

Newly Discovered FeAs-Superconductors: Opportunity and Challenge

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2008.5.16 Peking University

Outline

- Historical Review
 - Preliminary Experimental Results
 1. High T_c
 2. SDW at undoped state
 3. Multiband SC
 4. Unconventional SC
 - Existing Theories
 1. Band Structure calculations: LDA
 2. Proposed Pairing Symmetry
 - Our Minimal Model: two-band, d-wave pairing, SDW
 - Our Microscopic Model and Calculations: intra- and inter band SF fluctuations
 - Outlook
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□ Brief historical introduction

□ 1911: Onnes discovered superconductivity (Noble Prize)

□ 1933: Meissner effect (Meissner & Ochsenfeld)

□ ~~1934: A two-fluid model (London brothers)~~

□ 1950: Ginzburg-Landau theory (G-L)

1957: Type-I and type-II Superconductor (Noble Prize)

□ 1957: Microscopic theory of conventional superconductivity (BCS)
(Noble Prize)

□ 1962: Josephson effect (Noble Prize)

□ 1986: High-T_c superconductors LaBaCuO (T_c ~ 30K) (Bednorz & Müller) (Noble Prize)

□ 1987: Y₁Ba₂Cu₃O₇ (T_c ~ 90K, Wu & Chu)

□

Microscopic BCS Theory for Conventional Superconductivity



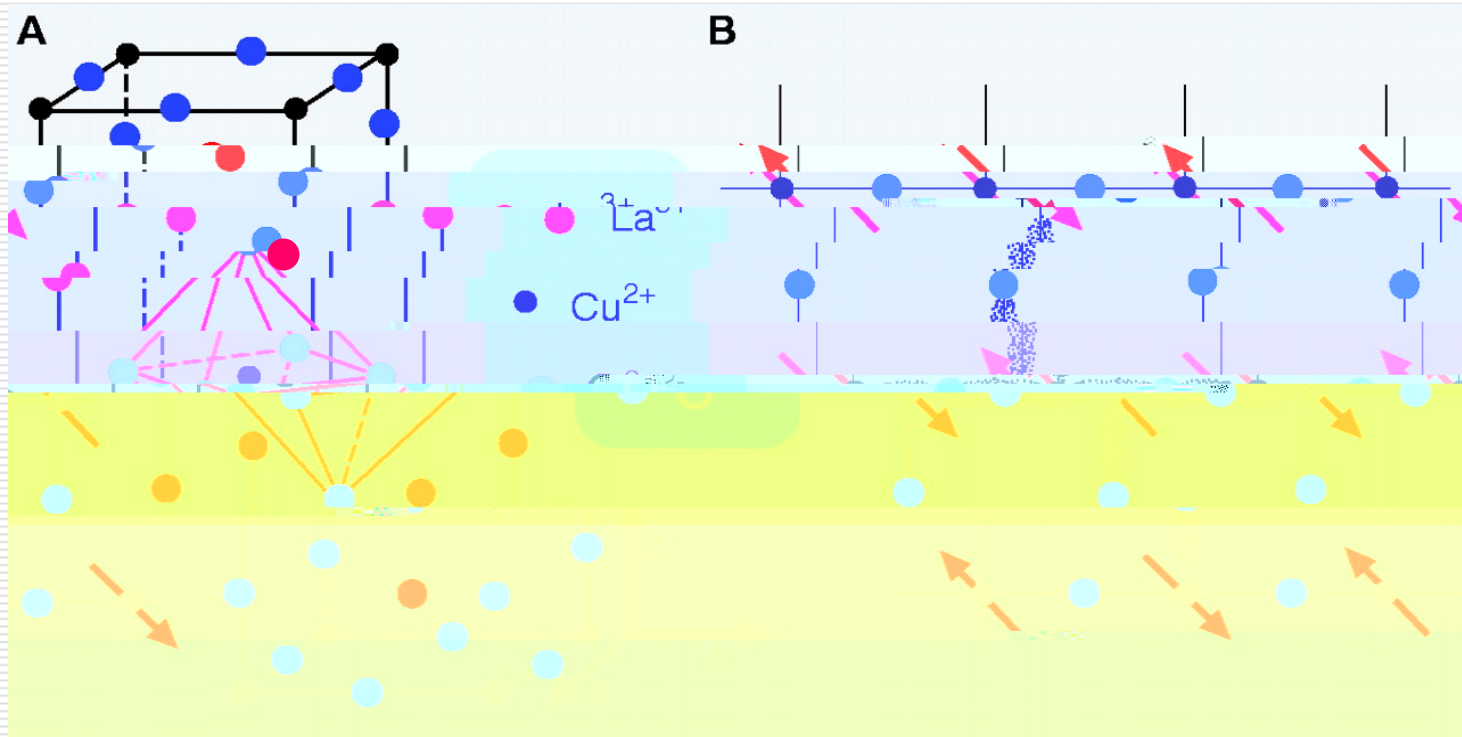
$$\begin{aligned} H = & \sum_{k, \sigma} (\varepsilon_k - \mu) C_{k\sigma}^\dagger C_{k\sigma} \\ & + \sum_{k, k'} V_{kk'} (C_{k\uparrow}^\dagger C_{-k\downarrow}^\dagger \langle C_{-k\downarrow} C_{k\uparrow} \rangle_k + h.c. \\ & - \langle C_{-k\downarrow} C_{k\uparrow} \rangle_k^* \langle C_{-k'\downarrow} C_{k'\uparrow} \rangle_{k'}) \end{aligned}$$

where

$\langle C_{-k\downarrow} C_{k\uparrow} \rangle_k$ is the Cooper pairing, whose order parameter

$$\Delta = - \sum_{k'} V_{kk'} \langle C_{-k'\downarrow} C_{k'\uparrow} \rangle_{k'}$$

High-Tc Copper-Oxides

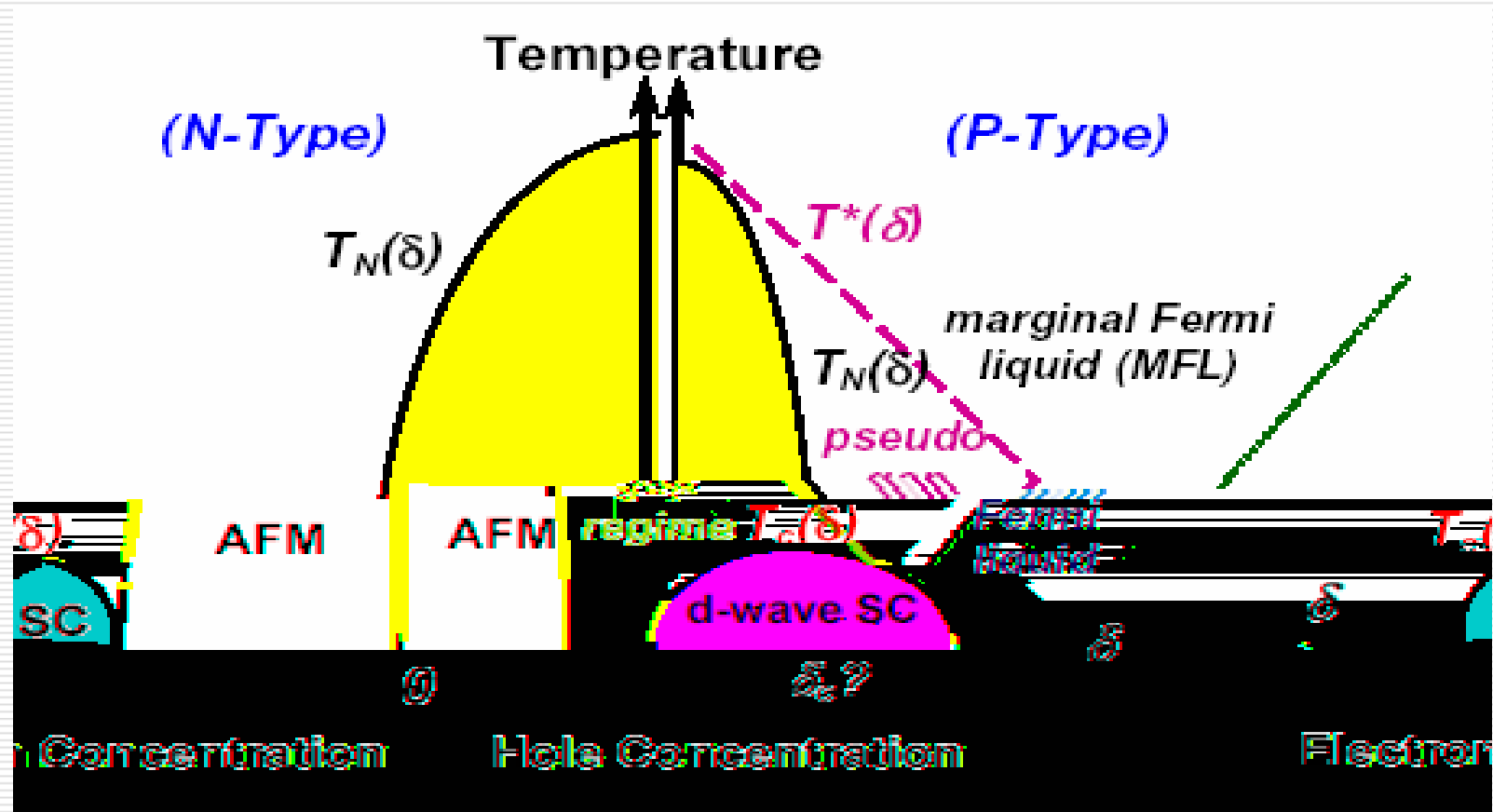


Crystal structure of La_2CuO_4 Schematic of CuO_2 plane

Main Understandings

- ❑ Doped Mott Insulators
 - ❑ Main Physics in CuO_2 Planes
 - Strong electronic correlation
 - AFM spin correlation
 - ❑ Superconducting state: rather normal; while normal state: abnormal;
 - ❑ An Acceptable Microscopic theory is still awaited
-

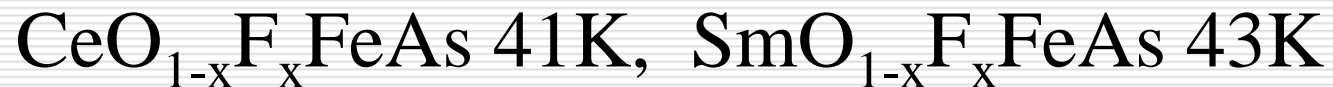
Schematic Phase Diagram



Fe-As SC: Experimental Results (I)

□ Higher T_c

Electron-doped Materials:



Hole-doped Materials:



Crystal Structure of LaOFeAsF

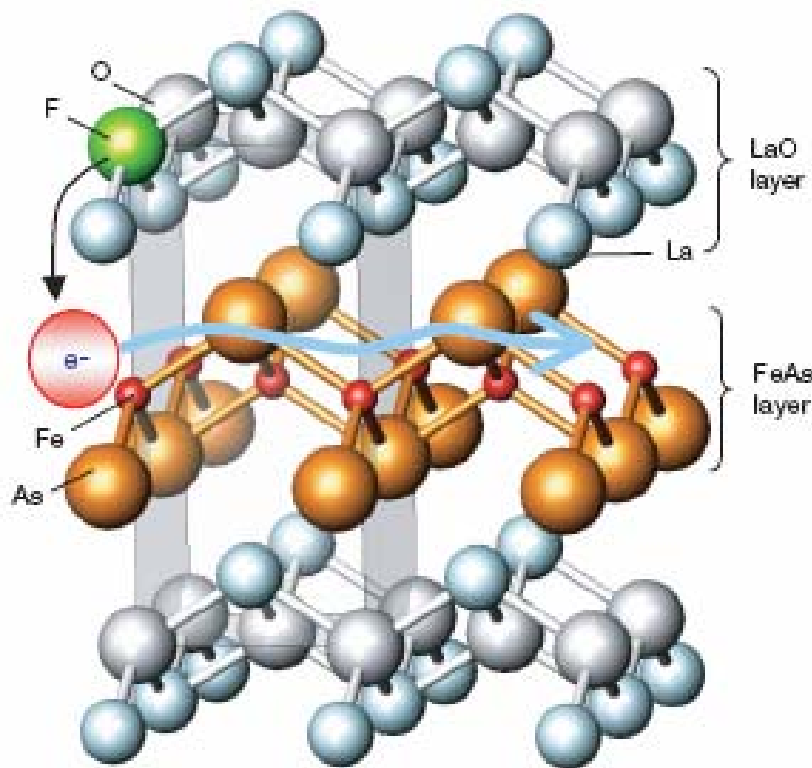
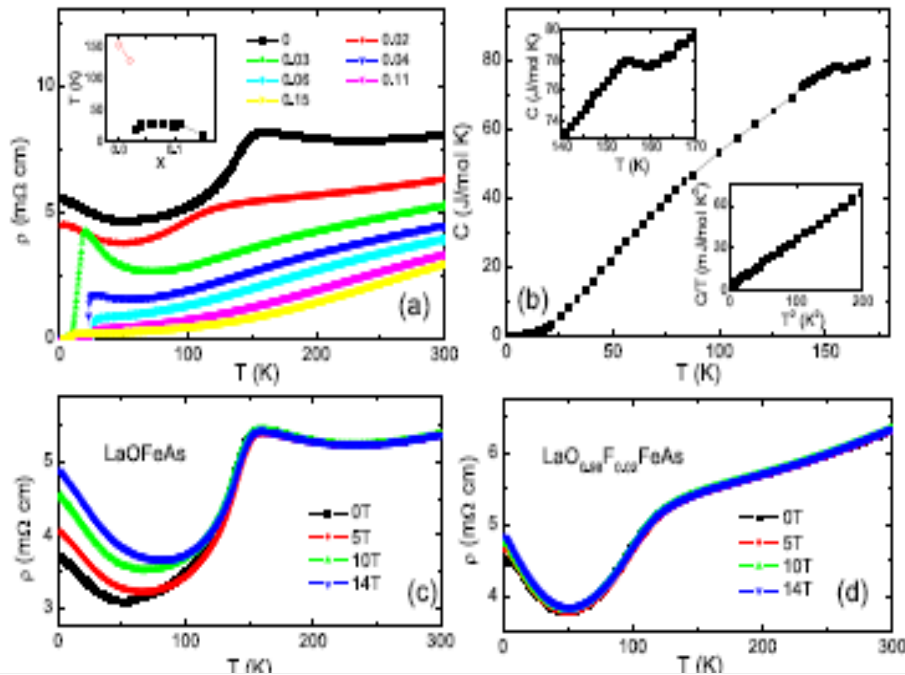


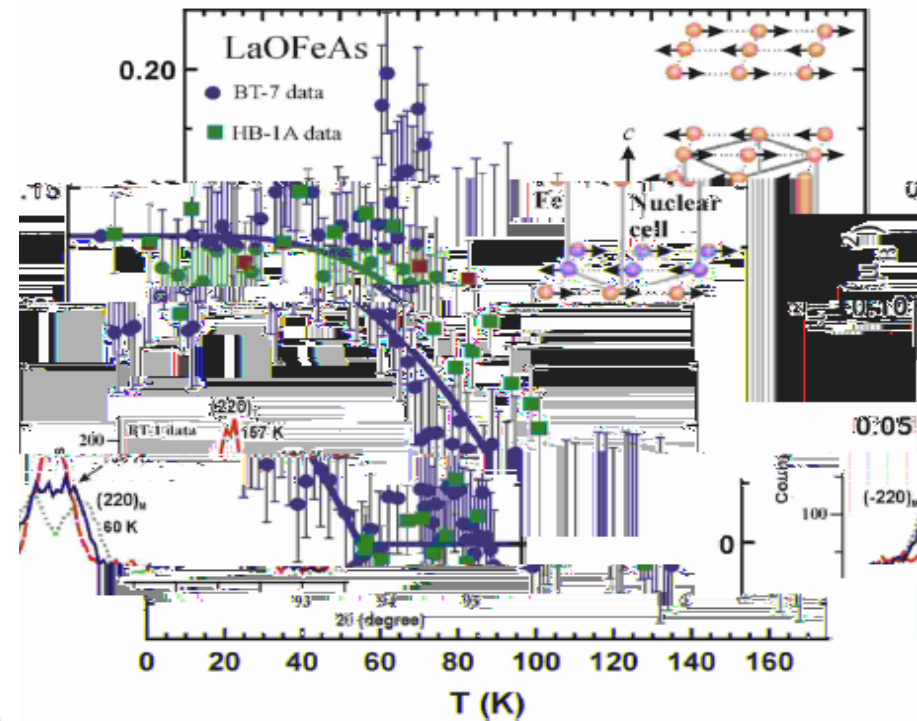
Figure 1 | Schem

Experimental Results (II)

□ SDW in the normal state



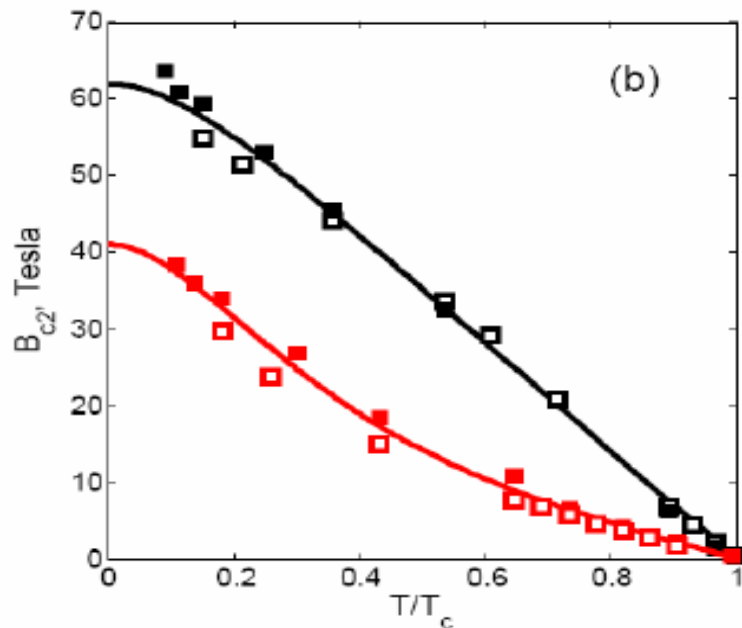
Reflective Optical Spectroscopy



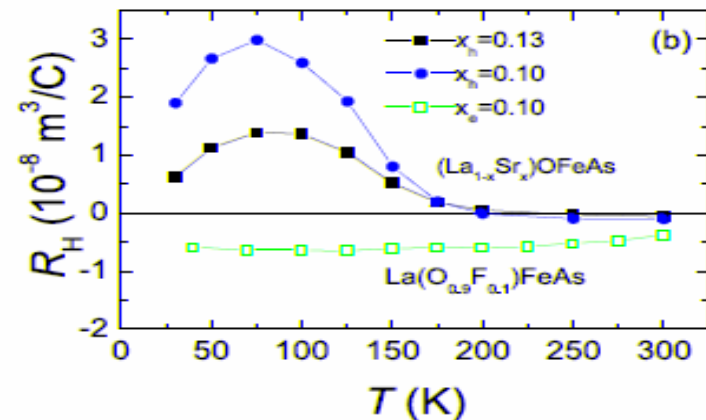
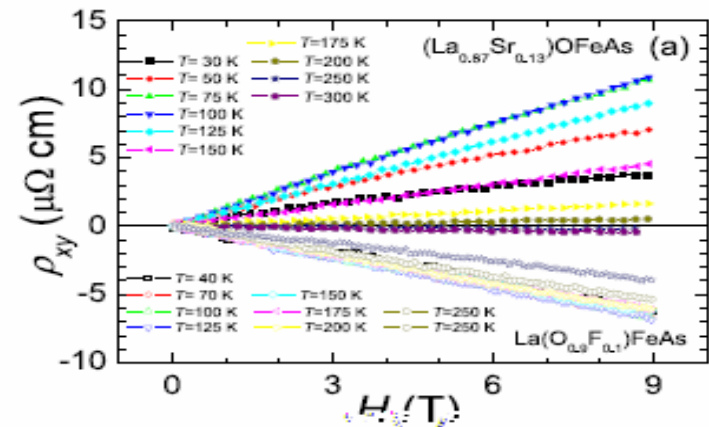
Neutron scattering data

Experimental Results (III)

□ Multiband Effect



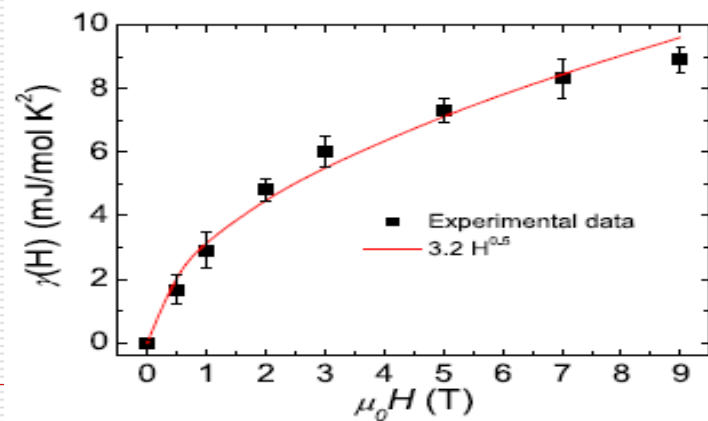
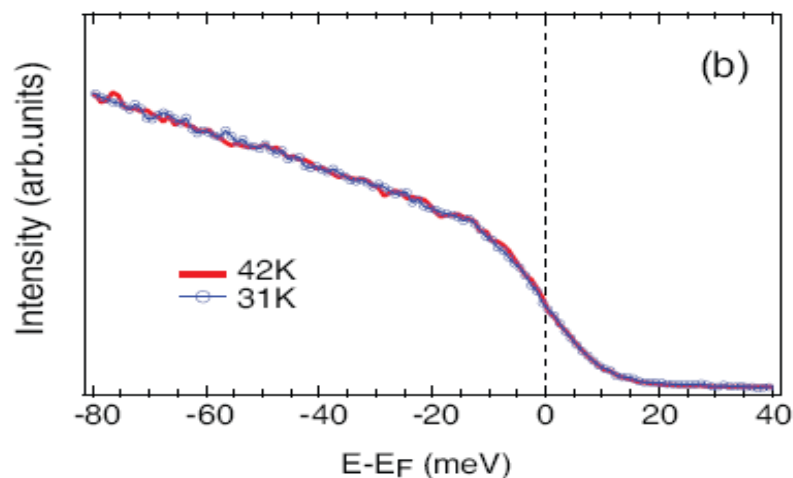
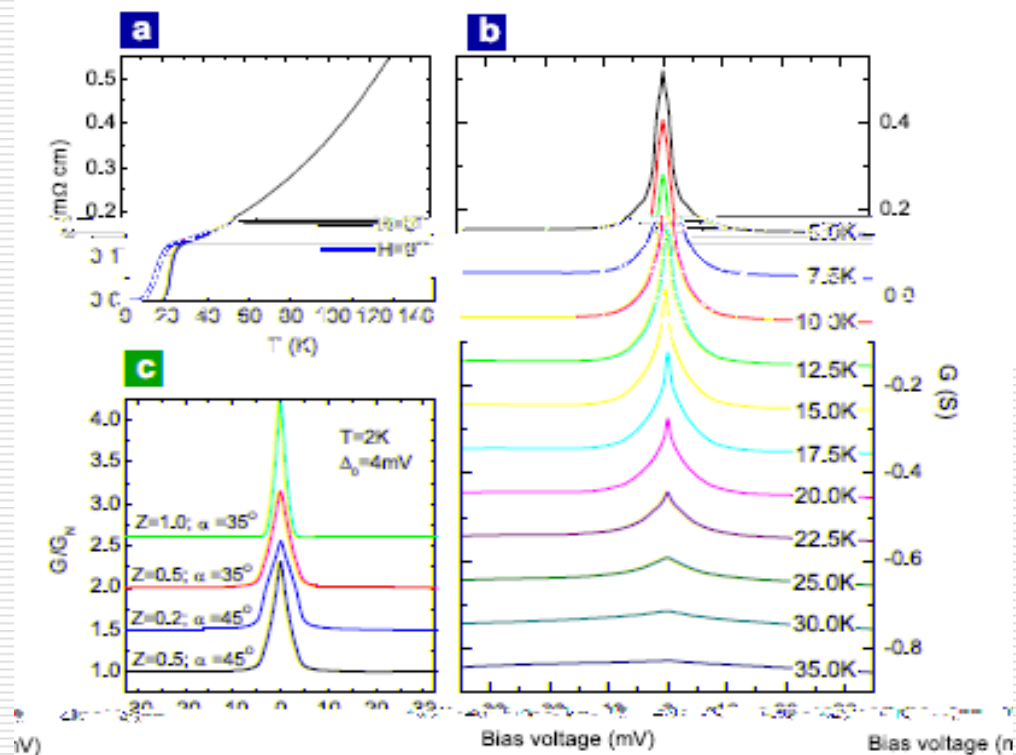
The lines corresponds to $B_{c2}(T)$ calculated from the two-gap theory.



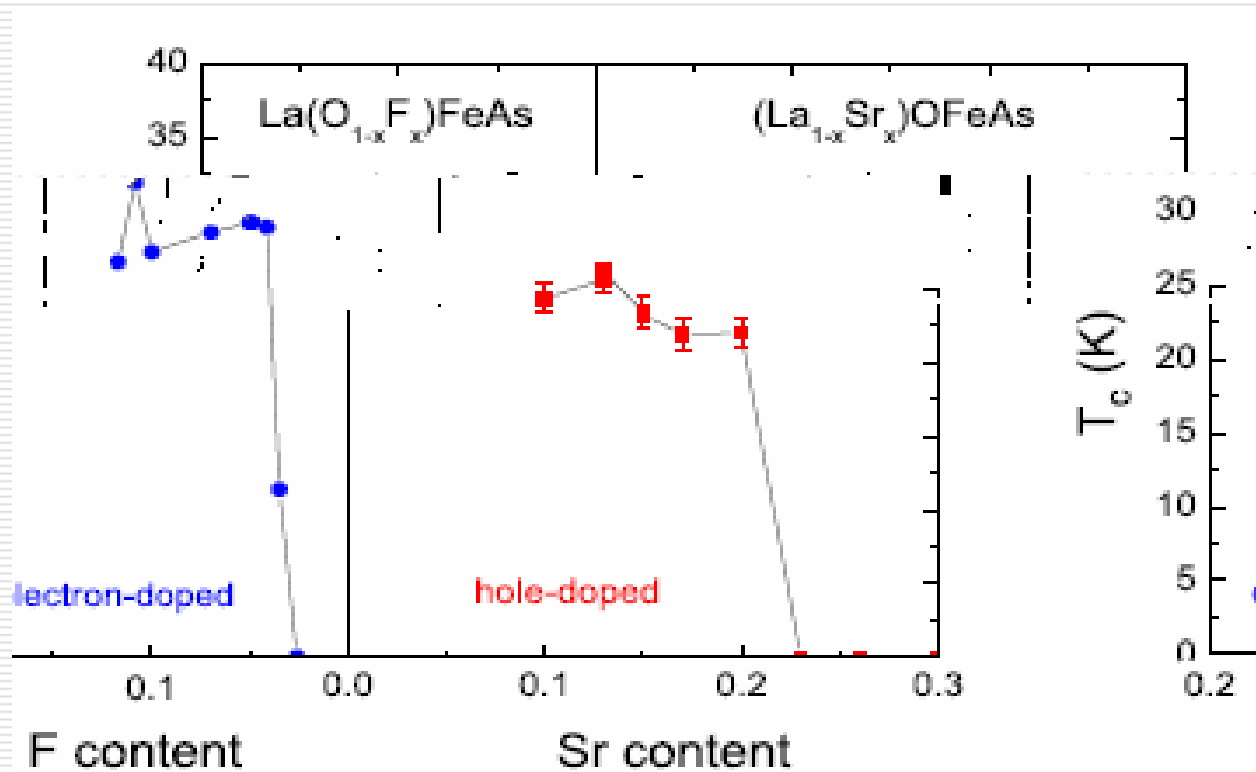
Temperature dependence of Hall resistivity was observed which may suggest a strong multiband effect in the electron-doped and hole-doped samples.

Experimental Results (IV)

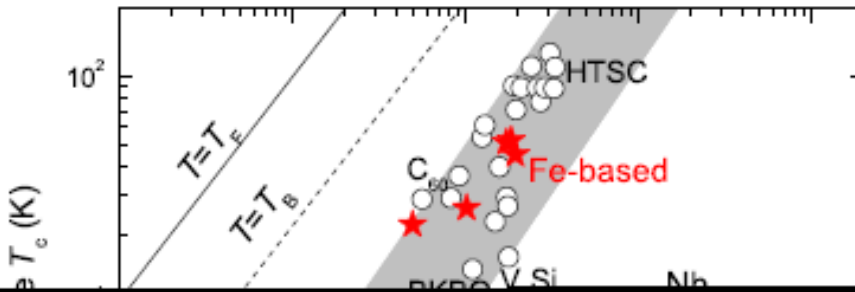
□ Unconventional SC



□ Symmetric Phase Diagram (Electron-doping vs hole-doping)



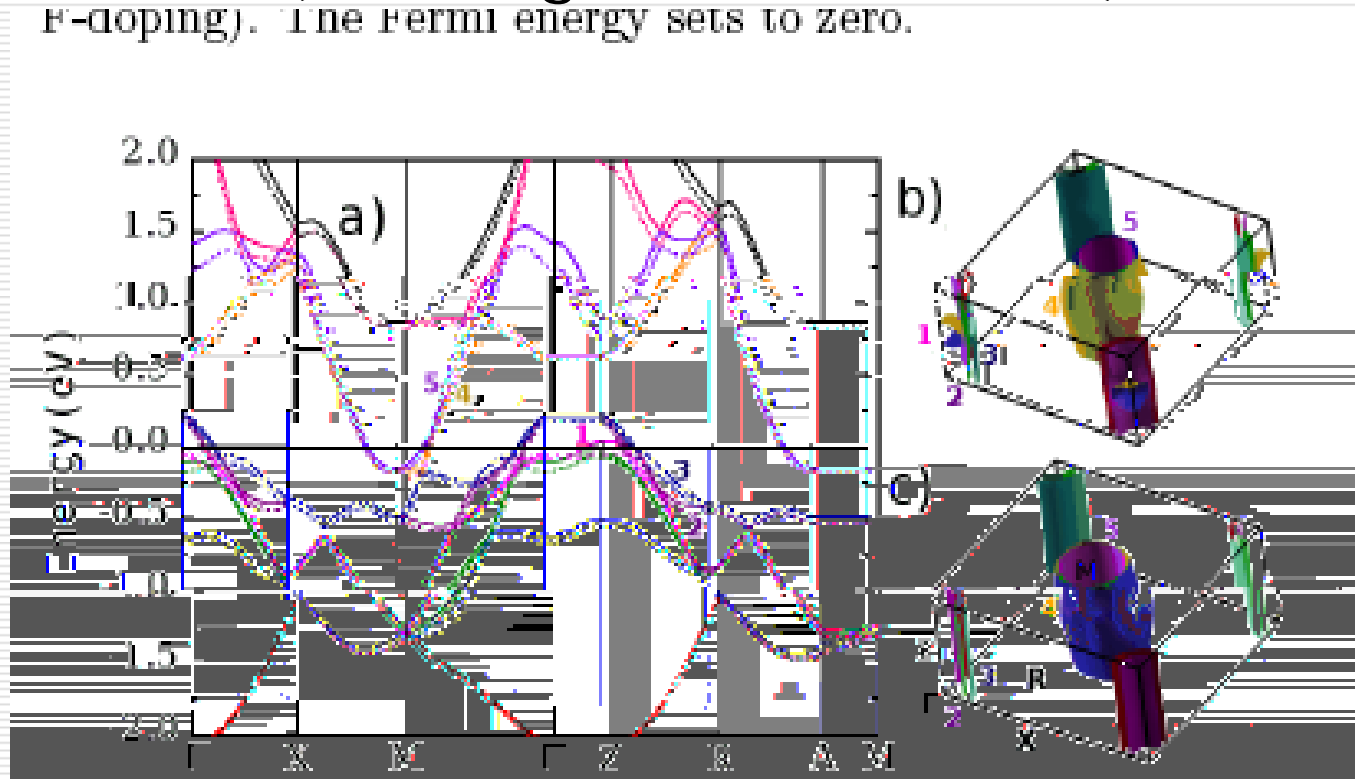
T_c vs T_F of unconventional superconductors (grey region)



Band Structure Calculations (LDA, DMFT)

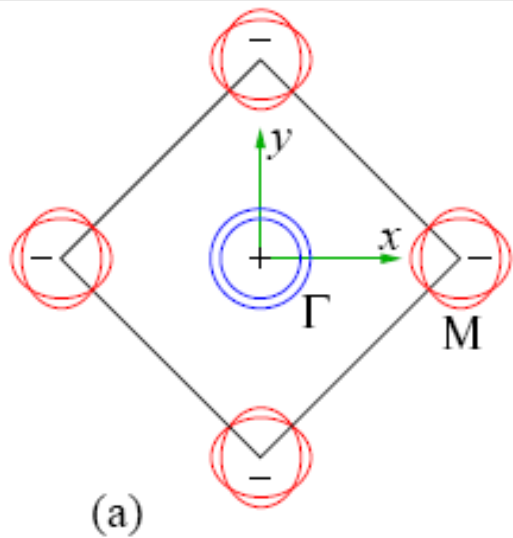
□ LDA (nonmagnetic structures)

F-doping). The Fermi energy sets to zero.



Proposed Pairing Symmetry

- Extended s-wave
- Spin-triplet p-wave
- Spin-triplet orbit-singlet s-wave



Extended s-wave:
FS pockets located around Γ and around M , SC order parameters on the two sets of the FSs have the opposite signs.

Our Work and Main Findings

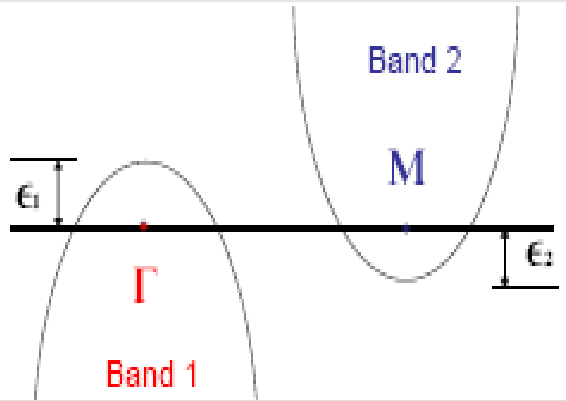
- (1) Han, Chen, Wang, EPL 82, 37007 (2008); arXiv: 0803.4346
(2) Yao, Li, Wang, arXiv: 0804.4166 (2008)

- The normal state has an SDW order ($Q=(\pi, \pi)$), while upon the charge carrier doping the SDW order drops rapidly and the SC order emerges
 - due to the two-band (electron and hole) SC nature of the material, T_c as a function of the effective doping density shows a nearly symmetric electron-hole doping dependence
 - two-band superconducting state exhibits a d-wave symmetry (SDW fluctuations)
 - Fluctuation-exchange approach on a microscopic two-band model yields quantitative results, supporting strongly our simple effective two-band model
-

Our Minimal Model

- 2-band BCS d-wave pairing + intraband Hubbard interaction

$$\begin{aligned}
 H = & \sum_{k\sigma} \xi_{1k} c_{k\sigma}^+ c_{k\sigma} + \sum_{k\sigma} \xi_{2k} d_{k\sigma}^+ d_{k\sigma} + U_{eff} \sum_{i\sigma} n_{1i\sigma} n_{2i\sigma} \\
 & + \sum_{kk'} V_{kk'}^{11} c_{k\uparrow}^+ c_{-k\downarrow}^+ c_{-k\uparrow} c_{k\downarrow} + \sum_{kk'} V_{kk'}^{22} d_{k\uparrow}^+ d_{-k\downarrow}^+ d_{-k\uparrow} d_{k\downarrow} \\
 & + \sum_{kk'} (V_{kk'}^{12} c_{k\uparrow}^+ c_{-k\downarrow}^+ d_{-k\uparrow} d_{k\downarrow} + h.c.)
 \end{aligned}$$



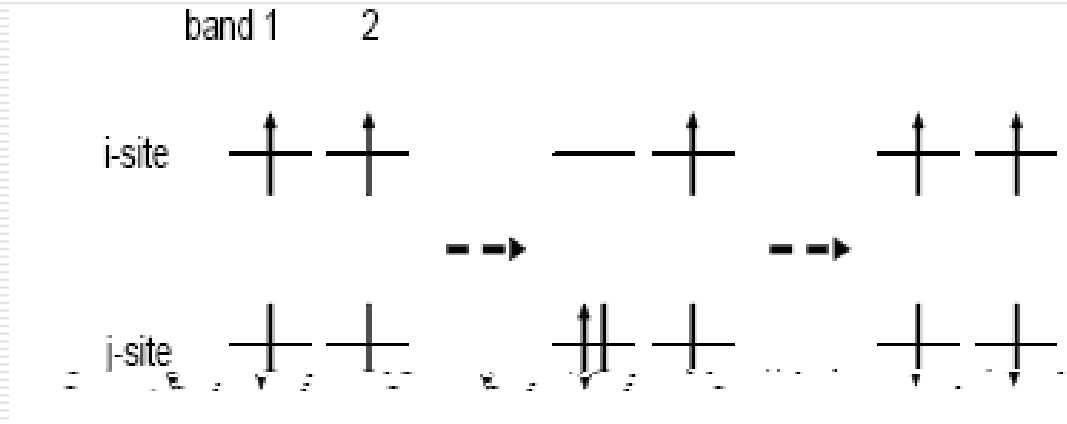
$$DOS : \rho_{1,2} = 1 / (4 \pi t_{1,2}), W_{h,e} = 1 / \rho_{1,2}$$

$$n_h^0 = 2 \rho_1 \epsilon_0^{(1)}, n_e^0 = 2 \rho_2 \epsilon_0^{(2)}$$

Double-degenerated with each for one Fe-sublattice

Origin of the SC Pairing

$$H_i = U \sum_{l\sigma} n_{il\sigma} n_{il\bar{\sigma}} + U' \sum_{\sigma\sigma'} n_{i1\sigma} n_{i2\sigma'} + J_H \vec{\sigma}_{i1} \cdot \vec{\sigma}_{i2}$$

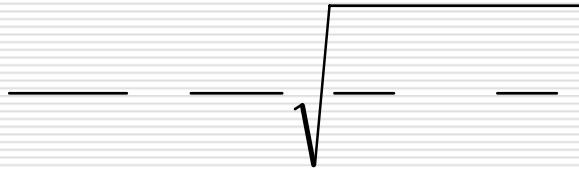


➡ Intraband AF fluctuation ➡ Intraband d-wave SC

Origin of SDW Order

- Condensate of bound electron-hole pairs “excitons”

$$1 = U_{eff} \chi_0^{12}(Q), \chi_0^{12}(Q) = - \sum_k \frac{f(\xi_{1k}) - f(\xi_{2k+Q})}{\xi_{1k} - \xi_{2k+Q}}$$



SDW State

- Below T_{SDW} , the SDW ordering emerges, SDW order parameter is defined as

$$\Delta_{SDW} = U_{eff} \sum_k \langle c_{k\uparrow} d_{k+Q\downarrow}^+ \rangle$$

$$1 = -U_{eff} \sum_k \frac{f(\eta_{2k} + \Omega_k) - f(\eta_{2k} - \Omega_k)}{2\Omega_k},$$

$$\Omega_k = \sqrt{\eta_{1k}^2 + \Delta_{SDW}^2}, \eta_{1k} = (\xi_{1k} - \xi_{2k+Q})/2, \eta_{2k} = (\xi_{1k} + \xi_{2k+Q})/2$$

SDW State

- Counterpart of Cooper electron-electron pair

$$2\Delta_{SDW} / T_{SDW} \approx 3.53 (BCS.result)$$

According to optical conductivity spectra,

$$2\Delta_{SDW}(8K) \approx 350 cm^{-1} = 504K, T_{SDW} \approx 150K$$

$$so.. 2\Delta_{SDW}(8K) / T_{SDW} \approx 3.4$$

The AF moment/Fe is estimated ~ 0.31 , (exp. ~ 0.36) ;

T_{SDW} decreases with the shrinkage of lattice.

SC State

- Two band (hole and electron) SC

$$\Delta_h = \sum_k \gamma_k (J_{hh} \langle c_{-k\downarrow} c_{k\uparrow} \rangle + J_{he} \langle d_{-k\downarrow} d_{k\uparrow} \rangle),$$

$$\Delta_e = \sum_k \gamma_k (J_{eh} \langle d_{-k\downarrow} d_{k\uparrow} \rangle + J_{ee} \langle c_{-k\downarrow} c_{k\uparrow} \rangle),$$

At T_c , we have linearized gap equation,

$$\begin{pmatrix} J_{hh}K_1 & J_{he}K_2 \\ J_{eh}K_1 & J_{ee}K_2 \end{pmatrix} \begin{pmatrix} \Delta_h \\ \Delta_e \end{pmatrix} = \begin{pmatrix} \Delta_h \\ \Delta_e \end{pmatrix}, \quad K_{1,2} = \sum_k \frac{\tanh(\xi_{1,2k} / 2T_c)}{2\xi_{1,2k}} \gamma_k^2$$

Non-zero solution,
for T_c

$$\det \begin{pmatrix} J_{hh}K_1 - 1 & J_{he}K_2 \\ J_{eh}K_1 & J_{ee}K_2 - 1 \end{pmatrix} = 0$$

SC State

□ General case: $J_{ee}, J_{hh} > 0, J_{ee}J_{hh} \mp J_{eh}J_{he} > 0$.

$$\check{J}_{hh} = J_{hh}/W_h, \check{J}_{ee} = J_{ee}/W_e, \check{J}_{eh}^2 = (J_{eh}J_{he})/W_eW_h, \check{J}\check{J} = \check{J}_{eh}\check{J}_{he} - \check{J}_{ee}\check{J}_{hh}$$

We obtain,

$$\frac{T_c}{\sqrt{W_eW_h}} = \frac{e^\gamma}{\pi} [n_e n_h (2 - n_e)(2 - n_h)]^{1/4} e^{-\frac{1}{\lambda_{eff}}}, \text{ where}$$

$$\frac{1}{\lambda_{eff}} = \left\{ \left[\left(\frac{1}{4} \check{J}\check{J} \ln \frac{n_e(2-n_e)W_e^2}{n_h(2-n_h)W_h^2} + \frac{\check{J}_{hh} - \check{J}_{ee}}{2} \right)^2 + \check{J}_{eh}\check{J}_{he} \right]^{1/2} - \frac{1}{2}(\check{J}_{hh} + \check{J}_{ee}) \right\} / \check{J}\check{J}$$

SC State

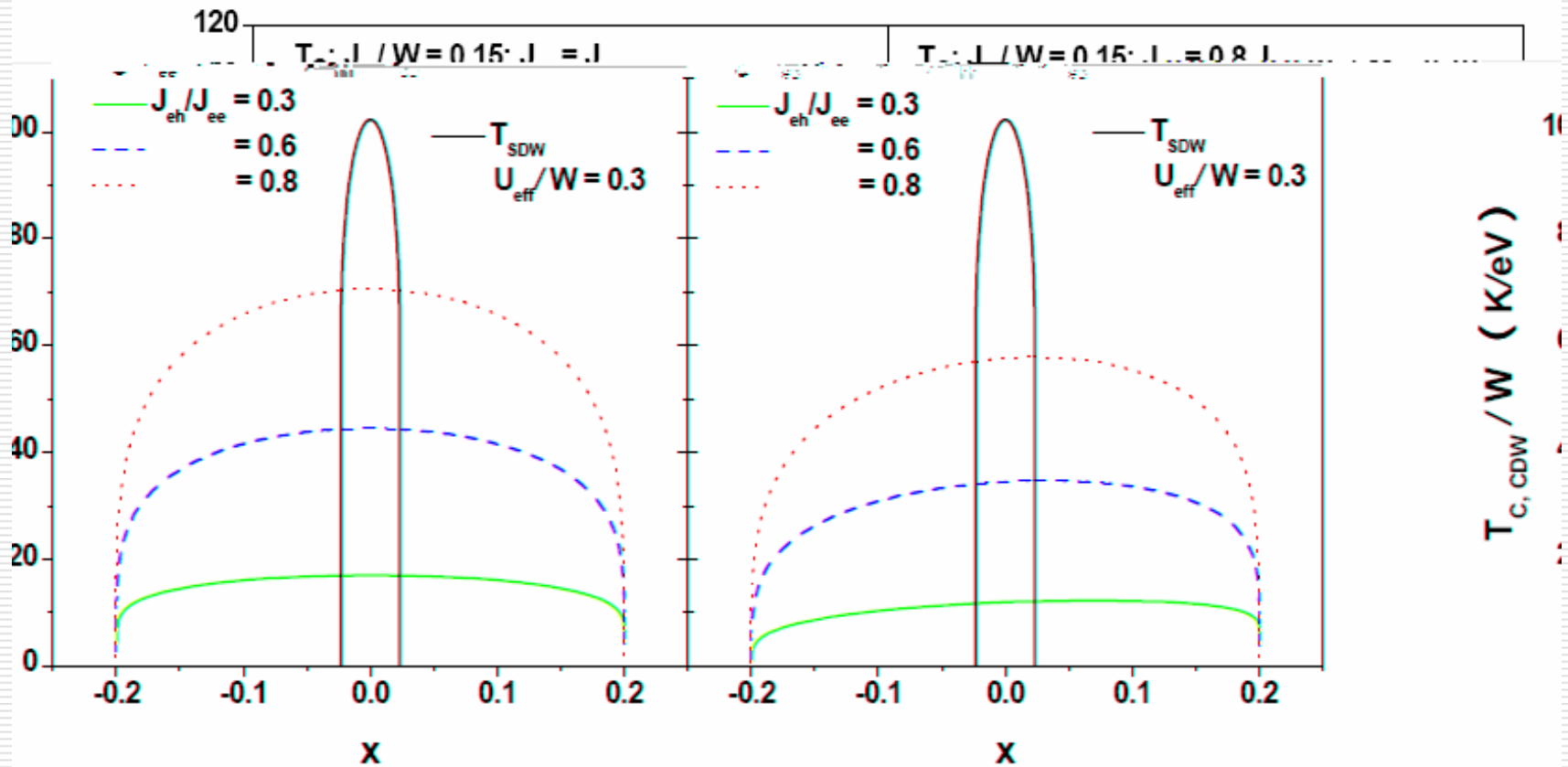
□ Special case: $J_{eh}J_{he}=J_{ee}J_{hh}$.

$$\frac{T_c}{\sqrt{W_e W_h}} = \frac{e^\gamma}{\pi} \left(\sqrt{\frac{W_e}{W_h}} \right)^{\frac{\check{J}_{ee}-\check{J}_{hh}}{\check{J}_{ee}+\check{J}_{hh}}} [\sqrt{n_e(2-n_e)}]^{\frac{\check{J}_{ee}}{\check{J}_{ee}+\check{J}_{hh}}} [\sqrt{n_h(2-n_h)}]^{\frac{\check{J}_{hh}}{\check{J}_{ee}+\check{J}_{hh}}} e^{-\frac{1}{\check{J}_{ee}+\check{J}_{hh}}}$$

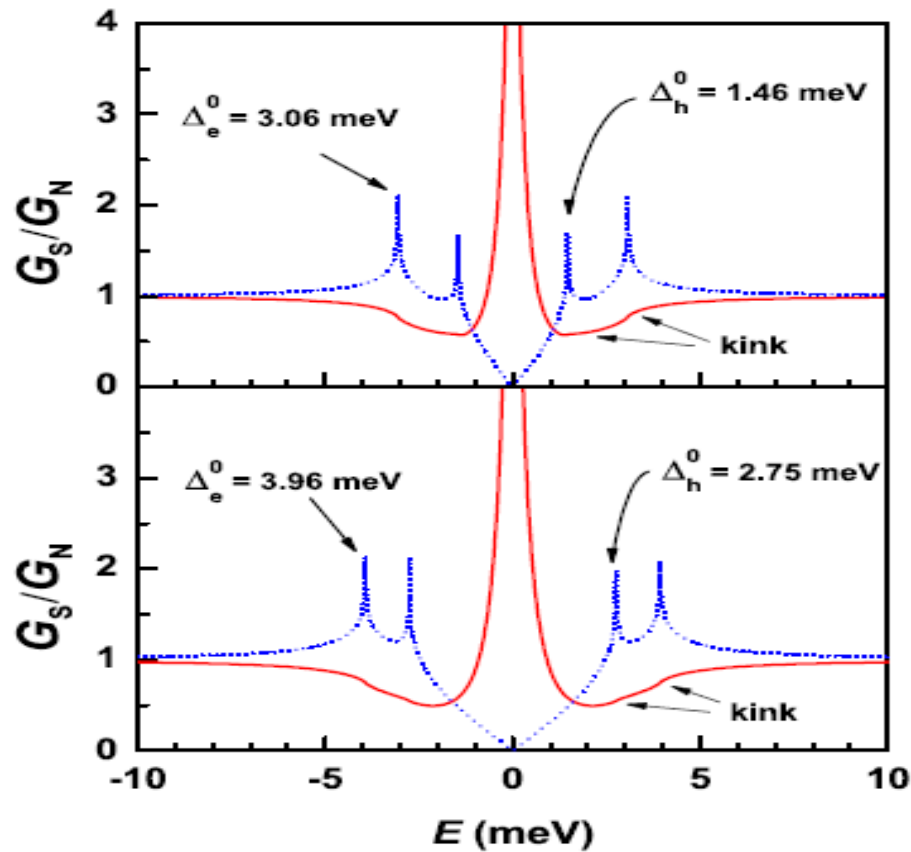
We choose the parameters as,

$$W_e = W_h = W, U_{eff} / W = 0.3, J_{eh} / W = 0.15, \varepsilon_0^{1,2} = 0.05W$$

Phase Diagram



Zero-bias Coherent Peak



Nodal d-wave pairing
(two gaps behavior)

Useful Relations

$$\frac{|-\ln(|\Delta_h^0|/T_c) + C_0 - C_{T_c}|}{|-\ln(|\Delta_e^0|/T_c) + C_0 - C_{T_c}|} \times |r_0 r_c| = \frac{W_h}{W_e},$$

where $r_{0,c} = r(0), r(T_c)$ are respectively the above introduced gap ratio at zero and transition temperatures.

$$\frac{\ln |r_0|}{[1 + (W_h/W_e)|r_0 r_c|^{-1}](|r_c| - |r_0|)} = \frac{|J_{eh}|/W_h}{\tilde{J}_{eh}^2 - \tilde{J}_{ee}\tilde{J}_{hh}}.$$

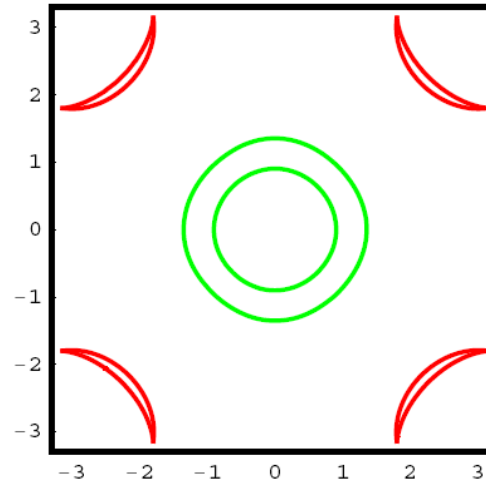
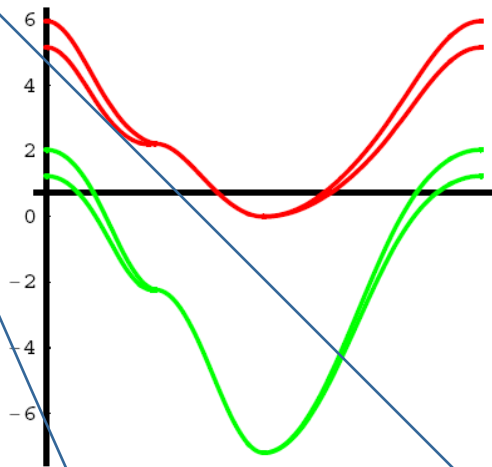
II. FLEX Results

□ Microscopic Model Hamiltonian

$$H = H_0 + H_{int}$$

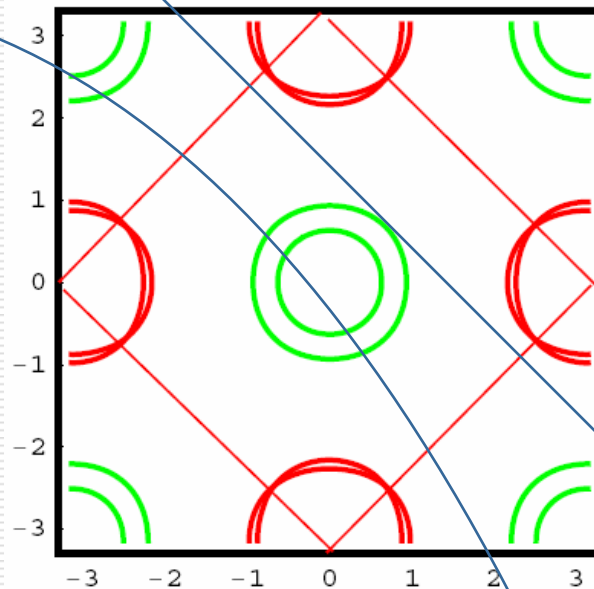
The interacting term H_{int} consists of the effective intraband Coulomb interaction [27], $(U/2) \sum_{i,l,\sigma \neq \sigma'} c_{il\sigma}^\dagger c_{il\sigma'}^\dagger c_{il\sigma'} c_{il\sigma}$, the effective interband Coulomb interaction $(U'/2) \sum_{i,l \neq l',\sigma,\sigma'} c_{il\sigma}^\dagger c_{il'\sigma'}^\dagger c_{il'\sigma'} c_{il\sigma}$, the Hund's coupling $J \sum_{i,l \neq l',\sigma\sigma'} c_{il\sigma}^\dagger c_{il'\sigma'}^\dagger c_{il\sigma} c_{il'\sigma'}$, and the interband pair-hopping term $J' \sum_{i,l \neq l',\sigma\sigma'} c_{il\sigma}^\dagger c_{il'\sigma'}^\dagger c_{il'\sigma'} c_{il\sigma}$, where the i -site is defined on the reduced lattice (one per cell).

Two-band structure in the reduced (original) BZ



Γ

X



Fermi pockets in the
extended BZ

Spin susceptibility

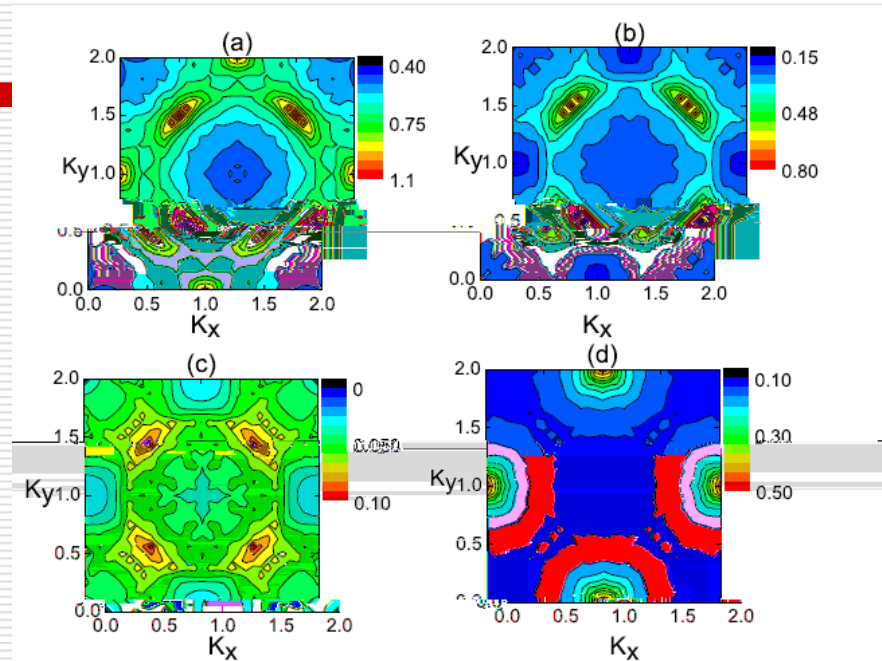


FIG. 2: (Color online) The q -dependence of the static spin susceptibility calculated with $U = 6.5$, $U' = 3.5$, $J = J' = 1$ at temperature $T = 0.01$. (a) The physical spin susceptibility (see text). (b)-(c) The components of the spin susceptibility, χ_{11}^s , χ_{22}^s and χ_{12}^s , respectively.

Superconducting pairing

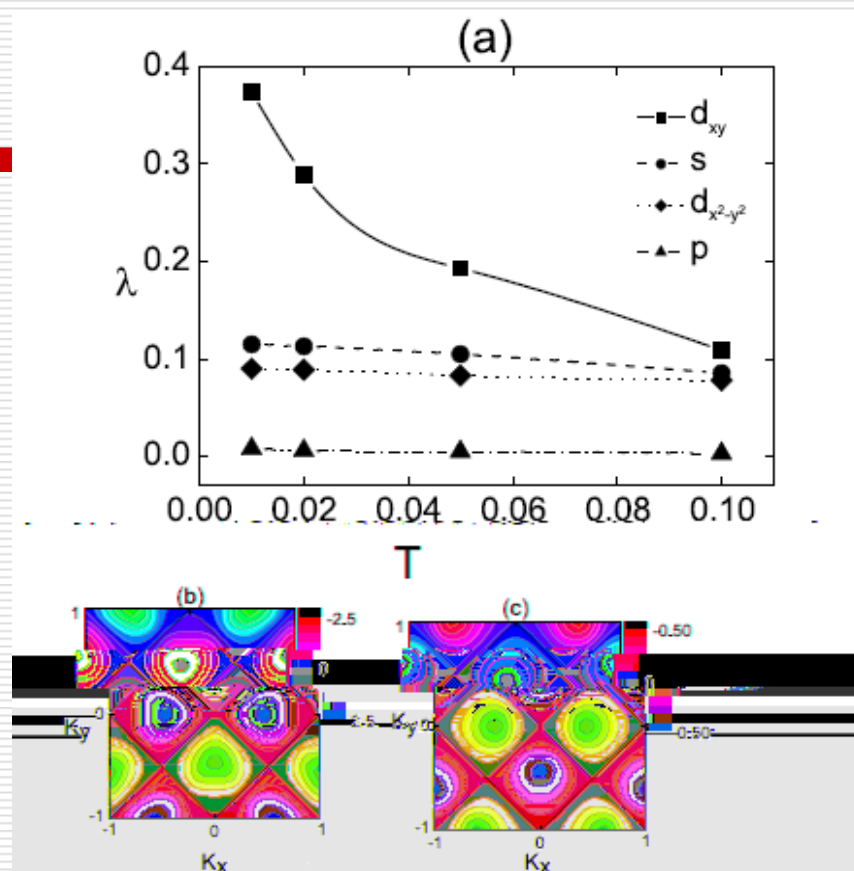


FIG. 3: (Color online) (a) Temperature dependence of the maximum eigenvalues for $U = 6.5, U' = 3.5, J = J' = 1.0$. (b) and (c): Momentum dependence of the gap functions $\Delta_{11,22}(k)$ corresponding to the largest eigenvalue at temperature $T = 0.01$.

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Outlook

1. Origin of Fe-As Superconductivity:
electron-electron interaction? If yes, intraband or interband SF fluctuations? Or both? Or doped Mott physics?
 2. Pairing symmetry: s-, d-, or p- wave ? To be determined by experiments on **single crystals(?)**
 3. Profound understandings on the above two key points may provide some clue to resolve a long standing issue of copper oxide SC mechanism.
 4. Even higher T_c above 77K?
 5. Novel phenomena and physics?
 6. Applications?
-

Superconductors *redux*

Yet another surprise has been uncovered in the complex oxides.

Thank you!
