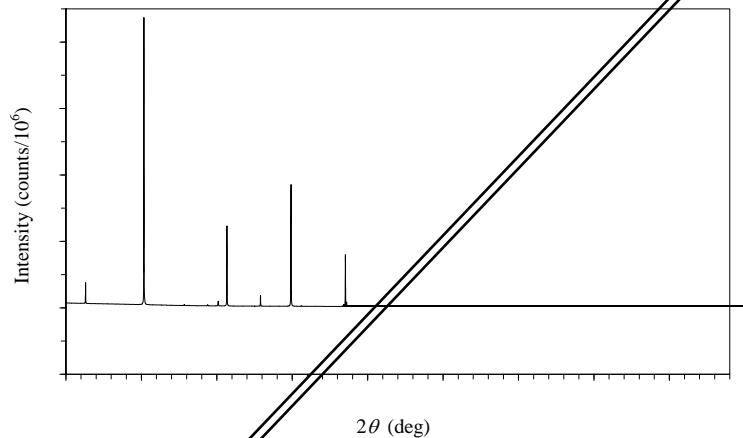
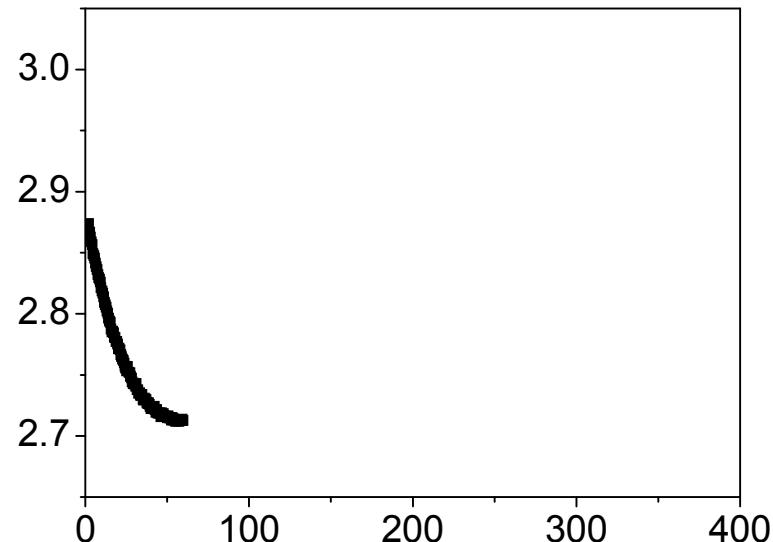


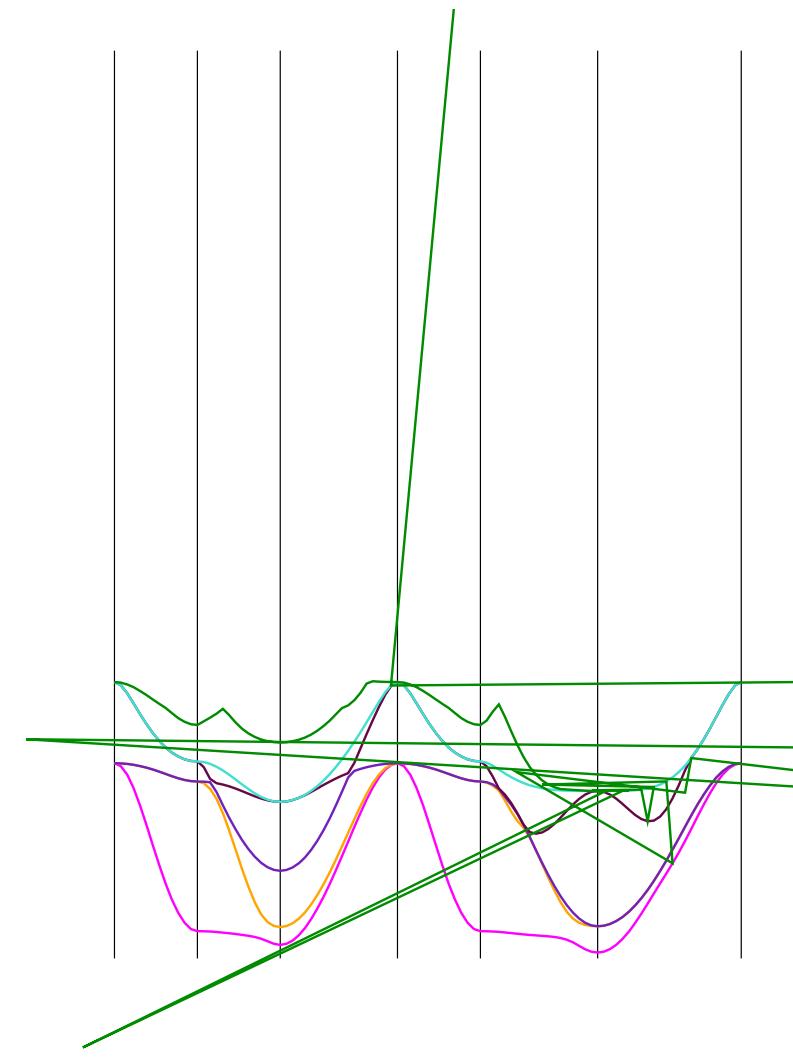
! "#\$%&' \$() *+, -\$. ' \$) %&/ *+, 0) %1 /) 1%\$,



Observed (crosses), calculated (solid line), and difference synchrotron X-ray powder diffraction patterns of EuOsO_3 at 300 K. Bragg reflections are indicated by tick marks. The lower tick marks are given for reflections from the Os impurity (2.9 weight %).

! " # \$ % & ' () * + , * - + . - \$ /) - 0 * - + 1)
2 - ' \$ 3 + - 2 - 4 5 \$)

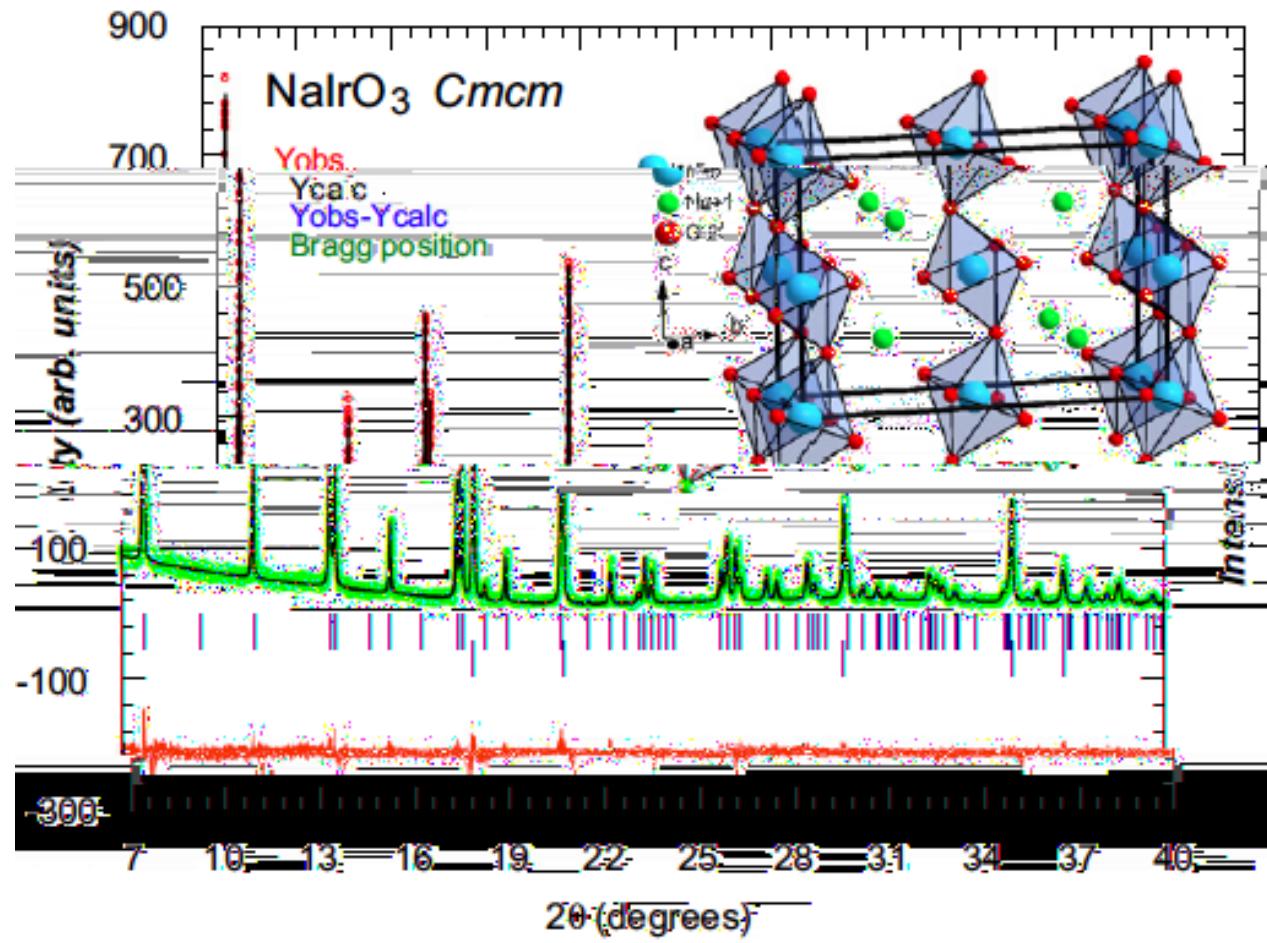




First-principles calculations: within GGA SOC U (U . eV) Ferromagnetic state

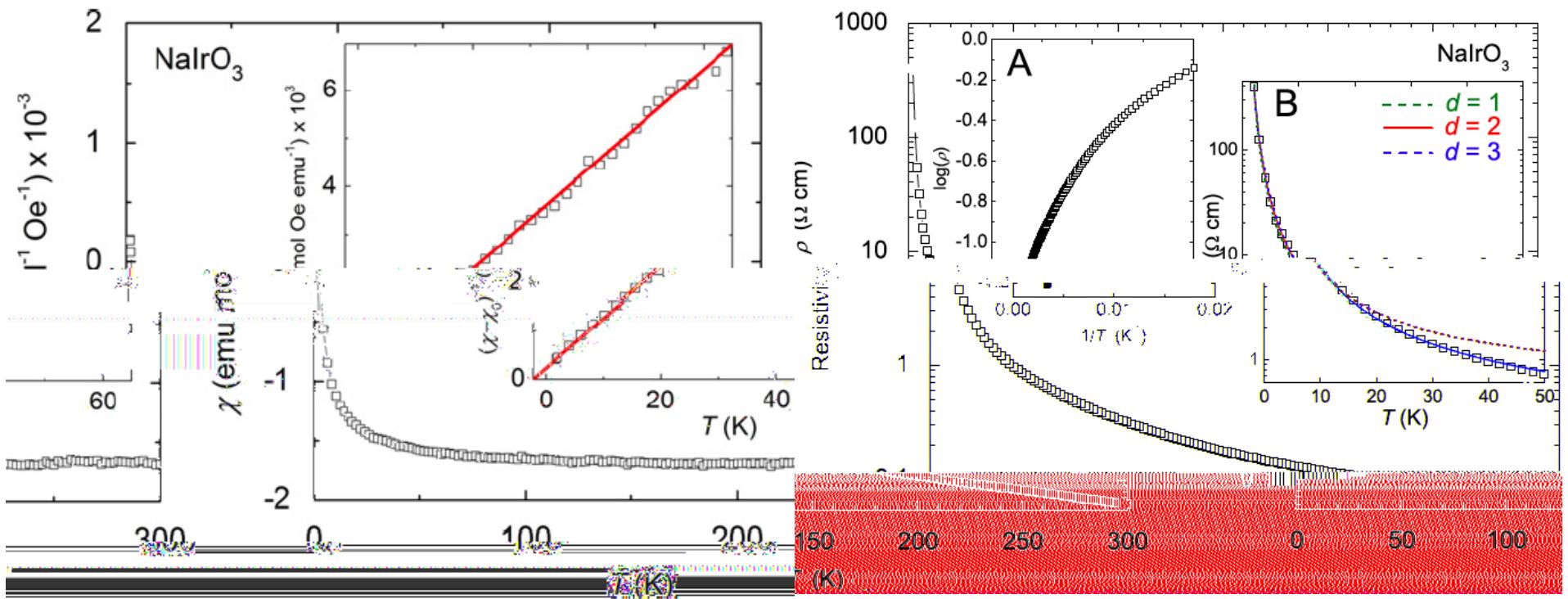


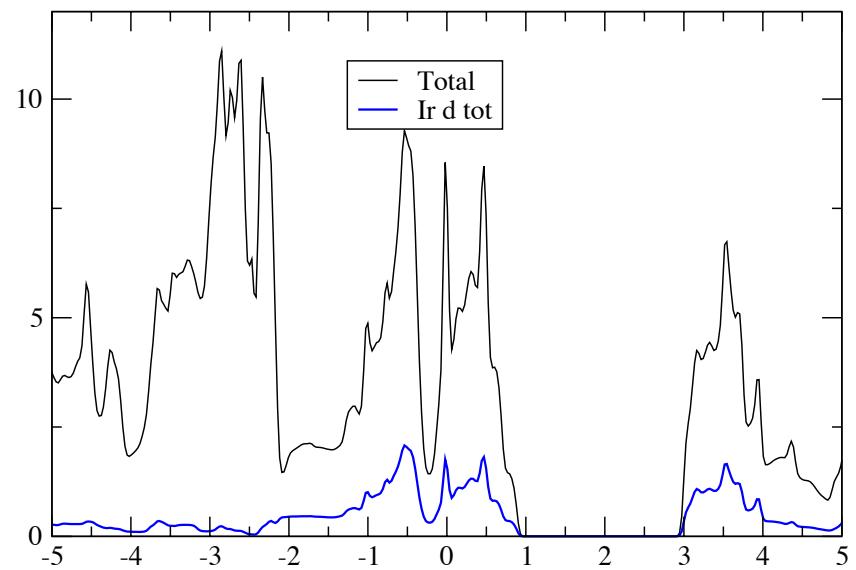
! "#\$%& \$()^*+,-\$. ' \$)%&/^*+,0)%1/)1%\$,

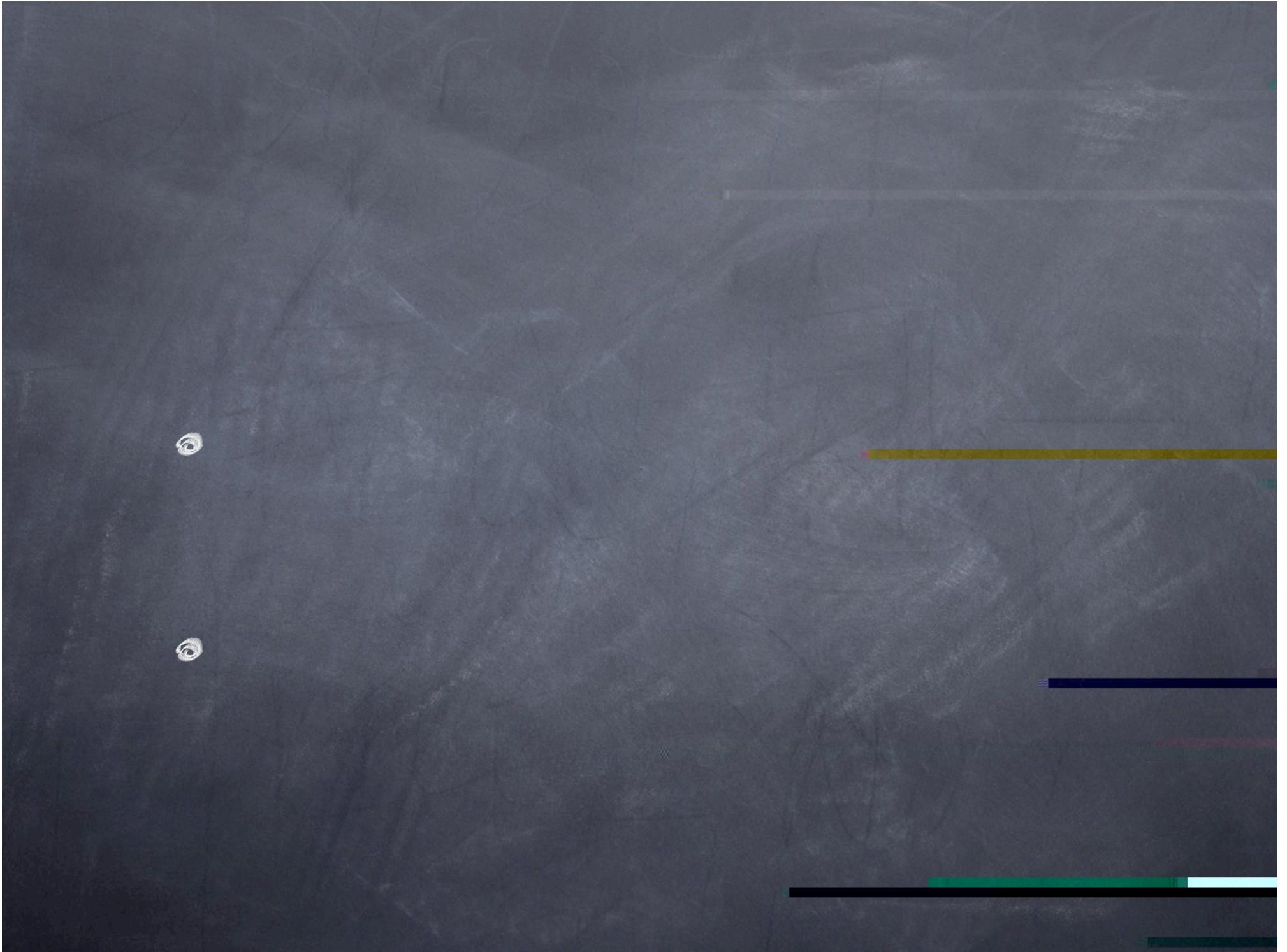


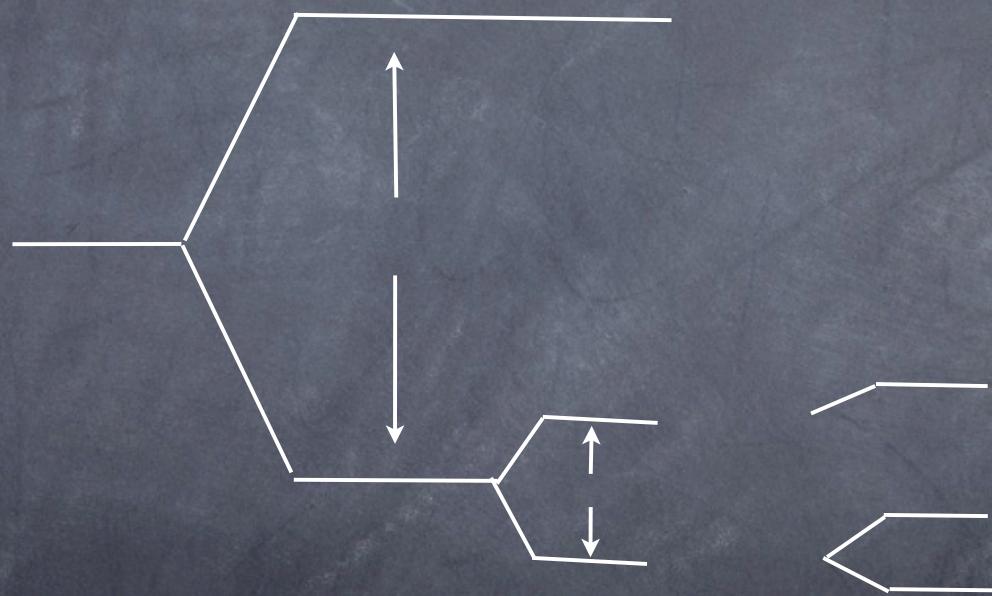
2#*/\$,-%. 1#,
3' /' ,4(. 5,678,
*9757: 6; 7,<,
=9>?57@A6>B,<,
/9A5>A667,<,

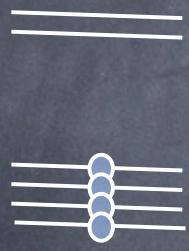
! " #\$/% ' ()*+, * -+. -\$/) -0* -+1)
2- ' \$3+-2-45\$)



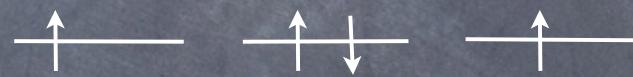








|



General Tight-binding Hamiltonian

Three-band Hubbard Model With SOC:

$$H = H_0 + H_{SO} + H_U$$

Kinetic Energy Terms: $\frac{1}{2m} \nabla^2$ (Energy terms)

$$\sum_{j,a\sigma} t_{ij}^{a\sigma} d_{i,a\sigma}^\dagger d_{j,a\sigma}$$

$$H_0 = \sum_{i \neq j}$$

Spin-Orbit Coupling Terms:

$$x s_x + l_y s_y + l_z s_z |b\sigma'\rangle d_{a\sigma}^\dagger d_{b\sigma'}$$

$$H_{SO} = \sum_{a\sigma} \sum_{b\sigma'} \zeta \langle a\sigma | l$$

Coulomb Interaction Terms:

$$\sum_{i < b, \sigma\sigma'} n_{a,\sigma} n_{b,\sigma'} - J_z \sum_{a < b, \sigma} n_{a,\sigma} n_{b,\sigma}$$

$$d_{b,\uparrow} + d_{a,\uparrow}^\dagger d_{a,\downarrow}^\dagger d_{b,\uparrow} d_{b,\downarrow} + h.c.)$$

$$H_U = U \sum_a n_{a,\uparrow} n_{a,\downarrow} + U'$$

$$- J_{xy} \sum_{a < b} \left(d_{a,\uparrow}^\dagger d_{a,\downarrow} d_{b,\downarrow}^\dagger d_{b,\uparrow} + h.c. \right)$$

M



Rotational Invariant Gutzwiller Approximation

Gutzwiller variational wavefunction:

$$|\Psi_G\rangle = \mathcal{P}|\Psi_0\rangle = \prod_{\mathbf{R}} \mathcal{P}_{\mathbf{R}} |\Psi_0\rangle$$

$$\mathcal{P}_{\mathbf{R}} = \sum_{\Gamma \Gamma'} \text{weight}_{\Gamma \Gamma'}(\mathbf{R}) \mathcal{P}_{\Gamma} = \sum_{\Gamma} \lambda(\mathbf{R}) |\Gamma, \mathbf{R}\rangle \langle \Gamma', \mathbf{R}'|$$

atomic hamiltonian H_U

gutzwiller variational function $\lambda(\mathbf{R})$ < 1 decreases energy

vector operator modify weight of local configuration

$|\Gamma\rangle$: eigenstates of

Gutzwiller Constraints:

$$\langle \Psi_0 | \mathcal{P}^\dagger \mathcal{P} | \Psi_0 \rangle = 1$$

$$\langle \Psi_0 | \mathcal{P}^\dagger \mathcal{P}_{n_{i\sigma}} | \Psi_0 \rangle = \langle \Psi_0 | n_{i\sigma} | \Psi_0 \rangle$$

Total Energy In Gutzwiller Wavefunction:

$$E^G = E_{kin}^G + E_{loc}^G = \langle \Psi_G | H_0 | \Psi_G \rangle + \langle \Psi_G | (H_U + H_{SO}) | \Psi_G \rangle$$

Computational Procedure(Fixed n^0 Algorithm):

Gutzwiller variational principle

$$\frac{\partial E^G}{\partial \langle \Psi_0 |} = \sum_{i \neq j} \sum_{\gamma \delta} \sum_{\alpha \beta} t_{ij} R_{\alpha \gamma} R_{\delta \beta} c_{i \gamma} c_{j \delta} |\Psi_0\rangle - \sum_{i \alpha} \eta_\alpha c_{i \alpha} c_{i \alpha} |\Psi_0\rangle = 0$$

$$\frac{\partial E^G}{\partial \lambda_{\Gamma\Gamma'}} = \sum_{\delta \beta} \left(\frac{\partial E_{kin}}{\partial R_{\delta \beta}} \frac{\partial R_{\delta \beta}}{\partial \lambda_{\Gamma\Gamma'}} + \frac{\partial E_{kin}}{\partial R_{\beta \delta}^\dagger} \frac{\partial R_{\beta \delta}^\dagger}{\partial \lambda_{\Gamma\Gamma'}} \right) + \frac{\partial E_{loc}}{\partial \lambda_{\Gamma\Gamma'}} + \sum_\alpha \eta_\alpha \frac{\partial n_\alpha^G}{\partial \lambda_{\Gamma\Gamma'}} = 0$$

The Lagrange parameters η_α come from Gutzwiller Constraint.

$$R_{\beta \delta}^\dagger = \frac{\text{Tr}(\phi^\dagger c_\alpha^\dagger \phi c_\gamma)}{\sqrt{n_\gamma^0 (1 - n_\gamma^0)}}$$

$$\phi_{II'} = \langle I | \hat{P} | I' \rangle \sqrt{\langle \Psi_0 | I' \rangle \langle I' | \Psi_0 \rangle}$$

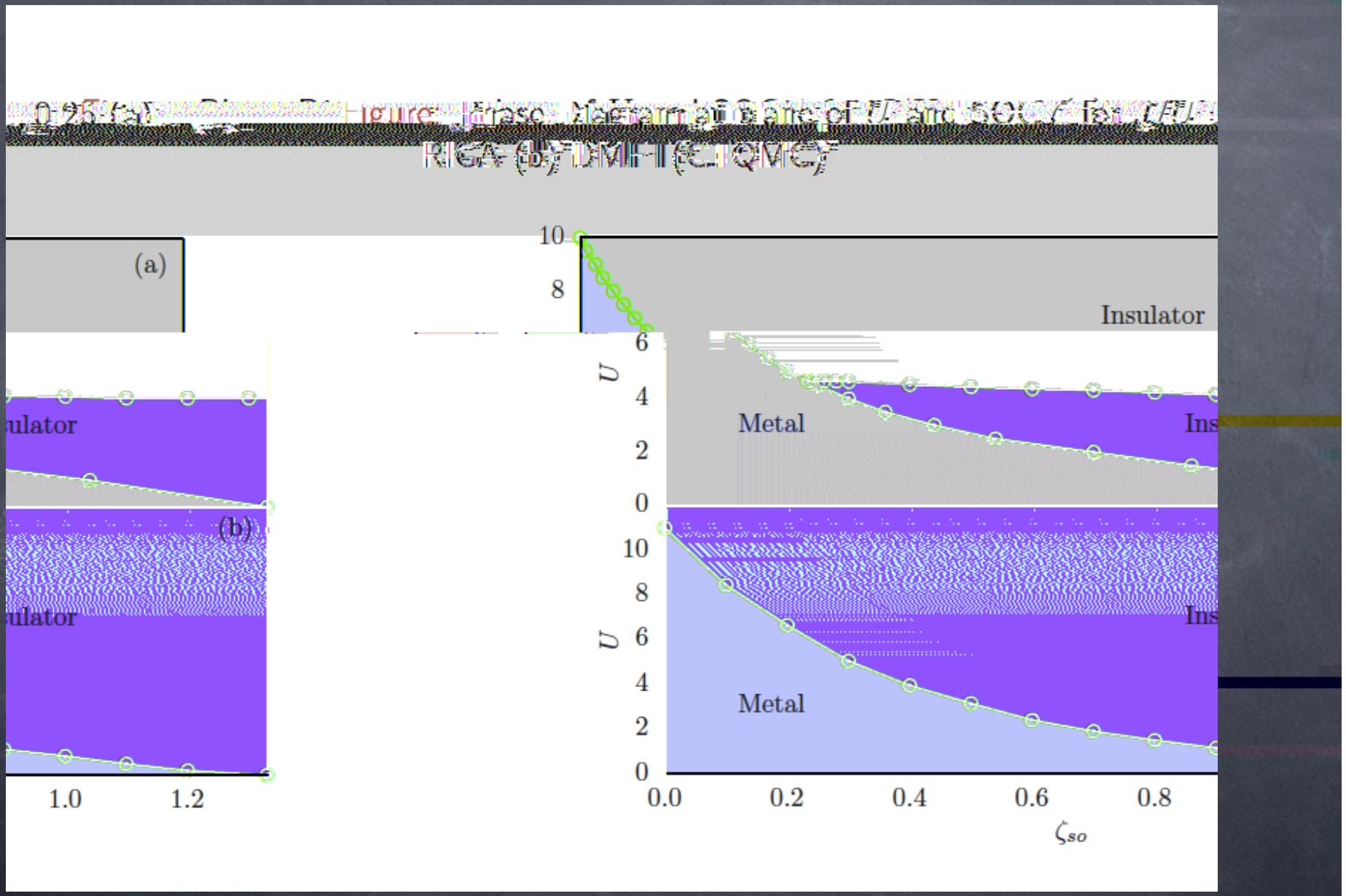


Figure: Energy and Quasiparticle weight as function of $0 \leq \delta n^0 \leq 1$ at

fixed SOC $\zeta = 0.7$ and different U values. Panel (d) is the corresponding DMRG result.

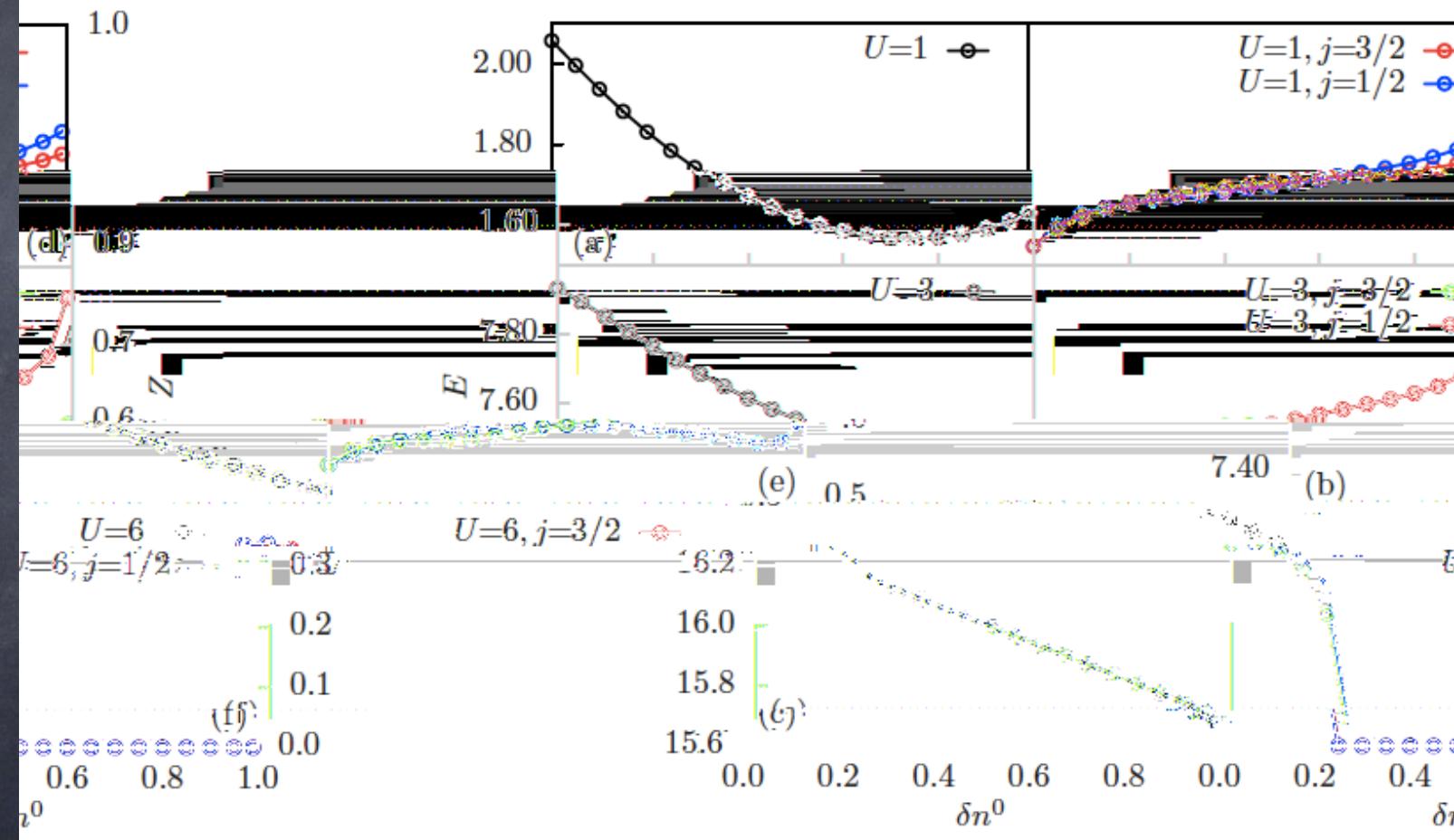


Figure: Expectation Value of L^2 , S^2 , J^2 as function of U with fix SOC $\zeta = 0.7$, Derived by DMFT+CTQMC

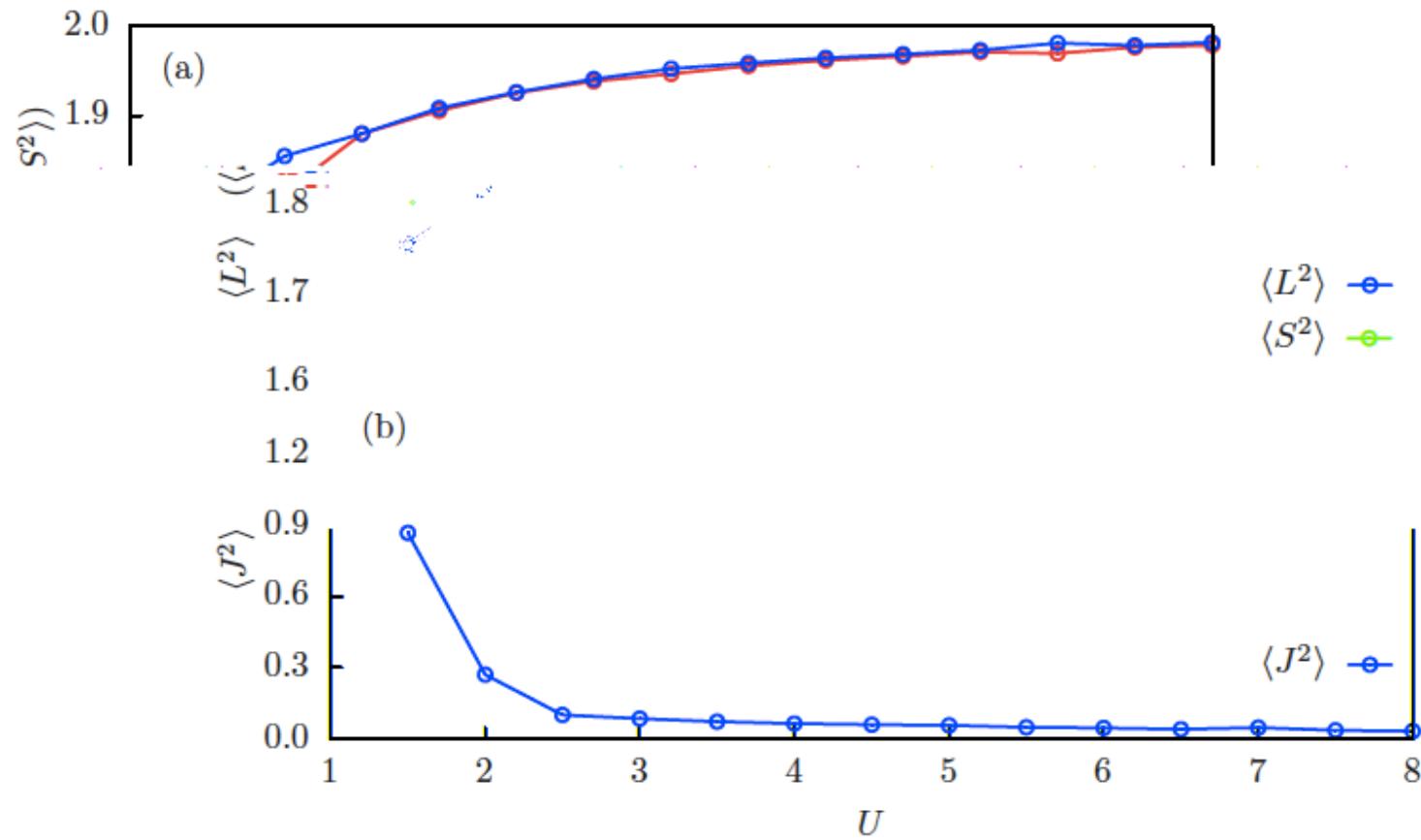
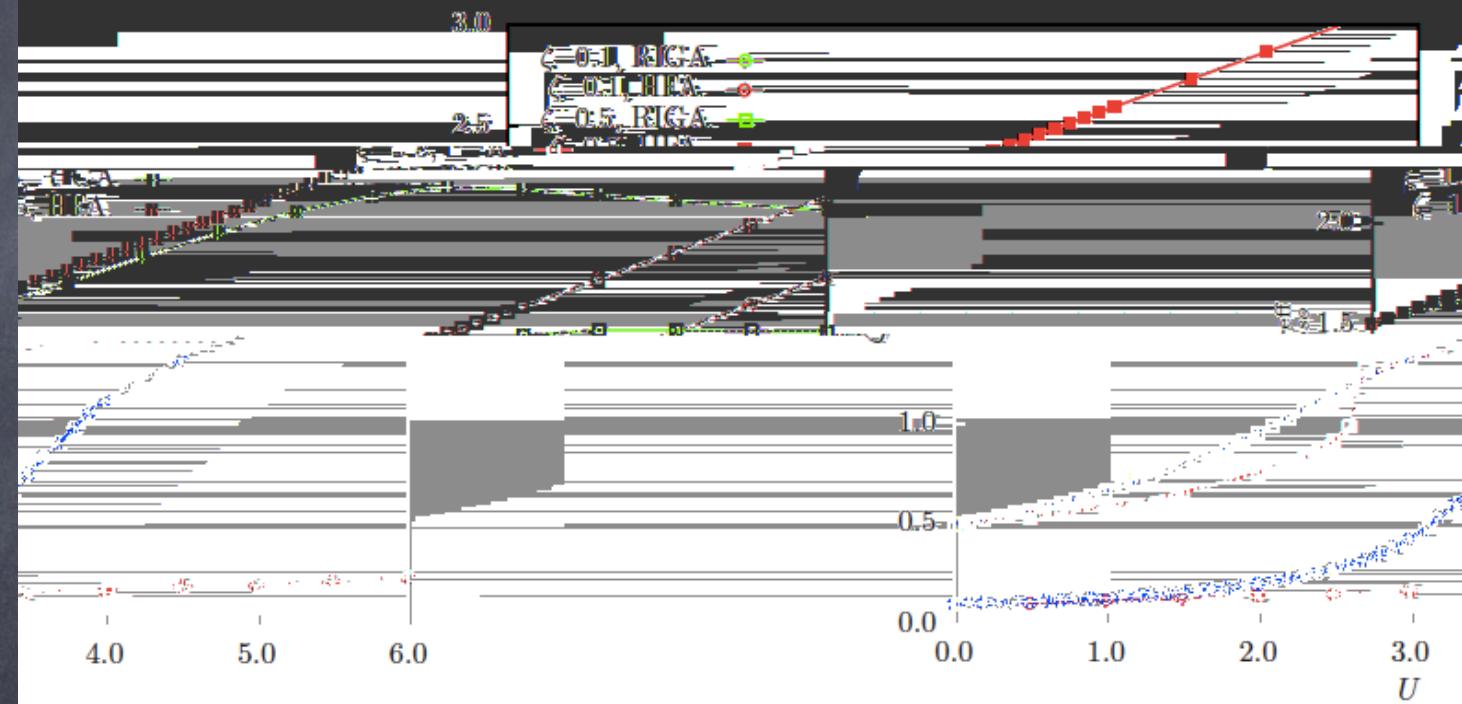
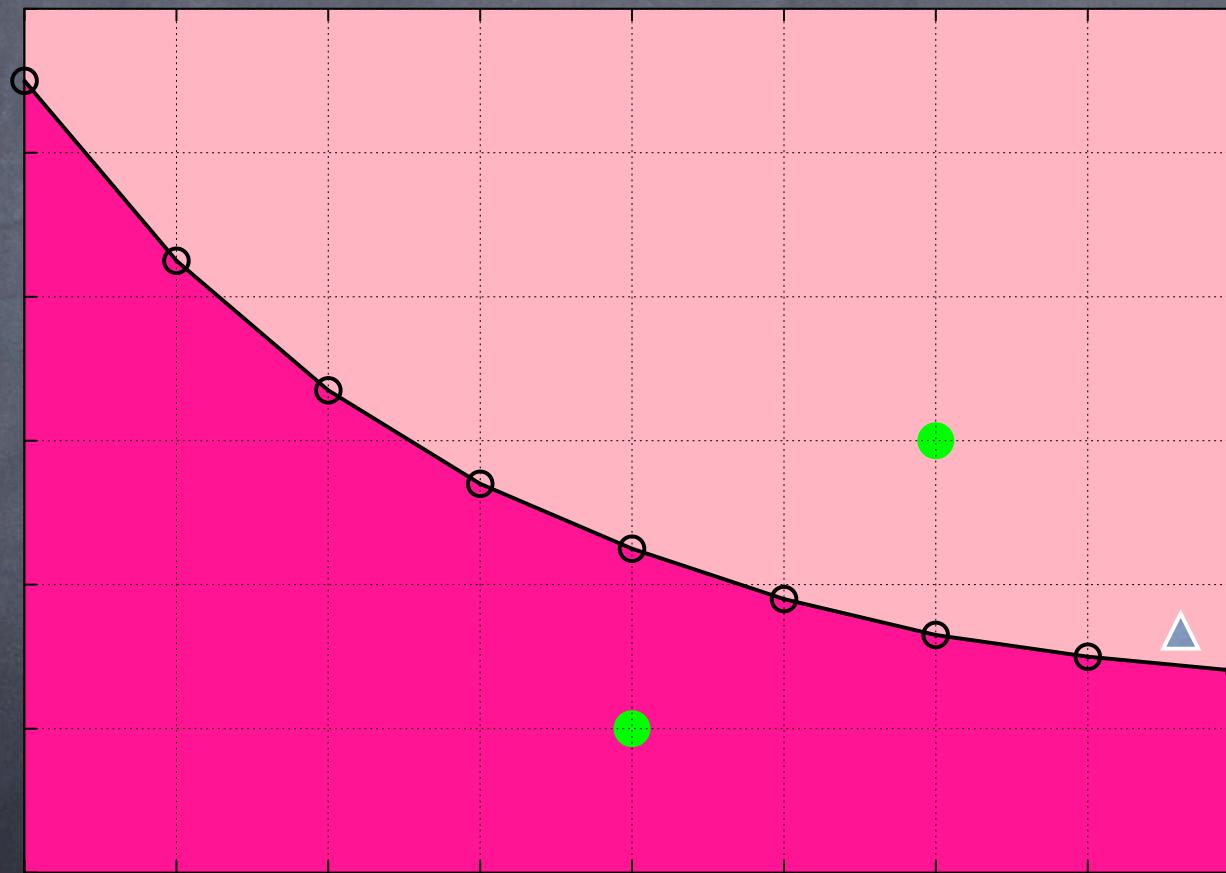


Figure: Effective spin-orbit coupling λ_{eff} as function U at fixed

$\zeta = 0.1, 0.5, 1.5$, derived by RPA and RIGA



$$\lambda_{eff} = \frac{\partial E_{int}}{\partial n_{1/2}^0} - \frac{\partial E_{int}}{\partial n_{3/2}^0}$$



λ

