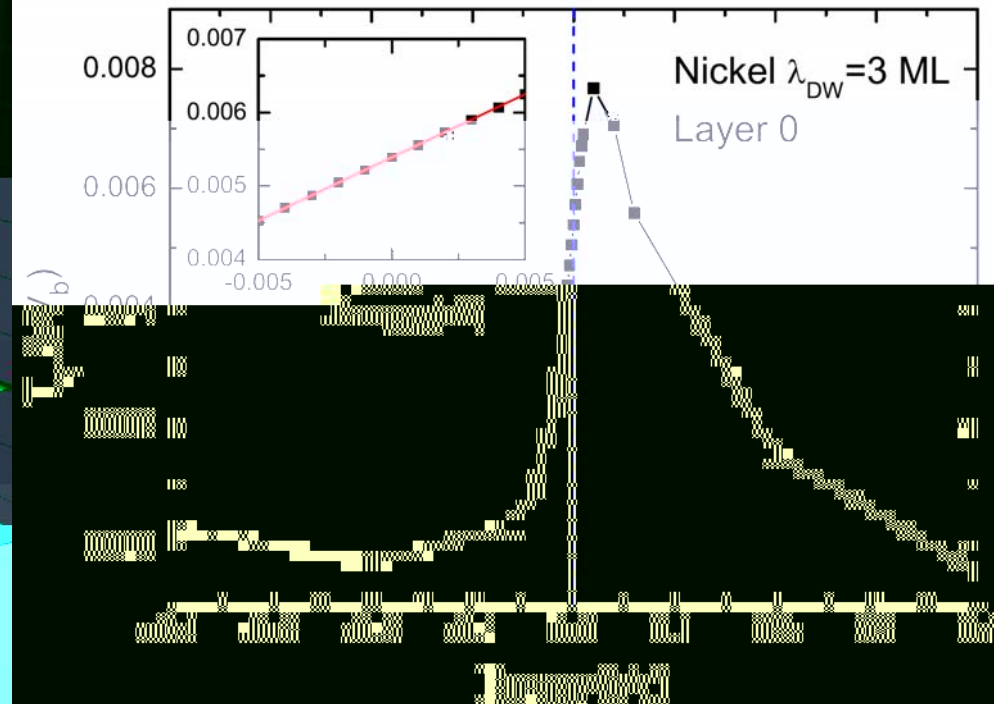
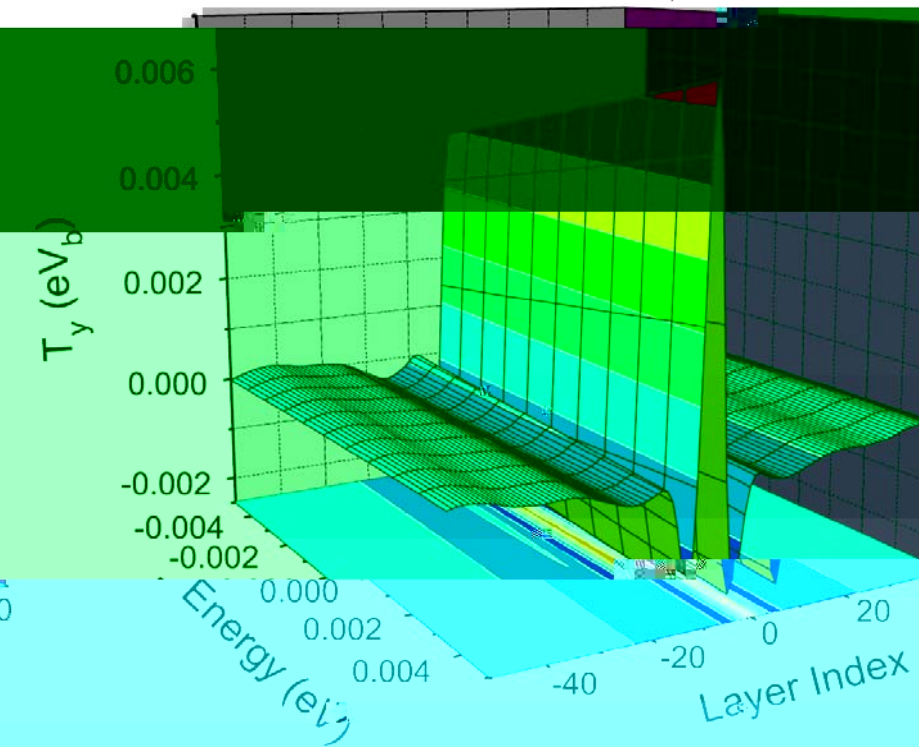
Model



First-principles spin-transfer torque

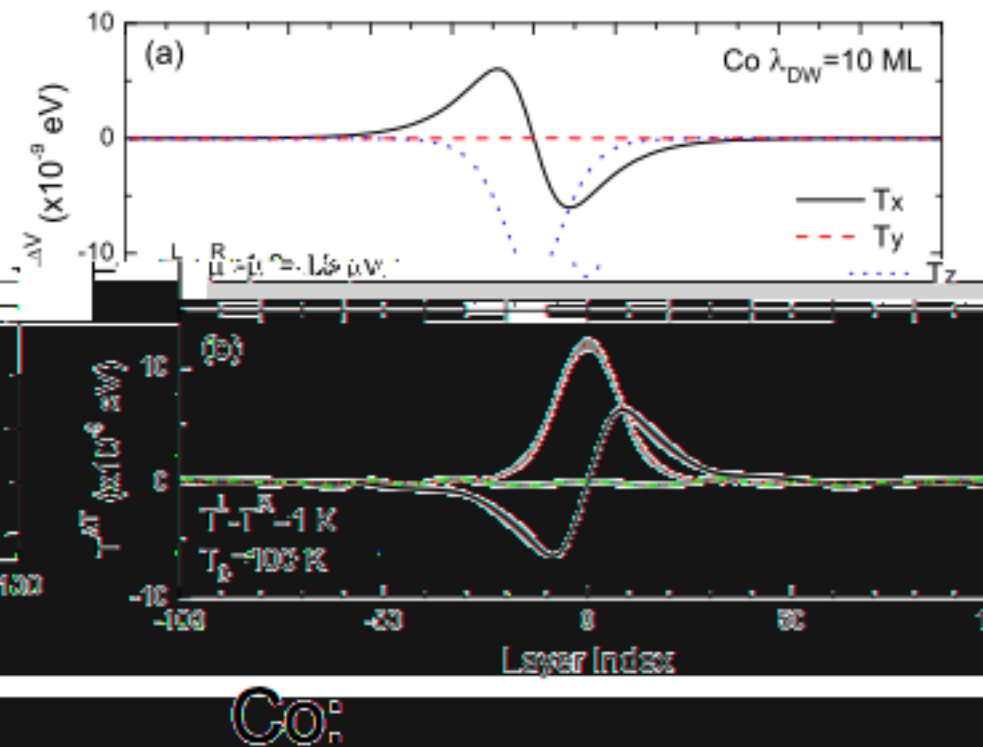
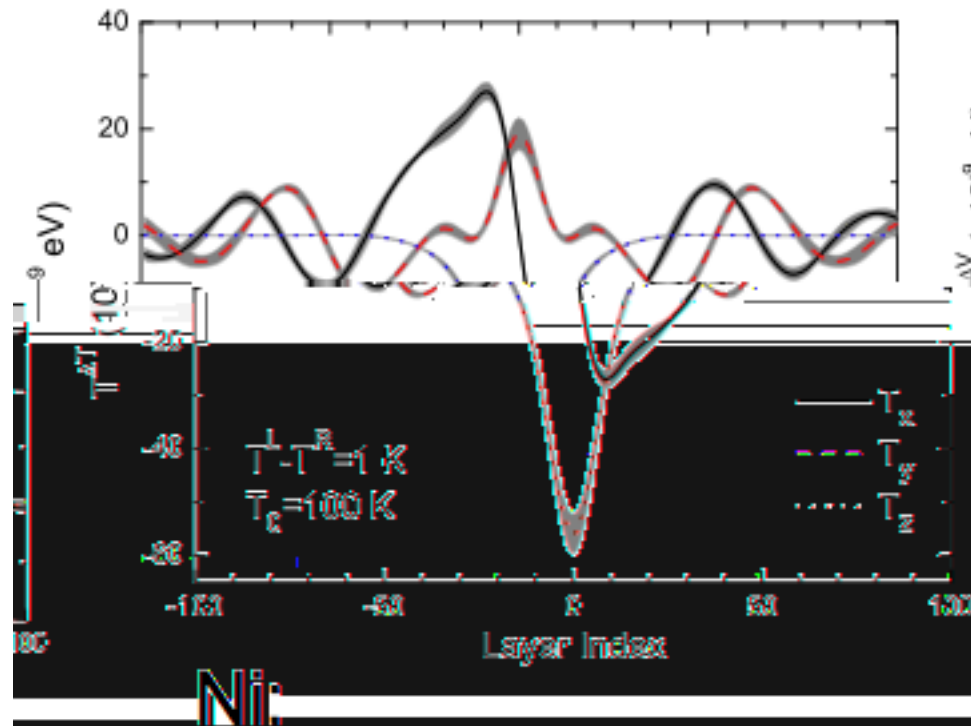
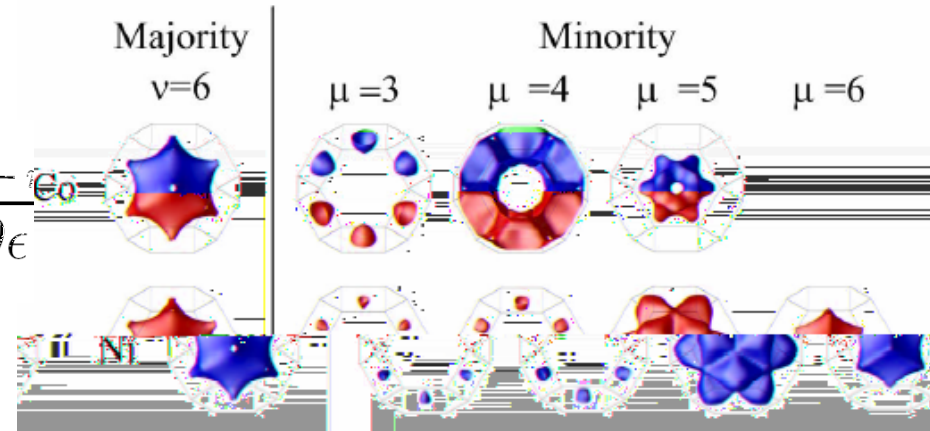
$$\hat{\mathcal{J}} \equiv \frac{1}{2} \left[\hat{\sigma} \otimes \hat{\mathbf{V}} + \hat{\mathbf{V}} \otimes \hat{\sigma} \right]$$

$$\mathbf{T}_{\mathbf{R}}(\mathbf{k}_{\parallel}, \epsilon) = \sum_{\mathbf{R}' \in I-1, I} \mathcal{J}_{\mathbf{R}', \mathbf{R}}(\mathbf{k}_{\parallel}, \epsilon) - \sum_{\mathbf{R}' \in I, I+1} \mathcal{J}_{\mathbf{R}, \mathbf{R}'}(\mathbf{k}_{\parallel}, \epsilon)$$



Bias- and temperature-STT

$$T_n = \left[\frac{\partial}{\partial \epsilon} \left(T_n e V_b + \frac{\pi^2 \hbar^2 T_n^2}{6} \frac{\partial \tilde{T}_n}{\partial \epsilon} \right) \right]_{\epsilon=\mu_0}$$

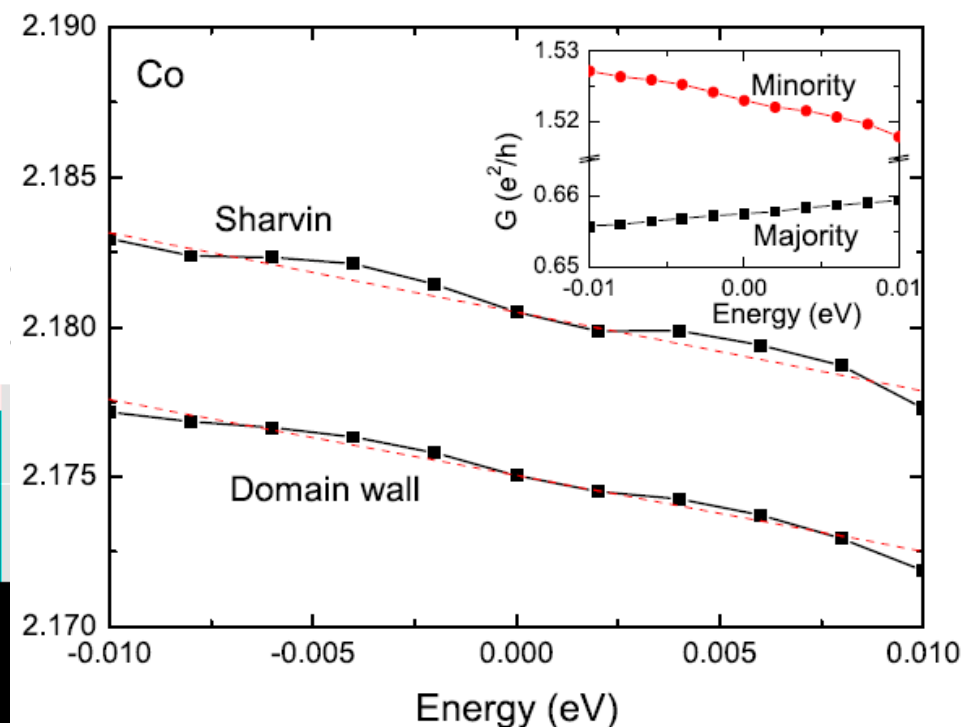
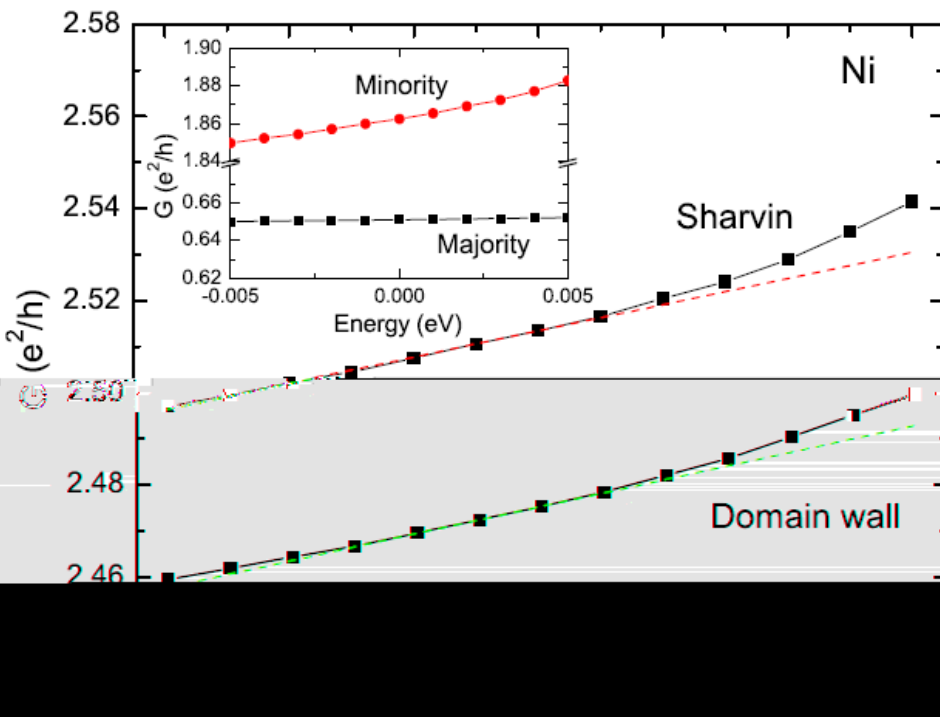


Peltier and Seebeck coefficients

	$G' (e/hV)$	$G (e^2/h)$	$\partial_\epsilon \ln G _{\epsilon_F} (eV^{-1})$	$S/T (nV/K^2)$	
Ni domain wall	2.94	2.48	1.19	-28.9	
Ni Sharvin	2.84	2.51	1.13	-27.5	
Polarized Sharvin	—	—	0.57	-13.9	I
Co domain wall	-0.253	2.175	-0.116	2.83	
Co Sharvin	-0.264	2.181	-0.121	2.95	
Polarized Sharvin	—	—	0.184	-4.50	I

$$P \equiv \frac{w_\uparrow G_\uparrow - w_\downarrow G_\downarrow}{w_\uparrow G_\uparrow + w_\downarrow G_\downarrow}$$

$$\bar{S} = w_\uparrow S_\uparrow + w_\downarrow S_\downarrow$$



Messages

Spin-dependent transport properties of interfaces govern many magnetoelectronic phenomena.

Agreement between interface-dominated transport properties calculated by first principles and the isotropy assumption with experimental values is (semi)-quantitative for itinerant systems like transition metals.

Mixing conductance and spin-torque can be calculated and measured accurately.

Computational Material Science

The End